Chapter 2

Introduction to Fluidization

2.1 Introduction

“The arrival time of a space probe traveling to Saturn can be predicted more accurately than the behavior of a fluidized bed chemical reactor!” Even though the above quotation (Geldart, 1986) is almost 20 years old it remains true in the new millennium of fluidization engineering. The difficulties in prediction stem in part from the complexity and ambiguity in defining the fundamental parameters such as size, shape and density of the particles. These parameters play an important role in the calculation and prediction of dynamic behavior in fluidized beds. Most physical properties of the particles are estimated indirectly, such as estimating particle shape by the bed voidage. All factors are explicitly and implicitly significant in the estimation of the behavior of fluidization operations. Although new technology is helping us to understand and give more precise prediction in fluidization, more research is still needed.

Either a gas or a liquid can fluidize a bed of particles. In this thesis, the focus is purely on gas-solid fluidization. This chapter is a short literature survey of fluidization, which will cover mainly the topics that are relevant to this work. More information about fluidization processes can be found in the references.

2.2 Review of Fluidization Basics

Fluidization is a process in which solids are caused to behave like a fluid by blowing gas or liquid upwards through the solid-filled reactor. Fluidization is widely used in commercial operations; the applications can be roughly divided into two categories, i.e.,

- physical operations, such as transportation, heating, absorption, mixing of fine powder, etc. and
- chemical operations, such as reactions of gases on solid catalysts and reactions of solids with gases etc.

The fluidized bed is one of the best known contacting methods used in the processing industry, for instance in oil refinery plants. Among its chief advantages are that the particles are well mixed leading to low temperature gradients, they are
suitable for both small and large scale operations and they allow continuous processing. There are many well established operations that utilize this technology, including cracking and reforming of hydrocarbons, coal carbonization and gasification, ore roasting, Fisher-Tropsch synthesis, coking, aluminum production, melamine production, and coating preparations. The application of fluidization is also well recognized in nuclear engineering as a unit operation for example, in uranium extraction, nuclear fuel fabrication, reprocessing of fuel and waste disposal.

2.3 Fluidization Regimes

When the solid particles are fluidized, the fluidized bed behaves differently as velocity, gas and solid properties are varied. It has become evident that there are number of regimes of fluidization, as shown in Figure 2.1. When the flow of a gas passed through a bed of particles is increased continually, a few vibrate, but still within the same height as the bed at rest. This is called a fixed bed (Figure 2.1A). With increasing gas velocity, a point is reached where the drag force imparted by the upward moving gas equals the weight of the particles, and the voidage of the bed increases slightly: this is the onset of fluidization and is called minimum fluidization (Figure 2.1B) with a corresponding minimum fluidization velocity, $U_{mf}$. Increasing the gas flow further, the formation of fluidization bubbles sets in. At this point, a bubbling fluidized bed occurs as shown in Figure 2.1C. As the velocity is increased further still, the bubbles in a bubbling fluidized bed will coalesce and grow as they rise. If the ratio of the height to the diameter of the bed is high enough, the size of bubbles may become almost the same as diameter of the bed. This is called slugging (Figure 2.1D). If the particles are fluidized at a high enough gas flow rate, the velocity exceeds the terminal velocity of the particles. The upper surface of the bed disappears and, instead of bubbles, one observes a turbulent motion of solid clusters and voids of gas of various sizes and shapes. Beds under these conditions are called turbulent beds as shown in Figure 2.1E. With further increases of gas velocity, eventually the fluidized bed becomes an entrained bed in which we have disperse, dilute or lean phase fluidized bed, which amounts to pneumatic transport of solids.
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2.4 Geldart’s Classic Classification of Powders

Not every particle can be fluidized. The behavior of solid particles in fluidized beds depends mostly on their size and density. A careful observation by Geldart (1973, 1978) is shown in Figure 2.2 in which the characteristics of the four different powder types were categorized as follows:
• Group A is designated as ‘aeratable’ particles. These materials have small mean particle size \(d_p < 30 \, \mu m\) and/or low particle density \(<~1.4 \, g/cm^3\). Fluid cracking catalysts typically are in this category. These solids fluidize easily, with smooth fluidization at low gas velocities without the formation of bubbles. At higher gas velocity, a point is eventually reached when bubbles start to form and the minimum bubbling velocity, \(U_{mb}\) is always greater than \(U_{mf}\).

• Group B is called ‘sandlike’ particles and some call it bubbly particles. Most particles of this group have size 150 \(\mu m\) to 500 \(\mu m\) and density from 1.4 to 4 \(g/cm^3\). For these particles, once the minimum fluidization velocity is exceeded, the excess gas appears in the form of bubbles. Bubbles in a bed of group B particles can grow to a large size. Typically used group B materials are glass beads (ballotini) and coarse sand.

• Group C materials are ‘cohesive’, or very fine powders. Their sizes are usually less than 30 \(\mu m\), and they are extremely difficult to fluidize because interparticle forces are relatively large, compared to those resulting from the action of gas. In small diameter beds, group C particles easily give rise to channeling. Examples of group C materials are talc, flour and starch.

• Group D is called ‘spoutable’ and the materials are either very large or very dense. They are difficult to fluidize in deep beds. Unlike group B particles, as velocity increases, a jet can be formed in the bed and material may then be blown out with the jet in a spouting motion. If the gas distribution is uneven, spouting behavior and severe channeling can be expected. Roasting coffee beans, lead shot and some roasting metal ores are examples of group D materials.

Geldart’s classification is clear and easy to use as displayed in Figure 2.2 for fluidization at ambient conditions and for \(U\) less than about \(10 \cdot U_{mf}\). For any solid of a known density \(\rho_s\) and mean particle size \(d_p\) this graph shows the type of fluidization to be expected. It also helps predicting other properties such as bubble size, bubble velocity, the existence of slugs etc.
2.5 Bubbling Fluidized Beds

When talking about a fluidized bed, mostly one refers to a bubbling fluidized bed type as shown in Fig. 2.1C. Gas fluidized beds are characterized by the ‘bubbles’ which form at superficial gas velocities only slightly higher than that required to just fluidize the particles. This type of fluidization has been called ‘aggregative fluidization’, and under these conditions, the bed appears to be divided into two phases, the bubble phase and the emulsion phase. The bubbles appear to be very similar to gas bubbles formed in a liquid and they behave in a similar manner. The bubbles coalesce as they rise through the bed.

The movement of particles in fluidized beds is known to depend largely on bubbles rising through the bed. Therefore, special attention is paid to bubbles and their properties. To give an impression of the processes occurring inside a fluidized bed reactor, the principles of fluidization, the formation of bubbles, their path through the bed, the way they transport particles concerning gas fluidized bed and important parameters are described below.

2.5.1 Minimum Fluidization Velocity

The superficial gas velocity at which the bed of powder is just fluidized, is normally called the minimum fluidization velocity or designated by \( U_{mf} \). This state of incipient fluidization can be described by an equation giving the pressure drop in a gas flowing through a packed bed, such as the so-called Ergun equation:
in which $\Delta P$ is equal to the bed weight per unit cross-sectional area, and the particle sphericity, $\phi_s$, is defined as the surface area of a volume equivalent sphere divided by the particle’s surface area.

When applying the Ergun equation, one has to know the minimum fluidization voidage, $\varepsilon_{mf}$, although it is frequently an unknown. Wen and Yu (1966) developed an expression for the minimum fluidization velocity for a range of particle types and sizes by assuming the following approximations to hold based on experimental data:

$$\frac{1-\varepsilon_{mf}}{\phi_s^3\varepsilon_{mf}^3} = 11 \text{ and } \frac{1}{\phi_s^3\varepsilon_{mf}^3} = 14.$$ 

They combined these with the Ergun equation and obtained the relation:

$$\text{Re}_{mf} = \frac{d_p \cdot U_{mf} \cdot \rho_g}{\mu} = \sqrt{33.7^2 + 0.0408 \left( \frac{d_p^3 \cdot \rho_g \cdot (\rho_s - \rho_g) \cdot g}{\mu^2} \right)} - 33.7. \quad (2.2)$$

Leva (1959) obtained empirically another widely used expression:

$$U_{mf} = 7.90 \times 10^{-2} d_p^{1.82} (\rho_s - \rho_f)^{0.04} \mu_f^{-0.88} \quad (2.3)$$

This equation is valid for $\text{Re}_{mf} \leq 10$, whereas for higher values of $\text{Re}_{mf}$ a correction factor must be applied.

### 2.5.2 Bubble Size

The mean size of the bubble population in fluidized beds increases with height above the distributor plate due to coalescence of bubbles. Researchers have attempted to predict the size of bubbles, not only the variation in mean size, but also the distributions of the diameters and volumes.
As far as the mean size is concerned, Geldart (1972) used the expression of Kato and Wen (1969) for the initial bubble size at the gas distributor. He asserted that a porous plate distributor behaves as a distributor plate with 1 hole per 10 cm², and added his own empirical expression for the bubble growth with bed height due to coalescence:

\[
D_B = \frac{1.43}{g^{0.2}} \left( \frac{(U - U_{mf}) \pi D_{bed}^2}{4 N_0} \right)^{0.4} + 2.05(U - U_{mf})^{0.94} h \quad (2.4)
\]

where \(D_B\) is the bubble diameter, \(D_{bed}\) is the diameter of the bed and \(N_0\) is the number of holes in the distributor plate.

A number of other relationships have been proposed since then, some of which will be given and used in later chapters.

### 2.5.3 Bubble Wake

When a bubble rises, it carries some amount of solids inside as seen in Fig. 2.3. This is called ‘wake’. The formation of a wake follows directly when the bubble forms. Hence, the bubble picks up most of its solids at the bottom of the bed as it leaves the distributor plate. An idealized bubble has an upper surface that is approximately spherical, with a radius of curvature \(r\), and a wake at the bottom, with wake angle \(\theta_w\) as shown in Figure 2.3.

![Figure 2.3 A ideally spherical bubble (Geldart, 1962)](image-url)
The bubble size is often expressed in terms of the volume equivalent diameter, $D_{eq}$, and can be calculated as $D_{eq} = \left( \frac{6V_b}{\pi} \right)^{\frac{1}{3}}$, where $V_b$ is a bubble volume.

Several researchers, for example Rowe and Widmer (1972) and Rowe and Yacono (1976) investigated the relationship of wake volume of a bubble as a function of its parameters, such as a bubble diameter, wake angle etc. by using X-ray techniques. The wake angle was also estimated by Naimer et al. (1982) who gave an empirical relation for the variation of the wake angle with the bubble diameter. Hoffmann (1983) proposed an improved equation for wake angle calculation:

$$\theta_w = 160 - 160 \exp(-60D_B)$$  \hspace{1cm} (2.4)

where $D_B$ is the bubble diameter and $\theta_w$ is expressed in degrees. In some symposium publications (Hoffmann, 1991), a constant value of 55 is used instead of 60 in Equation 2.4, although the quality of the fit to the experimental data is essentially the same for the two constants. Equation 2.4 will be applied throughout this thesis.

The other important parameter is the ratio of the volumes of the wake and the sphere and this is called the wake fraction $f_w$:

$$f_w = \frac{3V_w}{4\pi r^3}$$  \hspace{1cm} (2.5)

The wake volume, $V_w$ can be calculated as a function of $\theta_w$, $D_B$ and $r$. $V_w$ is taken as the volume of that part of the circumscribing sphere not occupied by the bubble void for an approximation. Generally, moving from group A through group B to group D, the wake fraction decreases and therefore the volume of particulate phase transported per unit bubble volume decreases (Geldart, 1986). The wake of the bubble in beds of spherical material is roughly 30% of the bubble volume (Yates, 1983).

2.5.4 Bubble Rise Velocity

The rise velocity of a large spherical cap bubble in a liquid is dependent on the radius of curvature at the nose of the bubble as described by Davies and Taylor (1950):
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\[ U_b = 0.667 \sqrt{g \cdot r} \]  

(2.6)

A semi-empirical relation in terms of the volume-equivalent diameter is:

\[ U_b = 0.711 \sqrt{g \cdot D_{eq}} \]  

(2.7)

This expression is widely used for calculations of the velocity of rise of single bubbles in fluidized beds.

2.5.5 Bubble Flow Rate and the Two-Phase Theory

According to the two-phase theory of fluidization proposed by Toomey and Johnstone (1952) and developed by Davidson and Harrison (1963), all gas in excess of that needed for minimum fluidization passes through the bed as bubbles. The particulate phase remains at minimum fluidizing conditions, which means that the voidage, not counting the bubbles, remains practically \( \varepsilon_{mf} \). The visible flow rate in a fluidized bed \( Q_b \), defined as the rate at which bubble volume crosses any section \( A \) in the bed, is then approximately equal to the excess gas flow above that required for minimum fluidization (Davidson and Harrison, 1963):

\[ \frac{Q_b}{A} = U - U_{mf} \]  

(2.8)

2.5.6 The Davidson Model

The movement of both gas and solid caused by the rise of bubbles can be described by the Davidson model (Davidson, 1961), assuming that the bubble is solid free and spherical, that particles behave like an incompressible fluid of bulk density \( \rho_s (1 - \varepsilon_{mf}) \) and that the gas in the emulsion phase flows as an incompressible viscous fluid that obeys Darcy’s law.

Davidson (1961) described the gas flow in terms of a stream function and found that the bubble velocity affects the geometry of the stream function. If the bubble moves slower than the gas in the emulsion phase, this gas uses the bubble as a shortcut, entering the bubble at the bottom and leaving it at the top. Some gas circulates with the bubble, moving upward with it. This circulation increases with the bubble rise velocity. If the bubble moves faster than the gas in the emulsion phase, all gas entering the bubble circulates and a “cloud” of recirculating gas is formed around the bubble, while the rest of the gas in the bed moves past it without
mixing. The gas in the bubble and the cloud is then essentially isolated from the rest of the gas in the bed except for dispersion mass transfer.

Other extensions to the Davidson model can be made; for example, some workers claim that some particles fall through the bubble due to a thin, unstable layer of larger voidage around the upper boundary of the bubble, but this may be a feature of two-dimensional beds only. Another property of bubbles in dense beds is their break-up when they become too large. If the rise velocity of the bubble exceeds the terminal velocity of the particles (their free-fall velocity), the bubble becomes unstable and will break up into smaller bubbles. There are other models for the bubble movement in fluidized beds, which are more realistic than Davidson’s model for example, by Jackson (1963) and Murray (1965). However, the simple treatment of Davidson’s model is still essentially applied in many circumstances.

2.5.7 Flow Pattern of Fluidization Bubbles

As bubbles rise through the bed, they coalesce to form bigger bubbles and when they become too large, they split (see Figure 2.4). The average bubble size equilibrates at about the maximum stable size. The location in the bed where the equilibrium size is attained depends on the kind of particles. For group A particles, the maximum stable diameter is relatively small, therefore the average bubble size stabilizes close to the distributor plate and remains constant through the rest of the bed. The maximum stable diameter for group B particles is larger and the equilibrium is reached typically only in the upper levels of the bed. The bubbles in group D particle beds behave differently; they do not rise as individual bubbles, but as horizontally associated swarms.

Bubbles can coalesce in two ways, by incorporating a bubble in front or by moving side-wards into the track of another bubble and then incorporating it. At the wall of the bed, bubbles can only move inwards, while other bubbles can move in any horizontal direction. The result is an active zone away from the wall, which intensifies and moves closer to the axis with increasing distance from the distributor plate. Solid particles are dragged up by the bubbles and, by continuity, will move downwards in regions with lower bubble densities.

As a consequence of fewer bubbles being close to the wall, there is a predominantly downward flow of particles near the wall, which, once established, maintains the tendency for bubbles to move inwards. The overall circulation is upwards near the axis and downwards near the wall in higher regions; the converse seems to be the case in the lower regions.
The circulation pattern can be modified by internals, like tubes or baffles or disturbed by mal-distribution at the distributor plate. Apart from the mal-distribution caused by the plate that disturbed the flow pattern, Merry and Davidson (1973) found a phenomenon called gulf streaming. The gulf streaming phenomenon is caused by a cross-sectionally non-uniform bubble flow, causing a general upward material flow in one part of the bed, and downward in the other. Due to this effect much more material is brought to the top of the bed by the bubble flow than would be expected on basis of the flow in the wake phase itself, and thus the downward flow in the bulk is also higher. Gulf-streaming will cause the fluidization bubbles to move faster than one would expect from the single bubble velocity. On the other hand, a certain slip between the bubbles and the dense phase in the region of upward motion can be expected. Gulf-streaming will always take place in a fluidized bed to some extent. More discussions about gulf-streaming effects can be found in Chapter 4.

### 2.5.8 Bed Expansion

With an average bubble velocity \( <U_b> \) the average fraction of the bed area occupied by bubbles can be given as:

\[
\varepsilon_b = \frac{Q_b}{A_{bed} \cdot <U_b>}. \tag{2.9}
\]

Assuming that the void fraction of the particulate phase equals the void fraction at minimum fluidization, hence all gas in excess of that needed for minimum
fluidization passes through the bed as bubbles, the height \( h \) of the bed can be derived:

\[
h - h_{mf} = \int_0^h \frac{Q_b}{A_{bed} \cdot <U_b>} dz.
\] (2.10)

If the assumption can be made that the bubble velocity is constant throughout the bed, the bed height can be estimated from:

\[
\frac{h - h_{mf}}{h_{mf}} = \frac{U - U_{mf}}{U_b}.
\] (2.11)

The expansion of the bed then equals the fraction of the bed consisting of bubbles:

\[
\varepsilon_b = \frac{h - h_{mf}}{h}.
\] (2.12)

In practice, the bubble fraction is a bit lower than this theoretical value.

### 2.6 Particle Transportation

Several mechanisms have been proposed to describe the movement of particles through a fluidized bed. Mechanisms governing the vertical particle transport processes in batch freely bubbling fluidized beds were first proposed by Rowe and Partridge (1962):

- Transport upwards in the wakes of fluidization bubbles and deposition on the bed surface
- Transport down to compensate for this (the combination of these two they called ‘circulation’) and
- Dispersion due to disturbance of the bed material by fluidization bubbles.

In addition, the wake and drift exchange solids with the emulsion phase from experimental findings of Gibilaro and Rowe (1974), Chiba and Kobayashi (1977), Chiba et al. (1979) and Nienow and Chiba (1985).

Mixing of solids occurs in both axial and radial directions. However, vertical solid mixing is generally many times faster than that due to lateral motion (Kunii and Levenspiel, 1991). More details of each mechanism are described below.
2.6.1 Solid Circulation

Solid circulation is mainly determined by the gas velocity. At low gas velocities solids circulation is negligible. In more vigorously bubbling beds, circulation becomes appreciable and the absolute upward gas velocity through the emulsion phase does not equal the minimum fluidizing velocity anymore. Here, the velocity of the downward flowing solids has to be taken into account.

Not only gas velocity, but also particle properties like shape, size, density, stickiness, and size distribution influence the mechanisms of axial and radial transport of particles within the bed. As mentioned previously, solids move in the vertical direction largely by being carried up by bubbles and carried down to the distributor by the bubble-free flow of particulate phase material. The upward movement is rapid (with the velocity of the bubbles) and the downward movement relatively slow.

2.6.2 Dispersion

Dispersion is one of the mechanisms of solids mixing in a fluidized bed. It occurs due to the disturbance of the bed material caused by the motion of the bubbles. Although it is thus a discrete process, linked to the motion of each individual bubble, it can be described as a continuous dispersion process and modeled using the diffusion equation:

\[
\frac{\partial c}{\partial t} = D \frac{\partial^2 c}{\partial x^2}
\]  

(2.13)

This equation is called Fick’s second law of diffusion or the diffusion equation, where \( D \) is a dispersion coefficient and \( c \) the concentration of the diffusing species is a function of both \( x \) and \( t \).

In this thesis, the method for calculating the dispersion coefficient \( D \) is by calculating the number and size of fluidization bubbles going through a given cross-section of the bed during a given time interval of \( t \) seconds and using empirical literature data for the particle drift caused by a single bubble.

From equation 2.13, the solution to the one-dimensional diffusion of particles, the concentration of which initially forms a Dirac delta function in \( x = 0 \) is:
\[ c(x,t) = \frac{1}{\sqrt{2\pi \mathcal{D} t}} e^{-\frac{x^2}{4\mathcal{D} t}}, \] where \( c(x,t) \) is the normalized particle concentration.

\( c(x,t) \, dx \) can, in the case of particles dispersing from a plane, be seen as the fraction of the particles with position \( x + \frac{1}{2} dx < x < x - \frac{1}{2} dx \) at time \( t \).

When comparing this with the density of the normal distribution,

\[ c(u) = \frac{1}{\sigma \sqrt{2\pi}} e^{-\frac{u^2}{2\sigma^2}}, \]

we see that the two are the same with \( \sigma^2 = 2 \mathcal{D} t \).

Since the mean is zero, the variance \( \sigma^2 \) is the expected value of \( u^2 \): \( \int_{-\infty}^{\infty} c(u)u^2 \, du \), so that:

\[ 2\mathcal{D} t = \int_{-\infty}^{\infty} c(x,t) x^2 \, dx \]

or in other words: \( 2\mathcal{D} t \) is the expected value of \( x^2 \), which is also the mean square particle displacement at time \( t \).

In what follows, we will use the mean square particle displacement per second, \( D = 2\mathcal{D} \), as a measure of dispersion. This is in line with what is common in the mathematical literature, but not in the engineering literature.

After that we calculate the particle displacement caused by one bubble from the empirical profiles given by Chiba \textit{et al.} (1976) and then calculate the cross-sectional mean of the square displacement. Taking \( t \) as the reciprocal of the bubble frequency at the given level in the bed, the dispersion coefficient used in our stochastic model is thus calculated.

Only axial dispersion is taken into account. Horizontal and vertical diffusion differ, the axial, or vertical, dispersion coefficient being appreciably higher than the radial dispersion coefficient.

An alternative to the above outlined concepts and method for estimating \( D \) is based on the notion of particle flow in and out of the bubble wake. This concept and the resulting expressions for the radial and axial dispersion coefficients are described below.
2.6.3 An Alternative Concept: Solid Exchange Between the Wake and the Emulsion

According to the extensions of bubbling bed model (the Davidson model), particles travel upwards in a wake and downwards in the particulate phase. As described before, the idealized bubble carries up solids in a closed wake, with the solids circulating within it. However, models have been proposed that include interchange of solids between the wake and the particulate phase. It was suggested that in beds of fast rising bubbles, the downward moving particles in the cloud around the bubble are swept into the wake and are fluidized there by the circulating gas. In the wake they are uniformly mixed by circulation and, by continuity, particles leave the wake at the same rate.

The coefficient of interchange of solids between the cloud-wake region and the particulate phase, based on bubble size, was derived by Yoshida and Kunii (1968):

$$K_w = \frac{3 \cdot (1 - \varepsilon_{mf}) \cdot U_{mf}}{(1 - \varepsilon_b) \cdot D_b \cdot \varepsilon_{mf}}. \quad (2.14)$$

The circulation in the wake gives rise to radial mixing of solids. Solids farther from the bubble move aside somewhat as the bubble passes by and then return close to their original position; for them, radial mixing can be neglected.

Using terms of the bubbling bed model and the solids interchange model from Kunii and Levenspiel, 1991, the following axial and radial dispersion coefficient, $D_{sa}$ and $D_{sr}$ respectively, can be found:

$$D_{sa} = \frac{(f_w \varepsilon_b (1 - \varepsilon_{mf}))^2 U_b^2}{\varepsilon_b K_w (1 - \varepsilon_b)(1 - \varepsilon_{mf})}. \quad (2.15)$$

Substituting $K_w$ from equation 2.14 and simplifying, thus;

$$D_{sa} = \frac{f_w^2 \varepsilon_{mf} \varepsilon_b D_b U_b^2}{3U_{mf}}. \quad (2.16)$$

The above model for the solid exchange, Equation (2.14), was refined in the light of experimental results by Chiba et al. (1976, 1979). They have developed the following equations:
Solid mixing in a freely bubbling fluidized bed is caused not only by the vertical movement of bubbles and bursting of bubbles at the bed surface, but also by the lateral motion of bubbles as a result of the interaction and coalescence of neighboring bubbles. However, the lateral mixing of solids which is augmented by the lateral motion of bubbles is relatively small compared to the vertical motion of solids. Our stochastic model is one-dimensional at the present time, and we therefore do not consider the issue of radial mixing.

This a different concept in that the dispersion coefficient accounts for dispersion both due to the bubble's stirring action and due to take-up of particles in the bubble wake. The approach used in this thesis is to calculate a dispersion coefficient only on basis of the stirring action, and take the transport in bubble wakes into account in jumps to the bed surface. In the latter approach the material exchange between the bubble wake and bulk is assumed to be zero, although the model can easily be modified to take exchange with the bulk into account.

2.7 Particle Mixing and Segregation

Until now we have implicitly assumed that the bed particles are uniform. However, if the bed particles differ in physical properties, notably size and density, then segregation can take place.

Segregation of a binary mixture of particles occurs when there is a substantial difference between their drag per unit weight. A high drag per unit weight makes the particles move upwards, whereas particles with a low drag per unit weight will tend to sink to the bottom. These two types of particles are called flotsam and jetsam, respectively.

A quantitative measure for segregation is given by Tanimoto et al. (1981) in terms of the segregation distance $Y$, made dimensionless with the radius of the fluidization bubble. It characterizes the distance over which the jetsam particles sink as a single bubble passes by. The segregation distance was modified by Hoffmann and Romp (1991) to ensure that $Y$ becomes zero when the bed particles are uniform:

$$K_w = \frac{4}{\pi} \frac{U_{mf}}{\epsilon_{mf} D_B}$$ for a 2-dimensional bubble \hspace{1cm} (2.17)

$$K_w = \frac{3}{2} \frac{U_{mf}}{\epsilon_{mf} D_B}$$ for a 3-dimensional bubble \hspace{1cm} (2.18)
\[ Y = 0.8 \left( \frac{\rho_j}{\rho_f} \right) \left( \frac{d_j}{d_f} \right)^{\frac{1}{3}} - 0.8 \]  

(2.19)

This shows that the particle density difference is more dominant in segregation than the size difference. The superficial segregation velocity depends on the segregation distance as follows:

\[ v_{segr} = \frac{3}{4} \cdot Y \cdot \left( U - U_{mf} \right) \]  

(2.20)

The competitive mechanisms of segregation and mixing occur simultaneously producing equilibrium through the bed. Radial distribution is essentially uniform and axial distribution varies with height (Gibilaro and Rowe, 1973). As the gas velocity increases, the segregation pattern changes from a pure jetsam layer at the bottom through a gradient in jetsam concentration to a uniform mixture.

As the composition of the mixture of particles varies with bed height, so does the minimum fluidization velocity. In some cases, segregation leads to defluidization in the bottom of the bed. The segregating fluidized bed containing two types of particles has been modeled by Gibilaro and Rowe (1974), who recognized four physical mechanisms: overall particle circulation, interchange between bulk and wake phases, axial spreading and a relative segregating flow rate. The first three are modes of mixing and only the last mechanism distinguishes jetsam and flotsam. Segregation, like mixing, depends almost solely on bubbles.

Naimer et al. (1982) suggested a segregation mechanism where jetsam can overtake flotsam by falling rapidly through bubbles. Jetsam particles also descend faster through the temporarily disturbed region with lower density below each bubble. This mechanism is illustrated in Fig. 2.5, where a jetsam layer is disturbed by a bubble moving through it.
Hartholt et al. (1996) found by visual observation that jetsam particles, which are not fully supported by the gas stream, rest on a grid-like structure formed by flotsam particles due to their lasting contacts. These structures are sheared as bubbles pass, resulting in a downward migration of the jetsam. It was found that the effect of interchange between the bulk phase and the wake phase is very small and can generally be neglected. Axial spreading was found to be only important at high gas velocities or in weakly segregating systems. At high jetsam concentrations, the bubble momentum can carry the jetsam-rich wake through the flotsam to the top of the bed and deposits the jetsam on the surface.

Inserting horizontal baffles in the fluidized bed enhances segregation of larger and especially denser particles, and causes a decrease in the axial mixing of particles (Hartholt et al., 1996, 1997). Experiments showed that as a bubble passes through a baffle, part of the wake material is left underneath the baffle (van Dijk et al., 1998). For vigorous fluidization, sometimes down-flow through the baffles is insufficient, causing the bed to become multi-stage fluidized. At low velocities the baffles have no significant influence on the mean bubble size or velocity. More details about fluidized beds with baffles can be found in Chapters 5 and 8.

### 2.8 Notation

<table>
<thead>
<tr>
<th>Symbol</th>
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<tr>
<td>$A$</td>
<td>cross-sectional area</td>
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<tr>
<td>$A_{bed}$</td>
<td>bed vessel cross-sectional area</td>
</tr>
<tr>
<td>$C_s$</td>
<td>solid concentration</td>
</tr>
<tr>
<td>$D_B$</td>
<td>effective bubble diameter</td>
</tr>
<tr>
<td>$D$</td>
<td>dispersion coefficient</td>
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<tr>
<td>$D_{bed}$</td>
<td>bed diameter</td>
</tr>
<tr>
<td>$D_{ad}$</td>
<td>axial dispersion coefficient</td>
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\[ D_{dr} = \text{radial dispersion coefficient} \]
\[ D_{eq} = \text{the diameter of a volume equivalent sphere} \]
\[ d_p = \text{particle diameter} \]
\[ \overline{d_p} = \text{mean particle diameter} \]
\[ f_d = \text{drift fraction} \]
\[ f_w = \text{wake fraction} \]
\[ h = \text{height in the bed} \]
\[ h_{mf} = \text{height of the bed at } U_{mf} \]
\[ K_w = \text{solid exchange coefficient between wake and emulsion phase} \]
\[ L = \text{bed height} \]
\[ N_0 = \text{number of holes of a distributor plate} \]
\[ \Delta P = \text{pressure drop} \]
\[ Q_b = \text{visible gas flow rate in a fluidized bed} \]
\[ r = \text{radius of curvature of the bubble front} \]
\[ \text{Re}_{mf} = \text{Reynolds number of particle at minimum fluidization condition} \]
\[ \text{Re}_b = \text{Reynolds number of bubbles} \]
\[ t = \text{time} \]
\[ U = \text{velocity} \]
\[ \langle U \rangle = \text{average bubble velocity} \]
\[ U_b = \text{bubble velocity} \]
\[ U_0 = \text{superficial fluid velocity} \]
\[ U_{mf} = \text{superficial fluid velocity at minimum fluidizing conditions} \]
\[ v_{segr} = \text{superficial segregation velocity} \]
\[ V_b = \text{a bubble volume} \]
\[ V_w = \text{a wake volume} \]
\[ Y = \text{dimensionless segregation distance} \]

Greek symbols:

\[ \mu = \text{viscosity of fluid} \]
\[ \varepsilon = \text{void fraction} \]
\[ \varepsilon_b = \text{fraction of bed occupied by bubbles} \]
\[ \varepsilon_{mf} = \text{void fraction at minimum fluidization condition} \]
\[ \theta_w = \text{wake angle} \]
\[ \rho = \text{density} \]
\[ \rho_f = \text{flotsam density} \]
\[ \rho_j = \text{jetsam density} \]
\[ \rho_s = \text{solid density} \]
2.9 References


Hoffmann, A.C., Ph.D. thesis, University College London, Department of Chemical and Biochemical Engineering, 1983.


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