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Order fulfillment: warehouse and inventory models

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university of
 groningen

Order fulfillment: warehouse and inventory models

PhD thesis

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 on the authority of the
 Rector Magnificus Prof. E. Sterken
 and in accordance with
 the decision by the College of Deans.

This thesis will be defended in public on

Monday 1 July 2019 at 14.30 hours

by

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Preface

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