We present a detailed analysis of the specific star formation rate–stellar mass (sSFR–$M_*$) of $z \leq 0.13$ disc central galaxies using a morphologically selected mass-complete sample ($M_* \geq 10^{9.5} M_\odot$). Considering samples of grouped and ungrouped galaxies, we find the sSFR–$M_*$ relations of disc-dominated central galaxies to have no detectable dependence on host dark-matter halo (DMH) mass, even where weak-lensing measurements indicate a difference in halo mass of a factor $\gtrsim 5$. We further detect a gradual evolution of the sSFR–$M_*$ relation of non-grouped (field) central disc galaxies with redshift, even over a $\Delta z \approx 0.04 (\approx 5 \times 10^8 \text{yr})$ interval, while the scatter remains constant. This evolution is consistent with extrapolation of the ‘main sequence of star-forming-galaxies’ from previous literature that uses larger redshift baselines and coarser sampling. Taken together, our results present new constraints on the paradigm under which the SFR of galaxies is determined by a self-regulated balance between gas inflows and outflows, and consumption of gas by star formation in discs, with the inflow being determined by the product of the cosmological accretion rate and a fuelling efficiency $\dot{M}_{h,\text{halo}} \zeta$. In particular, maintaining the paradigm requires $\dot{M}_{h,\text{halo}} \zeta$ to be independent of the mass $M_{\text{halo}}$ of the host DMH. Furthermore, it requires the fuelling efficiency $\zeta$ to have a strong redshift dependence ($\propto (1 + z)^{2.7}$ for $M_* = 10^{10.3} M_\odot$ over $z = 0–0.13$), even though no morphological transformation to spheroids can be invoked to explain this in our disc-dominated sample. The physical mechanisms capable of giving rise to such dependencies of $\zeta$ on $M_{\text{halo}}$ and $z$ for discs are unclear.

Key words: gravitational lensing: weak – galaxies: evolution – galaxies: groups: general – intergalactic medium – galaxies: ISM – galaxies: spiral.

1 INTRODUCTION

Over the past decade, a wide range of observational work has established the existence of a tight relation between the star formation rate (SFR, or $\Phi_*$) and the stellar mass ($M_*$) of star-forming galaxies, with this relation having been in place at least as early in the history
of the Universe as \( z \approx 2.5 \) and maybe even as early as \( z \approx 6 \) (Noeske et al. 2007; Elbaz et al. 2007; Wuyts et al. 2011; Whitaker et al. 2012; Speagle et al. 2014). This relation—widely referred to as the ‘main sequence of star-forming galaxies’ (MS)—takes the form of a power law with normalization and slope evolving with redshift \( z \), while the scatter \(^1\) remains roughly constant at \( \Delta z \approx 0.3 \) dex. Notably, it has also been demonstrated that the MS is preferentially populated by disc-dominated galaxies, and has been so since at least \( z \approx 2 \) (Wuyts et al. 2011). Accordingly, the majority of stars that have formed in the Universe since at least the peak of the cosmic SF history at \( z \approx 1.9 \) (Madau & Dickinson 2014) have condensed out of cold gas distributed over the discs of spiral galaxies. It may thus be argued that the physically more fundamental relation underlying the MS relation is the SFR–\( M_\star \) relation for disc galaxies; connecting their ability to sustain extended SF to their rotationally supported kinematic structure (Driver et al. 2006; Abramson et al. 2014; Grootes et al. 2014, 2017). Given observational evidence implying that the gas required to sustain this process is supplied via continuous accretion from the intergalactic medium (IGM, e.g. L’Huillier, Combes & Semelin 2012; Robotham et al. 2014), the processes regulating this ‘gas fuelling’ are central to our understanding of galaxy formation and evolution.

Under the present paradigm of structure formation, galaxies initially form and evolve as disc galaxies at the centre of dark-matter haloes (DMHs, e.g. Rees & Ostriker 1977; White & Rees 1978; Fall & Efstathiou 1980; White & Frenk 1991; Mo, Mao & White 1998). Their subsequent evolution is determined by the ongoing formation of stars from the interstellar medium (ISM) following the Schmidt–Kennicutt relation (Schmidt 1959; Kennicutt 1998). The availability of ISM, in turn, is expected to be determined by a balance between flows of gas into the galaxy, and removal and consumption of the ISM by outflows and SF; respectively (e.g. Rasera & Teyssier 2006; Finlator & Davé 2008; Bouché et al. 2010; Dutton, van den Bosch & Dekel 2010; Davé, Finlator & Oppenheimer 2012; Lilly et al. 2013), i.e. a baryon cycle.

In this picture, the SFR of a galaxy is set by the interplay and the evolving balance of

(i) the rate at which the gas flows into the ISM,

(ii) feedback from energetic processes in the galaxy (including SF) driving outflows of ISM from the galaxy and disrupting flows of incoming gas (e.g. Faucher-Giguère, Kereš & Ma 2011; Hopkins et al. 2013, and references therein), and

(iii) the efficiency with which ISM is converted into stars.

Of these three, the latter two are assumed to depend largely on galaxy-specific processes and properties (e.g. SF and SNe feedback, galaxy mass, and metallicity), while the inflow rate is (predominantly) expected to depend both on the cosmological epoch as well as on the mass of the galaxy’s host DMH. While the cosmological epoch influences the prevalence of gas via the cosmological accretion rate of DM and baryons from the IGM on to DMHs (e.g. Genel et al. 2008; McBride, Fakhouri & Ma 2009), the mass of the DMH sets the (mix of) accretion model(s), i.e. ‘cold mode’ accretion from filamentary flows (e.g. Kereš et al. 2005; Dekel et al. 2009; Brooks et al. 2009; Kereš et al. 2009; Pichon et al. 2011; Nelson et al. 2013) and/or ‘hot mode’ accretion from a hot/warm virialized intrahalo medium\(^2\) (IHM; e.g. Kereš et al. 2005; Dekel & Birnboim 2006; van de Voort et al. 2011c; Dekel et al. 2013). Theory predicts a transition between the two modes at DMH masses of \( \sim 10^{12} \ M_\odot \) and a further decline of the propensity of gas to cool and be accreted in the hot mode with increasing DMH mass (Birnboim & Dekel 2003; Kereš et al. 2005; Dekel & Birnboim 2006; Benson & Bower 2011; van de Voort et al. 2011a).

Accordingly, one expects a gradually evolving, inflow-driven, self-regulated, balance of ISM content and SF; at least for central disc galaxies; for satellite galaxies inflows are predicted to be curtailed by the stripping of cold and cooling gas resulting from the motion of the galaxy with respect to the host DMH (Gunn & Gott 1972; Abadi, Moore & Bower 1999; Hester 2006; Bahé & McCarthy 2015; Larson, Tinsley & Caldwell 1980; Kimm et al. 2009). Indeed, implementations of the baryon cycle, both in a sophisticated emergent manner in the form of hydrodynamic simulations (e.g. Kereš et al. 2005; Schaye et al. 2010; Crain et al. 2009; Hopkins et al. 2014; Schaye et al. 2015) and in semi-analytic models of galaxy evolution (Cole et al. 2000; Lacey et al. 2008; Lagos et al. 2011; Croton et al. 2006; Guo et al. 2011; Henriques et al. 2015), as well as in a simplified analytic form (Finlator & Davé 2008; Bouché et al. 2010; Davé et al. 2012; Lilly et al. 2013; Peng & Maiolino 2014), successfully recover the qualitative behaviour of the observed MS relation, lending credence to the baryon cycle and self-regulated feedback in disc galaxies as the underlying driver for the evolution of galaxies on the MS.

However, in a recent analysis focusing on isolating and empirically constraining the process of gas fuelling in disc galaxies in a range of environments, we have shown that the gas fuelling of these objects is largely independent of the satellite/central dichotomy. In addition, this analysis has shown that, even for central galaxies, the environment (group versus field a proxy for DMH mass) seems to have a negligible impact on their gas fuelling and SF (Grootes et al. 2017; henceforth Paper I). Both findings are contrary to the theoretical expectations outlined above, and indicate that our understanding of the processes governing gas fuelling and determining the baryon cycle remains incomplete.

The aim of this paper is therefore to empirically test and constrain the elements of the baryon cycle (of central disc galaxies) and the resulting picture of an inflow-driven self-regulated SFR. In particular, we focus on the evolution of the specific SFR–\( M_\star \) (\( \psi \sim M_\star \)) relation of central disc galaxies over short redshift intervals (\( \Delta z \approx 0.04 \)) in the local Universe, as well as on the dependence on host DMH mass at fixed redshift and stellar mass.

Under the reasonable assumption that the physical processes regulating SF in galaxies remain constant, in nature and efficiency, in the local Universe (for \( 0 \leq z \leq 0.13 \)), the former will enable us to identify variations in galaxy SFR as a result of a gradually evolving inflow/supply of gas and to isolate these from potential variations in the galaxy-specific processes such as SF/feedback. Conversely, the latter will enable us to directly constrain the postulated DMH mass dependence and to test in detail to which degree the baryon cycle and gas fuelling of central galaxies is impacted by the group environment thus following up our unexpected result from Paper I.

We make use of the samples and methodology defined and described in detail in Paper I, and briefly recapitulate the data

\(^{1}\) In the sense of the 1σ dispersion of galaxies around the MS relation.

\(^{2}\) Of course, to be accreted into the ISM of a galaxy, the gas being accreted must be cold in the sense that its thermal velocity must be lower than the escape velocity of the ISM. ‘Cold mode’ and ‘hot mode’ refers to the temperature history of the gas, with cold mode accretion consisting of gas that has never been shock heated to temperatures comparable to the virial temperature, but instead has always remained in a cold, dense state, while hot mode refers to gas that has been shocked and heated and has subsequently cooled.
products and samples used in the analysis in Section 2. In Section 3, we present our results on the redshift evolution of the $\psi$–$M_*$ relation for central disc/spiral galaxies, followed by the results of our investigation of the DMH mass dependence (Section 4). We discuss the direct implications of our results for the gas fuelling and the baryon cycle of central disc galaxies in Section 5 and discuss their broader implications in Section 6. Finally, a summary and conclusions are presented in Section 7.

Throughout the paper, except where stated otherwise, we make use of magnitudes on the AB scale (Oke & Gunn 1983) and an $\Omega_{\text{M}} = 0.3$, $\Omega_{\Lambda} = 0.7$, and $H_0 = 70 \text{ km s}^{-1}\text{Mpc}^{-1}$ ($h = 0.7$) cosmology.

2 DATA AND SAMPLES

As in Paper I, the Galaxy And Mass Assembly survey (GAMA, Driver et al. 2011; Liske et al. 2015) forms the basis for our analysis. In addition to the combined spectroscopic and multiwavelength broad-band imaging data from the far-ultraviolet (FUV) to the far-infrared (FIR), GAMA also provides a wide range of ancillary data products, including, but not limited to, emission-line measurements (Hopkins et al. 2013), aperture matched (Hill et al. 2011), and single Sérsic profile photometry in the optical–near-IR (Kelvin et al. 2012, with associated structural parameters), UV photometry (Liske et al. 2015, Andrae et al., in preparation), stellar mass estimates (Taylor et al. 2011), and a highly complete friends-of-friends group catalogue (Robotham et al. 2011).

In Paper I, we used these data products to define volume-limited, morphologically selected samples of local Universe ($z \leq 0.13$) disc galaxies, including samples of field (FCS) and group central (GCS) disc galaxies. For these, we use GAMA’s NUV photometry in combination with a novel radiation-transfer-model-based attenuation correction technique (Popescu et al. 2011; Grootes et al. 2013), to derive precise and accurate intrinsic total SFRs as a tracer of gas content.

We refer the reader to Driver et al. (2011, 2016b), Liske et al. (2015), and references therein, as well as to the references provided above, for details of the GAMA survey and the individual data products. Furthermore, we refer the reader to Paper I, for a detailed synopsis of the derived properties used in this analysis, including in particular stellar mass and SFR, as well as for a full description of the sample selection. In the following, however, we briefly outline the most salient details.

2.1 Data and derived physical properties

Our analysis uses the first 3 yr of data of the GAMA survey – frozen and referred to as GAMA I – consisting of the three equatorial fields to a homogeneous depth of $V_{\text{AB}} \leq 19.4$ mag. $^3$ We make use of GAMA’s quantitative spectroscopy as well as of the UV/optical (NUV, $u$, $g$, $r$, $i$, $z$) broad-band photometry.

2.1.1 Quantitative spectroscopy and the galaxy group catalogue

GAMA provides spectroscopy and derived quantities, including emission-line fluxes, for $>98$ per cent of $r < 19.4$ galaxies in the survey area. The spectroscopy enables (i) identification and removal of disc galaxies hosting active galactic nuclei (AGNs) using the Kewley et al. (2001) BPT criterion, and (ii) the construction of the GAMA galaxy group catalogue (G’C, Robotham et al. 2011). Uniquely, as a result of GAMA’s high spectroscopic completeness even on small angular scales, the G’C reliably samples the DMH mass function down to low mass ($M_{\text{dyn}} < 10^{12}$), low multiplicity ($N < 5$) galaxy groups. This catalogue also provides an estimate of the parent halo mass based on a group’s total luminosity, which has been cross-calibrated using weak-lensing measurements of the group halo mass and the GAMA survey mocks (Merson et al. 2013; Han et al. 2015).

2.1.2 Optical photometry, stellar masses, and weak lensing

Homogenized optical photometry – $u$, $g$, $r$, $i$, $z$, based on imaging by the Kilo Degree Survey (hereafter referred to as KiDS; Kuijken et al. 2015; Hildebrandt et al. 2017; de Jong et al. 2017) and archival imaging data of the Sloan Digital Sky Survey (SDSS) – is available for the entire GAMA I footprint. This has enabled the construction of a catalogue of aperture matched photometry (Hill et al. 2011; Driver et al. 2016b; Wright et al. 2016) as well as of a catalogue of single Sérsic photometry and structural measurements (Kelvin et al. 2012), providing measurements of effective radii, integrated luminosity, and Sérsic index in each band for the vast majority of GAMA sources. Foreground extinction corrections in all optical bands have been calculated following Schlegel, Finkbeiner & Davis (1998) and $k$-corrections to $z = 0$ have been calculated using KCORRECT_V4.2 (Blanton & Roweis 2007).

The optical photometry also represents the basis of GAMA’s stellar mass measurements following (Taylor et al. 2011). These estimates make use of a Chabrier (2003) initial mass function (IMF) and the Bruzual & Charlot (2003) stellar population library. Taylor et al. (2011) determine the formal random uncertainties on the derived stellar masses to be $\sim0.1–0.15$ dex on average, and the precision of the determined mass-to-light ratios to be better than 0.1 dex.

Finally, the overlap of GAMA with the KiDS surveys allows us to perform a stacked weak-lensing analysis of the DMHs hosting the galaxies from our samples, thus extracting mass estimates. This is discussed in greater detail in Section 4.2 and Appendix B. The KiDS data used for this purpose are processed by THELI (Erben et al. 2013) and ASTRO-WISE (Begeman et al 2013; de Jong et al. 2015). Shears are measured using LENSFIT (Miller et al. 2015), and photometric redshifts are obtained from point spread function (PSF) matched photometry and calibrated using external overlapping spectroscopic surveys (see Hildebrandt et al. 2016).

2.1.3 UV photometry and SFR

The majority of the GAMA I footprint has been observed in the NUV by GALEX (Galaxy Evolution Explorer) to a depth of $\sim23$ mag by the Medium Imaging Survey (MIS; Martin et al. 2005; Morrissey et al. 2007) survey and by a dedicated guest investigator program GALEX–GAMA providing largely homogeneous coverage. This forms the basis for GAMA’s NUV photometry. Details of the GAMA UV photometry are provided in Liske et al. (2015), Andrae et al. (in preparation), and on the GALEX–GAMA website, and a detailed synopsis is provided in Paper I. Foreground extinction corrections and $k$-corrections having been applied as in the optical bands.

$^3$ The $r$-band magnitude limit for the GAMA survey is defined as the SDSS Petrosian foreground extinction corrected $r$-band magnitude.

$^4$ www.mpi-hd.mpg.de/galex-gama/
As detailed in Paper I, the integrated NUV emission from a spiral/disc galaxy provides an SFR tracer which is sensitive to the total SFR of the galaxy on time-scales of \( \lesssim 10^8 \) yr (see e.g. fig. 1 of Paper I), while remaining robust against stochastic fluctuations, unlike H\(\alpha\)-based tracers. Thus, the time-scale probed by the NUV is short compared to the timespan corresponding to a redshift baseline of \( \Delta z \approx 0.04 \) (in the range \( z = 0\,–\,0.13 \)), making it well suited to investigate the evolution of the \( \psi_s - M_\ast \) relation. In this paper, we have adopted the calibration between NUV luminosity and SFR as given in Hao et al. (2011), scaled from a Kroupa (2001) IMF to a Chabrier (2003) IMF as in Speagle et al. (2014).  

To correct for the attenuation of stellar emission by dust in the galaxy, which is particularly severe at short (UV) wavelengths (e.g. Tuffs et al. 2004), we employ the method of Grootes et al. (2013). This method makes use of the radiation transfer model of Popescu et al. (2011) and supplies attenuation corrections on an object-by-object basis for spiral galaxies, taking into account the orientation of the galaxy in question and estimating the disc opacity from the stellar mass surface density. A comparison of the method and its performance with a range of other widely used SFR indicators can be found in Davies et al. (2016).

### 2.2 Samples of central disc galaxies

We make use of the sample of field central disc galaxies and the sample of group central disc galaxies as provided in Paper I. The samples are constructed by morphologically selecting disc galaxies from the full GAMA sample using the method described in Grootes et al. (2014), resulting in samples which are unbiased in their SF properties and are jointly optimized for purity and completeness.

We impose a redshift limit of \( z = 0.13 \), resulting in a mass-complete sample for galaxies with \( M_\ast \geq 10^{10.5} \) and deselect galaxies hosting an AGN based on their position in the BPT diagram. In our analysis, we only make use of the mass-complete sample, but do, in some cases, include galaxies below this mass on plots to indicate trends in the population.

#### 2.2.1 Field central discs

From the parent sample of disc galaxies, a sample of field central disc galaxies is selected as those which are not associated with any other galaxy to the limiting depth of the survey by the friends-of-friends group finding algorithm (Robotham et al. 2011). As such, these galaxies likely represent the dominant central galaxy of their DMH, with any satellite being at least less massive than \( M_\ast = 10^{10.5} \) and likely even less massive over most of the redshift range. In the following, we will refer to this sample, encompassing 3508 galaxies, as the FCS sample. Fig. 1 shows the fraction of disc galaxies in the field as a function of stellar mass, as well as the stellar mass distribution of the FCS sample.

#### 2.2.2 Group central discs

In selecting a sample of group central disk galaxies, we proceed by selecting those galaxy groups from the G3C which contain at least three member galaxies with \( M_\ast \geq 10^{10.5} \) (regardless of the galaxies’ morphology) and again impose the redshift limit of \( z = 0.13 \). This results in a volume-limited sample of galaxy groups. From these, we then select those galaxies which are the central galaxy of the group, are a member of the parent sample of disc galaxies, and have no neighbouring galaxy within 50 kpc \( h^{-1} \) and 1000 km s\(^{-1}\). This latter criterion is imposed to ensure that the SF activity of the galaxy is unlikely to be impacted by galaxy–galaxy interactions, which are known to influence the SFR and SF efficiency of galaxies (e.g. Barton, Geller & Kenyon 2000; Robotham et al. 2013, 2014; Davies et al. 2015; Alatalo et al. 2015; Bitsakis et al. 2016). In the following, we will refer to this sample of 79 largely isolated group central disc galaxies as the GCS sample. For reference, we show

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5 This choice is different from that adopted in Paper I, and is motivated solely by reasons of intercomparability, and only significantly impacts the normalization of the \( \psi_s - M_\ast \) relation.

6 In Paper I, we referred to this sample as the FIELDGALAXY sample.

7 The disc fraction is calculated relative to the supersample of galaxies which meet all the requirements of the FCS sample, save for the morphological requirements and the AGN deselection. The impact of the latter criterion is negligible (<1 per cent).
the disc fraction. The stellar mass distribution is clearly skewed towards more massive galaxies for the GCS sample than for the FCS sample, with the distribution being peaked at the median value of $M_* = 10^{10.6} M_\odot$.

3 REDSHIFT EVOLUTION OF THE $\psi_* - M_*$ RELATION OF FIELD CENTRAL DISC GALAXIES

The $\psi_* - M_*$ relation for field central disc galaxies likely underlies the so-called ‘main sequence of star-forming galaxies’ (Noeske et al. 2007; Wyders et al. 2011; Whitaker et al. 2012; Speagle et al. 2014), a cornerstone empirical result of galaxy evolution studies of the past decade. Although a recent meta-analysis by Speagle et al. (2014) has calibrated a smooth parametrization of the evolution of the MS relation over the redshift range $z = 0.25-4$, a probe of its actual smoothness, i.e. the continuity of its evolution over (very) short redshift intervals (and at very low $z$) – desirable in terms of constraints on the contribution and importance of different physical processes to the relation and its evolution – remains lacking.

Fig. 2 shows $\psi_*$ as a function of $M_*$ for the FCS sample, with the median relation overlaid. As demonstrated by the figure, the $\psi_* - M_*$ relation for the FCS sample is well described by a single power law

$$\log(\psi_*) = A + \gamma(\log(M_*) - 10)$$

over its entire range in stellar mass, with $\gamma = -0.45 \pm 0.01$ as in Paper I (see also Table 1). The relation is in good agreement with the low-$z$ extrapolation of the empirical parametrization of the MS presented by Speagle et al. (2014), shown in red. Both the power-law slope $\gamma$ and the normalization constant $A$ agree with the corresponding values of the parametrization of Speagle et al. (2014) at the mean redshift of the FCS sample ($z = 0.1$) within $2\sigma$ of their formal uncertainties. If we also consider the uncertainties on the predicted parameters then the power-law fits are consistent with the predictions for the MS within the $1\sigma$ uncertainties of the latter. The details of the fitted power laws are listed in Table 1, as are the slope and normalization of the parametrization of the MS presented by Speagle et al. (2014). We do note, however, that within the uncertainties, the fit to the $\psi_* - M_*$ relation has a slightly shallower slope than the parametrization of the MS, with the difference being most noticeable at higher $M_*$. This may result from the inclusion of more bulge-dominated galaxies in the MS sample of Speagle et al. (2014).

We have established that the median $\psi_* - M_*$ relation of central disc galaxies coincides with the parametrization of the MS for our volume-limited sample extending to $z = 0.13$ over the full extent in $M_*$ covered. We now investigate the what evolution, if any, occurs in this redshift range. For this purpose, we divide the FCS sample into three bins in redshift; $z_1: 0.03 \leq z \leq 0.06$, $z_2: 0.08 \leq z \leq 0.11$, and $z_3: 0.12 \leq z \leq 0.13$. For these three sub-samples, we find mean redshifts of $\overline{z}_1 = 0.05$, $\overline{z}_2 = 0.095$, and $\overline{z}_3 = 0.125$, respectively.

Figure 2. sSFR $\psi_*$ as a function of stellar mass $M_*$ for the FCS sample. Values for individual sample galaxies are shown as grey circles, with downward arrows indicating those galaxies for which the derived value of $\psi_*$ is an upper limit (at $2.5\sigma$; as discussed in detail in Paper I, the depth of the GALEX-GAMA UV data is such, that the second quartile and the median are defined by detections). The median $\psi_* - M_*$ relation in bins of 0.25 dex in $M_*$ is shown by the transparent shaded regions, with the width of the darker narrower region indicating the bootstrapped uncertainty in the median, and the width of the wider, lighter region indication the interquartile range. Given the mass limit of $M_* \geq 10^{10.5}$ to which the FCS sample is volume complete, and the low number of sources with $M_* \geq 10^{11} M_\odot$, we have fit a single power law $\log(\psi_*) = A + \gamma(\log(M_*) - 10)$ to the binwise median values denoted by the black filled circles, denoted by the black dash–dotted line. For comparison, the empirical parametrization of the main sequence of star-forming galaxies presented by Speagle et al. (2014), extrapolated to the median redshift of the FCS sample of $z = 0.1$, is shown as a red dashed line, while a black dotted line shows the result of fitting power law with the slope fixed to the expectation value for the main sequence.

The full details of the fits are listed in Table 1. The top panel of Fig. 3 depicts the median $\psi_* - M_*$ relation of the three sub-samples binned in stellar mass, as well as the best-fitting power law and the predictions of Speagle et al. (2014, making use of the mean redshift) for each sub-sample. The $\psi_* - M_*$ relations for the sub-samples agree well with the extrapolation of the empirical MS parametrization, albeit that small differences in normalization and/or slope are present, which largely averaged out in the full FCS sample. The normalization constants for all sub-samples agree with those expected for the MS within the $1\sigma$ formal uncertainties of the fits. Similarly, for sub-samples $z_1$ and $z_2$ the fitted power-law slopes agree with those of the extrapolated MS within the $1\sigma$ formal uncertainties of the fit, and only for the $z_3$ sub-sample do the slopes differ more, i.e. by $2\sigma$. The full details of the fits are listed in Table 1.

As the focus of our interest is on the relative evolution of the relations over the redshift range covered by our sample, in order to...
Table 1. Compilation of power-law fits to the $\psi_* - M_*$ relation.

<table>
<thead>
<tr>
<th>Sample</th>
<th>$z$</th>
<th>$A$</th>
<th>$\gamma$</th>
<th>$A_{\text{norm}}$</th>
<th>$\gamma_{\text{norm}}$</th>
<th>$A$</th>
<th>$\gamma$</th>
<th>$A_{\text{norm}}$</th>
<th>$\gamma_{\text{norm}}$</th>
</tr>
</thead>
<tbody>
<tr>
<td>FCS</td>
<td>0.1</td>
<td>-9.90 ± 0.01</td>
<td>-0.45 ± 0.01</td>
<td>-</td>
<td>-</td>
<td>-9.92</td>
<td>-0.47</td>
<td>-</td>
<td>-</td>
</tr>
<tr>
<td>$z_1$</td>
<td>0.05</td>
<td>-10.00 ± 0.02</td>
<td>-0.49 ± 0.06</td>
<td>-0.1 ± 0.02</td>
<td>-0.04 ± 0.06</td>
<td>-10.01</td>
<td>-0.49</td>
<td>-0.10</td>
<td>-0.02</td>
</tr>
<tr>
<td>$z_2$</td>
<td>0.095</td>
<td>-9.91 ± 0.01</td>
<td>-0.45 ± 0.02</td>
<td>-0.01 ± 0.01</td>
<td>-0.01 ± 0.02</td>
<td>-9.92</td>
<td>-0.47</td>
<td>-0.01</td>
<td>0.00</td>
</tr>
<tr>
<td>$z_3$</td>
<td>0.125</td>
<td>-9.88 ± 0.01</td>
<td>-0.42 ± 0.02</td>
<td>0.03 ± 0.01</td>
<td>0.03 ± 0.02</td>
<td>-9.88</td>
<td>-0.46</td>
<td>0.05</td>
<td>0.01</td>
</tr>
</tbody>
</table>

Notes: Power-law fits of the form $\log(\psi_*) = A + \gamma \cdot (\log(M_*) - 10)$ to the $\psi_* - M_*$ relations for different samples of spiral galaxies. The uncertainties reflect the formal uncertainties of the fit. The columns under Speagle et al. (2014) MS expectation provide the extrapolated expectation values for the MS following Speagle et al. (2014). For the purpose of our comparison, we have converted the empirical parametrization of the MS from the SFR to the specific SFR expectations, respectively. Colour coding and line styles are identical to the median redshift of $\approx 0.43 \text{dex}$. Parameters with subscript ‘norm’ correspond to the power-laws refit to the subsamples after normalization to the result obtained for the full FCS sample and the Speagle et al. (2014) expectation for the MS at $z = 0.1$, respectively.

Table 2. Compilation of evolution in normalization and slope for power-law fits to the $\psi_* - M_*$ relation.

<table>
<thead>
<tr>
<th>Sample 1</th>
<th>$z_1$</th>
<th>$\Delta A_{\text{obs}}$</th>
<th>$\Delta \gamma_{\text{obs}}$</th>
<th>$\Delta A_{\text{MS}}$</th>
<th>$\Delta \gamma_{\text{MS}}$</th>
</tr>
</thead>
<tbody>
<tr>
<td>$z_3$</td>
<td>0.013 ± 0.02</td>
<td>0.07 ± 0.06</td>
<td>0.15</td>
<td>0.03</td>
<td></td>
</tr>
<tr>
<td>$z_3$</td>
<td>0.04 ± 0.02</td>
<td>0.04 ± 0.02</td>
<td>0.06</td>
<td>0.01</td>
<td></td>
</tr>
<tr>
<td>$z_2$</td>
<td>0.09 ± 0.02</td>
<td>0.03 ± 0.06</td>
<td>0.09</td>
<td>0.02</td>
<td></td>
</tr>
</tbody>
</table>

Notes: Observed (obs) and expected (MS) values (for the MS) of evolution in normalization and slope of the $\psi_* - M_*$ between redshift sub-samples computed from the normalized power-law fits listed in Table 1. Uncertainties correspond to the formal uncertainties in sum quadrature. As in Table 1, we list no uncertainties for the predictions. For the redshift range considered typical values would be $\Delta A \approx 0.6 \text{dex}$ and $\Delta \gamma \approx 0.05 \text{dex}$.

Figure 3. Median $\psi_* - M_*$ relations for the $z_1$ (blue, 0.03 $\leq z \leq 0.06$), $z_2$ (green, 0.08 $\leq z \leq 0.11$), and $z_3$ (red, 0.12 $\leq z \leq 0.13$) sub-samples of the FCS sample (top). The width of the shaded regions indicate the bootstrapped uncertainty in the median. Single power-law fits of the form $\log(\psi_*) = A + \gamma \cdot (\log(M_*) - 10)$ to the bisine median relations are shown as dash–dotted lines in the corresponding colour, while dashed lines indicate the extrapolated expectation for the main sequence following Speagle et al. (2014) for the mean redshift of each sub-sample ($\bar{z}_1 = 0.05, \bar{z}_2 = 0.095$, and $\bar{z}_3 = 0.125$). The bisine expectations following Speagle et al. (2014) are shown as filled circles. For comparison, the results of fitting a single power law with the slope fixed to that expected for the main sequence is shown as a dotted line. The bottom panel shows the median relations normalized to the single power-law fit to the full FCS sample as shown in Fig. 2 and listed in Table 1 and to the extrapolated expectation for the main sequence at the median redshift of $z = 0.1$ for the power-law fits and the main-sequence expectations, respectively. Colour coding and line styles are identical to the top panel.

facilitate a comparison, we have normalized each sub-sample by the fit to the full FCS sample and have refit a power law. Analogously, we have normalized the extrapolated MS relations at the mean redshift of each sub-sample to the MS relation at $z = 0.1$; the results are shown in the bottom panel of Fig. 3 and the fit parameters $A_{\text{norm}}$ and $\gamma_{\text{norm}}$ are listed in Table 1. We find that all observed differences in normalization are consistent with those predicted for the MS, while also being statistically significant at $\sim 3 \sigma$, with the exception of $z_3 \rightarrow z_2$, for which the difference in normalization is only $0.04 \text{dex} (2\sigma)$. A synopsis of the observed and expected evolutions in normalization between the three sub-samples of the FCS sample is provided in Table 2.

In addition to an evolution of the normalization of the MS, the empirical parametrization presented by Speagle et al. (2014) also predicts the slope of the MS to evolve, becoming steeper with decreasing redshift. For the $z_1$ and $z_2$ sub-samples, the fitted slopes of the power-law relations are consistent with those expected for the MS within the formal uncertainties of the fits (see Table 1), while for the $z_3$ sub-sample, the slope is shallower than the MS expectation by $2\sigma$, as also visible in the top panel of Fig. 3. We note, however, that the evolution in slope is so small, that we cannot robustly exclude the scenario of no evolution.

We complement our investigation of the evolution of the median $\psi_* - M_*$ by an investigation of the distribution of $\psi_*$ at given $M_*$. To this end, we split each of our redshift sub-samples $z_i$ into three bins of stellar mass, $M_i: 9.5 \leq \log(M_i/M_\odot) < 10$, $10.0 \leq \log(M_i/M_\odot) < 10.5$, and $10.5 \leq \log(M_i/M_\odot)$.
respectively, where \( \psi_{z,\text{FCS}}(M_i) \) is the median value of \( \psi_z \) at \( M_i \) as determined from the full FCS sample and \( \langle \psi_x,\text{FCS}(M_i) \rangle \) is the corresponding median value as determined from the sub-sample \( z_i \). As such, \( \Delta \log(\psi_z) \) and \( \Delta_i \log(\psi_z) \) quantify the distribution of \( \psi_z \) around the median relation(s), thus normalizing out the dependence of \( \psi_z \) on \( M_i \).

Fig. 4 shows the distributions of \( \Delta \log(\psi_z) \) and \( \Delta_i \log(\psi_z) \) for each of the redshift sub-samples \( z_i \) in the stellar mass bins \( M_i \). In each stellar mass bin, the distributions of \( \Delta \log(\psi_z) \) and \( \Delta_i \log(\psi_z) \) are nigh identical between the \( z_i \) sub-samples, with only a variable offset visible for the distributions in \( \Delta \log(\psi_z) \) in line with the previously described evolution of the median. This entails that it is an overall shift of the distribution of \( \psi_z \) at fixed \( M_i \), rather than a change in shape of the relative distribution of \( \psi_z \), which drives the observed redshift evolution of the median \( \psi_z \)-\( M_i \) relation. In a more statistically robust sense, this is corroborated by three-sample Anderson–Darling tests comparing the distributions of \( \Delta \log(\psi_z) \) and \( \Delta_i \log(\psi_z) \). These find no grounds for rejecting the null hypothesis that the distributions are drawn from the same parent sample, modulo a redshift-dependent shift in the normalization (see Table 3). Of course, the lack of difference in a statistical sense does not prove similarity, but these results do reinforce our finding of similarity based on visual inspection of the distributions.

Finally, we note the existence in each stellar mass bin and in each redshift sub-sample of a population of disc galaxies with observed \( \psi_z \) much lower than the median (here we consider the population with \( \Delta_i \log(\psi_z) < -0.5 \)). The fractional size of this population increases with stellar mass from 5–10 percent in the low stellar mass bin to 12–17 percent in the highest stellar mass bin, however, is largely constant as a function of redshift. As discussed in Groote et al. (2014) and Paper I this population is dominated by genuine UV faint disc galaxies. The presence of such a low \( \psi_z \) population amongst the disc galaxies of the FCS sample, with fractional size increasing with stellar mass, may imply the existence of a secular mechanism, dependent on galaxy (stellar) mass, acting to shut down SF in disc galaxies.

In summary, we find evolution of the \( \psi_z \)-\( M_i \) relation of disc galaxies over the redshift range \( 0 < z < 0.13 \), sampled at intervals of \( \Delta z \approx 0.03–0.04 \), to be consistent with a smooth gradual evolution of the normalization and possibly the slope while the scatter, i.e. the distribution around the median, remains constant. Furthermore, we find the observed evolution to be fully consistent with the extrapolation of the parametrization of the MS presented by Speagle et al. (2014).

4 IMPACT OF ENVIRONMENT/DMH MASS ON THE \( \psi_z \)-\( M \) RELATION FOR CENTRAL DISC GALAXIES

For central galaxies, theory predicts the maximum achievable rate of accretion on to the galaxy to be a function of the host DMH mass. However, in Paper I we have presented evidence that the \( \psi_z \)-\( M \) relation for central disc galaxies of groups coincides with that found for their field counterparts. While this result may imply a possible lack of halo mass dependence of the \( \psi_z \)-\( M \) relation for central disc galaxies, it may also arise from the fact that the DMH masses of field and group central disc galaxies at fixed stellar mass are highly similar. Here, we focus on comparing the \( \psi_z \)-\( M \) relations for our samples of field and group central disc galaxies, the FCS and GCS samples, respectively – combining this comparison with an investigation of their respective DMH masses to constrain a possible dependence on DMH mass.

As discussed in Section 2 and shown in Fig. 1, the range in \( M_i \) common to the FCS and GCS samples is limited to \( M_i \geq 10^{10.8} \, M_\odot \). However, as is apparent from Fig. 1, even within this mutual stellar mass range the relative distributions of \( M_i \) differ radically, making any average property potentially vulnerable to a bias arising from this dissimilar distribution of stellar mass. We therefore proceed by creating four subsamples – two from the GCS sample and two from the FCS sample – with which to perform the brunt of our analysis. Those from the GCS sample are obtained by splitting the sample at its median stellar mass of \( \log(M_i/\, M_\odot) = 10.6 \), and we will refer to the low and the high stellar mass sub-samples as the LGCS and HGCS samples, respectively. To construct the two from the FCS sample, analogously referred to as the LFCS and HFCS samples, we begin by selecting all galaxies from the FCS sample with \( \log(M_i/\, M_\odot) \geq 9.8 \). This sample is then split at \( \log(M_i/\, M_\odot) = 10.6 \) analogously to the GCS sample. Subsequently, within each stellar mass range, we randomly select galaxies in such a manner as to reproduce the mass distributions of the LGCS and HGCS samples, respectively, while simultaneously maximizing sample size. A detailed description of this process is provided in Appendix A.

4.1 The \( \psi_z \)-\( M \) relation for field and group central spiral galaxies

We begin our investigation by considering the \( \psi_z \)-\( M \) relations of the FCS and GCS samples, as depicted in Fig. 5 (top panel). We find the median \( \Delta \log(\psi_z) \)-\( M \) relations to coincide. This finding is supported by the bottom (middle) panel of Fig. 5, which shows the distributions of \( \Delta \log(\psi_z) \) for the LGCS (HGCS) sample, the LFCS (HFCS) sample, and the FCS limited to the range \( 9.8 \leq \log(M_i/\, M_\odot) < 10.6 \) (10.6 \( \leq \log(M_i/\, M_\odot) \)). These all appear to be highly similar, and a three-sample Anderson–Darling test comparing the distributions finds no grounds to reject the null hypothesis that the distributions are all consistent with having been drawn from the same parent sample (\( p = 0.4 \) and \( p \geq 0.98 \), respectively). In line with this result, we find the scatter in the relations in each range of stellar mass, as characterized by the interquartile range of the distribution of \( \Delta \log(\psi_z) \), to be consistent between the LFCS, LGCS, HFCS, and HGCS samples, i.e. \( 0.37 \pm 0.02, \, 0.3(3) \pm 0.10, \, 0.3(4) \pm 0.12, \) and \( 0.3(7) \pm 0.10 \) dex, respectively.

We do note, however, that the \( \Delta \log(\psi_z) \) distributions of the LGCS and HGCS samples appear to be shifted slightly towards higher \( \psi_z \) compared to the mass-matched LFCS and HFCS samples, so that the \( \psi_z \)-\( M \) relation of the GCS sample may be slightly elevated compared to that of the FCS sample.

Overall, we thus find no robust evidence of a systematic difference in \( \psi_z \) at fixed \( M_i \) between field and group central disc galaxies.
Figure 4. Evolution of $\Delta \log(\psi_*)$ for the $z_1$, $z_2$, and $z_3$ sub-samples of the FCS sub-sample (top to bottom) in three bins of stellar mass $M_*$ as indicated (left to right). The mass range encompasses $\gtrsim 99$ per cent of the FCS sample. The distribution of $\Delta \log(\psi_*)$ in each mass bin for the full FCS sample is shown as a grey solid line, while the distributions of $\Delta \log(\psi_*)$ for the redshift subsamples are shown as dark shaded histograms and the distributions of $\Delta \log(\psi_*)$ are shown as lighter shaded histograms. Quantitative statistical tests of the similarity of the distributions within each stellar mass bin are listed in Table 3.
estimate average DMH masses for our four sub-samples, using several complementary methods. An initial expectation value for the average DMH mass of the field central disc galaxies of the LFCS and HFCS samples can be obtained from the stellar-mass–halo-mass (SMHM) relation. In Fig. 6, we show the SMHM relation for central galaxies, (i) as derived from KiDS (de Jong et al. 2015; Kuijken et al. 2015) weak-lensing observations (grey; van Uitert et al. 2016), and (ii) as expected based on abundance matching applied to the Millennium simulations (orange; Moster, Naab & White 2013, and references therein). 12 It is, however, initially unclear to what degree the average halo mass of our LFCS and HFCS samples conform to this expectation.

For each sample, we have therefore constructed a stacked shear profile and corresponding excess surface density (ESD) profile using the bespoke KiDS galaxy–galaxy weak-lensing pipeline and have fit a DMH mass assuming a single NFW halo. Details of this process are provided in Appendix B. As shown in Fig. 6, the average DMH masses derived for the LFCS and HFCS sub-samples \(\log(M_{\Delta}/M_\odot) = 11.9^{+0.3}_{-0.9} \) and \(12.5^{+0.1}_{-1.3}\), respectively 13) are consistent with the expectations.

We note, however, that the empirical SMHM relation derived by van Uitert et al. (2016) is based on the flux-limited GAMA sample, while our LFCS and HFCS are volume limited and morphologically selected, thus introducing the possibility of a systematic bias. For comparison, we therefore show the average DMH mass in bins of stellar mass determined for, (i) a volume-limited \(z < 0.2\) subsample of GAMA central galaxies using maximum-likelihood weak lensing (purple, Han et al. 2015), and (ii) a flux-limited sample of late-type SDSS central galaxies using stacked weak lensing (green; Mandelbaum et al. 2006, and references therein). We find our average DMH mass estimates for both sub-samples to be consistent within the uncertainties with the body of literature. Finally, we note that our limited sample size of 52 (1013) galaxies in the HFCS (LFCS) samples limits the strength of the shear signal and the tightness of our constraint on the average halo mass.

Nevertheless, our findings indicate that that the average halo mass of our samples are consistent with expectations and certainly provide a clear upper limit.

As for the field sub-samples, constraining the average DMH mass of the LGCS and HGCS samples using stacked weak-lensing measurements is complicated by the small sample sizes (40 and 39 sources, respectively), and we obtain \(\log(M_{\Delta}/M_\odot) = 12.8^{+0.2}_{-1.2}\) and \(12.8^{+0.4}_{-1.4}\) for the low and high stellar mass sub-samples, respectively.

12 These have been converted from the usual form \(\langle M_{\Delta} | M_\odot \rangle\) to \(\langle M_{\Delta} | M_\odot \rangle\) using Bayes’ theorem for conditional probabilities (Han et al. 2015; see also Coupon et al. 2015).

13 The values quoted correspond to the mode and the 68 per cent HPD interval of the posterior distribution.
Figure 6. Average host DMH mass of the LFCS and HFCS samples (grey filled circles) as well as of the LGCS and HGCS samples (filled salmon circles) as determined from stacked weak-lensing measurements using the KiDS galaxy–galaxy weak-lensing pipeline as detailed in Appendix B. The symbols denote the mode of the posterior PDFs, while the error bars show the 68 per cent HPD interval containing the mode. In stellar mass, the symbols denote the median with the error bars indicating the 16th–84th percentile range in stellar mass contributing to the stack. For the LGCS and HGCS samples, the independent group luminosity-based median DMH mass estimates are shown as filled red squares with the error bars indicating the uncertainty in the median. For comparison, the empirical median \(M_{\text{halo}}-M_\star\) relation derived by van Uitert et al. (2016) using the full KiDS–GAMA overlap, as well as the abundance matching based \(M_\star-M_{\text{halo}}\) relation of Moster et al. (2013) – converted to the form \(M_{\text{halo}}-M_\star\) (Han et al. 2015) – are shown as grey (dash-dotted) and yellow (dashed) outlined regions, with the width indicating the range between the 16th and 84th percentile. For further comparison, the results of two recent independent comparable weak-lensing analysis are overlaid. The median DMH halo masses found by Han et al. (2015) using an SDSS imaging-based maximum-likelihood weak-lensing analysis in bins of central galaxy stellar mass for a volume-limited (at \(z = 0.2\)) sample of GAMA central galaxies and a flux-limited sample of GAMA group central galaxies (\(N \geq 3\), i.e. with some similarity to our GCS sample), are shown as open purple diamonds and open blue squares, respectively. Similarly, the median DMH masses of a flux-limited sample of central late-type SDSS galaxies presented by Mandelbaum et al. (2006) are shown as open green circles.

However, for these samples, we can also make use of the group luminosity to derive an estimate of the mass of the (central) DMH of the group following Han et al. (2015). This is done by using the observed group luminosity from the G3C (Robotham et al. 2011) and equations (22) and (23) of Robotham et al. (2011) to estimate the total group luminosity and subsequently employing the luminosity-based halo mass estimator for GAMA presented by Han et al. (2015).

Using this estimator, we obtain average DMH masses of \(\log(M_{\text{DMH}}/M_\odot) = 12.5 \pm 0.1\) and \(12.8 \pm 0.1\), for the LGCS and HGCS samples, respectively, as shown in red in Fig. 6. As such, both estimators of the average DMH masses of our GCS sub-samples agree within their uncertainties, especially for the HGCS sample. Nevertheless, for the LGCS sample, although the luminosity-derived average mass is consistent with the stacked weak-lensing-based estimate within the uncertainties of the latter, the average DMH mass preferred by the luminosity-based estimate does seem to be slightly lower. Furthermore, the preferred stacked weak-lensing halo masses for both samples are highly similar.

We note, however, that the average halo mass preferred by the stacked weak-lensing analysis may differ systematically from the median of the luminosity-based estimates, due to the underlying \(M_\star\) distribution and the dependency of the tangential shear signal on DMH mass, in particular for the LCS sample where the shear signal from lower mass haloes might be dominated by that from higher mass systems.

Furthermore, we also note that our sample of group central disc galaxies includes a multiplicity-based selection, strongly akin to that used by Han et al. (2015). In Fig. 6, we therefore also show the maximum-likelihood weak-lensing-based estimates of the halo mass of the multiplicity limited sample of GAMA groups considered by Han et al. (2015) in bins of central stellar mass (shown in blue). We find our weak-lensing and group luminosity-derived halo mass estimates to be consistent with the findings of Han et al. (2015), and recover evidence for the dependence of the central SMHM relation on multiplicity at lower central stellar mass observed by these authors.

Finally, we emphasize, that the halo mass estimator of Han et al. (2015) is suitable to our consideration of potentially different halo masses at a fixed stellar mass, as it employs group luminosity as a proxy for halo mass, and has been directly calibrated on weak-lensing measurements of GAMA galaxy groups using a selection function closely related to that adopted in our analysis. We refer the inclined reader to Han et al. (2015) for further details, but also note...
that, as shown by Han et al., at the low halo mass end any bias in the estimator is likely to underestimate the true halo mass, making our measurements conservative estimates. Furthermore, we note that Viola et al. (2015) have presented an updated relation between group luminosity and halo mass using the combined GAMA and KiDS data. These authors find their results, obtained using a more sophisticated halo model, to be fully consistent with those of Han et al. (2015). As the halo model we have employed in our analysis corresponds to that of Han et al. (2015) and our sample is akin to the sample of groups with \( N \geq 3 \) used by Han et al. (2015), we have made use of the relation presented there, but emphasize that our results are robust against the substitution of this relation with that of Viola et al. (2015).

Overall, we thus conclude that the average DMH masses of the low and high stellar mass samples of group central galaxies are \( \gtrsim 10^{12.5} \) and \( \gtrsim 10^{12.9} \text{M}_\odot \), respectively, i.e. comparable to and possibly slightly higher than that of their field central counterparts in the high stellar mass range, and \( \gtrsim 4–8 \) times more massive in the low stellar mass range.

In summary, we find that at higher stellar mass both the distributions of \( \Delta \log(\psi,M) \) (and accordingly the median \( \psi,M \) relations) and the large-scale environment of these galaxies in terms of the mass of their host DMH are similar between the group and field central galaxies. In contrast, although in the lower stellar mass range \( (9.8 < \log(M_*/\text{M}_\odot) < 10.6) \) the average DMH mass of group central disc galaxies is \( \gtrsim 4–8 \) times greater than that of their field central counterparts, the \( \psi,M \) relations and the distributions of \( \Delta \log(\psi) \) are statistically indistinguishable. Thus, in the low DMH mass range probed by our lower stellar mass group and field central disc galaxies, our results disfavour a halo mass dependence of the \( \psi,M \) relation of these galaxies.

\section{Implications for Gas Fuelling and the Baryon Cycle}

In the previous sections, we have demonstrated (i) that the \( \psi,M \) relation for central disc galaxies evolves smoothly with redshift over very short redshift intervals (\( \Delta z \sim 0.04 \)), in line with the expected behaviour of the MS calibrated over much larger redshift intervals (Section 3), and (ii) that the \( \psi,M \) relations of group and field central disc galaxies are statistically indistinguishable over their full mutual range in stellar mass, even in the low stellar mass range where the host DMH masses differ by a factor of \( \gtrsim 4–8 \), i.e. we find no evidence for a halo mass dependence of the \( \psi,M \) relation of central disc galaxies, at least in the range of low DMH masses (Section 4). In the following, we will discuss the implications of these findings in the context of the baryon cycle and the gas fuelling of these central disc galaxies.

\subsection{The Baryon Cycle Paradigm}

For (largely isolated) disc central galaxies, such as those in our FCS and GCS samples, whose accretion history is dominated by smooth accretion, the mass of the ISM and its time-dependent evolution can be expressed as

\[ \dot{M}_{\text{ISM}} = M_{\text{in}} - M_{\text{out}} - (1 - \alpha)\Phi_* , \]

where \( M_{\text{in}} \) and \( M_{\text{out}} \) are the in- and outflow rates of gas from the galaxy, \( \Phi_* \) is the SFR and \( \alpha \) is the fraction of mass (instantaneously) recycled back to the ISM from high-mass stars. As detailed in Paper I, assuming a volumetric SF law (i.e. \( \Phi_* = \kappa M_{\text{ISM}} \) e.g. Krumholz, Dekel & McKee 2012), and that the outflow from a galaxy is proportional to its ISM mass, \(^{14}\) equation (4) can be equivalently formulated in terms of the ISM mass and the SFR as

\[ \dot{M}_{\text{ISM}} = M_{\text{in}} - \frac{M_{\text{ISM}}}{\tau_{\text{res}}} - \kappa M_{\text{ISM}} \]

\[ = \dot{M}_{\text{in}} - \lambda \Phi_* - (1 - \alpha)\Phi_* \]

where, in equation (5), we have cast the constant of proportionality relating the outflow rate to the ISM mass in terms of typical residence time \( \tau_{\text{res}} \) for a unit mass of gas in the ISM and have defined \( \kappa = (1 - \alpha)\kappa_b \), and in equation (6), we have defined the mass loading factor \( \lambda = 1/\tau_{\text{res}}\kappa_b \). Note that \( 1/\kappa = \tau_{\text{exhaust}} \) corresponds to the gas-exhaustion-by-SF time-scale in a closed box model. Here, we assume \( \tau_{\text{res}} \) and \( \kappa \) (and thus \( \lambda \)) to be determined by galaxy-specific processes, i.e. while they may vary as a function of e.g. galaxy stellar mass, they are constant for all galaxies of a fixed stellar mass.

Accordingly, for the disc galaxies in our samples (read an MS galaxy), provided the inflow is (approximately) stable on timescales longer than the system requires to adjust to perturbations, the SFR of a galaxy is expected to be determined by a self-regulated balance between flows of gas into and out of the ISM and consumption of the ISM via SF. In this case, the galaxy may be considered to be in a quasi-steady state with a quasi-constant SFR at any given time. Combined with a gradually evolving inflow, this model represents a widely favoured explanation of the observed small scatter in the MS and its gradual evolution with redshift (e.g. Keres et al. 2005; Davé, Finlator & Oppenheimer 2012; Lilly et al. 2013; Saintonge et al. 2013; Mitra, Davé & Finlator 2015) and we will return to this aspect in Section 5.3 below.

In such a self-regulated quasi-steady state \( \dot{M}_{\text{ISM}} \approx 0 \) in equation (6), \(^{15}\) which can then be reformulated as

\[ \Phi_* = \frac{1}{\lambda (1 - \alpha)} M_{\text{in}} \]

\[ = \frac{1}{\lambda_{\text{res}} + (1 - \alpha)} M_{\text{in}} \]

\[ = \tilde{\tau} \kappa \dot{M}_{\text{in}} \],

where \( \tilde{\tau} = \tau_{\text{res}}\tau_{\text{exhaust}}/\tau_{\text{res}} + \tau_{\text{exhaust}} \). It is then immediately apparent that the SF is expected to trace the inflow rate in such a case.

For central galaxies on the MS, the (evolving) inflow is widely surmised to be defined by the (evolving) rate of DM and baryon accretion on to DM haloes and an efficiency \( \zeta \), the fuelling efficiency, with which accretable gas is delivered to the ISM of the galaxy (e.g. Davé, Finlator & Oppenheimer 2012; Lilly et al. 2013; Behroozi, Wechsler & Conroy 2013a; Mitra, Davé & Finlator 2015; Rodríguez-Puebla et al. 2016), such that

\[ M_{\text{in}} = \zeta M_{\text{b,halo}} = \zeta f_b M_{\text{halo}} \],

where \( M_{\text{halo}} \) is the halo mass accretion rate, \( f_b \) is the (cosmological) baryon fraction, and \( M_{\text{b,halo}} \), accordingly, is the halo baryon accretion rate – generally well approximated in this manner (e.g. van de Weygaert et al. 2017).

\(^{14}\) Under a volumetric SF law, this is equivalent to the mass-loading formalism.

\(^{15}\) As discussed in Paper I, the actual behaviour of the ISM mass in a quasi steady state will be bracketed by the conditions \( M_{\text{ISM}} = 0 \) and \( \mu = M_{\text{ISM}}/M_* = \text{const.} \) In the latter case, the inflow is higher by a factor of \( (1 - \alpha)\mu \) with the end point of the inflow being the growing ISM. The functional form, however, is similar in both cases.
Voort et al. 2011b; Behroozi, Wechsler & Conroy 2013b; Wetzel et al. 2014). As an expectation for the MS, inserting equation (10) into equation (9), one obtains

$$\Phi = \tilde{\tau} \tilde{\kappa} \zeta \dot{M}_{\text{halo}} = \tilde{\tau} \tilde{\kappa} \dot{M}_{\text{halo}}.$$ (11)

I.e., assuming $\tilde{\tau}$ and $\tilde{\kappa}$ are fully determined by the galaxy-specific processes, the environmental dependence of the MS is encoded in the product $\zeta \dot{M}_{\text{halo}}$ of the fuelling efficiency and the halo baryon accretion rate.

5.2 Constraints on the DMH mass dependence of gas fuelling

In Section 4, we have shown the median $\psi - M_\ast$ relations for group and field central disc galaxies to be statistically indistinguishable over their full mutual range in stellar mass. If the picture of an inflow-driven self-regulated baryon cycle with $\tilde{\kappa}$ and $\tau_{\text{res}}$ determined by galaxy-specific processes, as outlined in Section 5.1 above is to hold for our samples of central disc galaxies, this result entails that the flow of gas into the ISM of the galaxy must be the same.

Expressed in the terms of equation (11), our empirical result thus implies that

$$\zeta \dot{M}_{\text{halo}} \approx \text{const.}$$ (12)

as a function of DMH mass, at least over the halo mass range of $10^{12} M_\odot \lesssim M_{\text{halo}} \lesssim 10^{15} M_\odot$ considered here, i.e. our direct empirical results thus require that the fuelling efficiency scales inversely linearly with the halo baryon accretion rate.\(^{16}\)

As the halo baryon accretion rate function of the DMH mass, the dependency of $\zeta$ on $M_{\text{halo}}$ (at a given redshift) can then be derived by inserting $\dot{M}_{\text{halo}}(M_{\text{halo}}, z)$ in equation (12). With recent parametrizations of the halo baryon accretion rate (Dekel et al. 2009; McBride, Fakhouri & Ma 2009; Fakhouri, Ma & Boylan-Kolchin 2010; Faucher-Giguère, Kereš & Ma 2011) favouring an approximately linear or slightly superlinear dependence ($\dot{M}_{\text{halo}} \propto M_{\text{halo}}^{1.06-1.15}$), our empirical requirement, representing the first direct constraints on the scaling of $\zeta$ with DM mass over the range $10^{12} M_\odot \lesssim M_{\text{halo}} \lesssim 10^{15} M_\odot$, results in

$$\zeta \propto M_{\text{halo}}^{-1.1},$$ (13)

i.e. a strong halo mass dependence for $\zeta$, where we have adopted the parametrization of Mitra et al. presented by Fakhouri et al. (2010).

We note that, qualitatively, our requirement of a strong halo mass dependence of $\zeta$ is consistent with a recent MCMC fit to the global population of a simple parametrized equilibrium model of the baryon cycle, closely related to the model adopted here, by Mitra et al. (2015). However, our direct result of $\zeta \propto M_{\text{halo}}^{-1.1}$ is slightly steeper than the $\zeta \propto M_{\text{halo}}^{-0.75}$ dependence favoured by Mitra et al. (2015) in the same halo mass range using their indirect approach.

\(^{16}\) Here, we have made use of the assumption of the standard paradigm the inflow rate of gas into the ISM of the galaxy can be expressed as $\dot{M}_{b} = \zeta \dot{M}_{\text{halo}}$. However, even if one only maintains the notion of an inflow-driven self-regulated baryon cycle and does not require that the inflow to the ISM of the galaxy can be adequately parametrized using the halo baryon accretion rate, the finding remains relevant in a more general form. Under the broad but reasonable assumption that the inflow to the ISM of the galaxy can be parametrized as $\dot{M}_{b} = \eta_{\text{acc}} \dot{M}_{\text{cool}}$, where $\dot{M}_{\text{cool}}$ represents the rate at which cool accretable gas becomes available at the centre of the halo and $\eta_{\text{acc}}$ represents the efficiency with which it is accreted, our result implies $\eta_{\text{acc}} \dot{M}_{\text{cool}} = \text{const}$. and thus tightly constrains the joint DMH mass dependence.

Similarly, our result is also qualitatively consistent with the findings of Behroozi, Wechsler & Conroy (2013a,c), who find a dependence of the ratio of SFR to halo baryon accretion rate (corresponding to $\tilde{\tau} \tilde{\kappa} \zeta \propto M_{\text{halo}}^{-1/3}$ for haloes with $M_{\text{halo}} \gtrsim 10^{11.7}$ using an abundance matching approach combined with halo merger trees and an MCMC-driven parameter optimization technique applied to the full galaxy population.

Finally, a comparison of our results with those of the full cosmological hydrodynamical simulations, e.g. those presented by van de Voort et al. (2011a), is interesting. At $z \approx 0$, these authors find the ratio of the rates of accretion of baryons into the ISM and on to the host DMH (i.e. comparable to $\zeta$) to initially increase from $M_{\text{halo}} = 10^{11.9} M_\odot$ up to $M_{\text{halo}} \gtrsim 10^{12.5}$ before then decreasing $\propto M_{\text{halo}}^{-1}$ (their fig. 2). While the eventual decrease at higher halo masses is consistent with our empirical results, we find no evidence of the initial increase, possibly indicating remaining issues in the model, e.g. the peak being located at too high halo mass.

5.3 Constraints on the redshift dependence of gas fuelling

Having considered 5.3 Constraints on the redshift dependence of gas fuelling

Having considered the halo mass dependence of gas fuelling, i.e. the environmental efficiency parameter $\zeta$, in the previous section, we now turn to investigating a second central aspect of the standard baryon cycle paradigm; the evolving normalization of the MS as the result of an inflow-driven self-regulated baryon cycle and an evolving inflow.

Our finding in Section 3 that the $\psi - M_\ast$ relation for central disc galaxies evolves smoothly with redshift, exactly in line with the evolution predicted for the MS, while new, is, in essence, not a surprising result, as the MS is dominated by disc galaxies in the local Universe (e.g. Wuyts et al. 2011).

Importantly, however, we have shown the evolution to be gradual and smooth. Given the low- ($z \lesssim 0.13$) and small-redshift intervals ($\Delta z \lesssim 0.1$) probed by the $z_1$, $z_2$, and $z_3$ sub-samples of our FCS subsample, and with redshift intervals between the samples of only $\Delta z \approx 0.04$ (corresponding to only $\approx 4 \times 10^3$ yr), we can reasonably expect the efficiency of SF and other galaxy-specific processes, i.e. the physics encoded in $\kappa$ and $\tau$ in equation (11), to be constant over the considered redshift range at a given stellar mass.

Under these assumptions, our empirical finding of a gradually and smoothly evolving SFR (see Table 2) is qualitatively consistent with the picture of an inflow-driven, self-regulated baryon cycle determining the SFR of disc central galaxies (MS galaxies), as encapsulated in equation (9), and a smoothly evolving inflow.

As outlined in Section 5.1, for central galaxies on the MS, the evolving inflow is widely surmised to be defined by the evolving rate of DM and baryon accretion on to DM haloes and the efficiency $\zeta$ (e.g. Davé et al. 2012; Lilly et al. 2013; Behroozi et al. 2013a; Mitra et al. 2015; Rodríguez-Puebla et al. 2016). Inserting this assumption in equation (9) results in equation (11) as a description of the MS cycle and the expectation that the normalization (i.e. at fixed $M_\ast$) of the median $\psi - M_\ast$ relation/the MS should evolve as the product $\zeta \dot{M}_{\text{halo}}$ over the redshift range probed by our samples. Given this expectation, it is interesting to compare the shift in normalization, we find for the $\psi - M_\ast$ relation of field central disc

\(^{17}\) This refers to the efficiency with which ISM is converted to stars in the galaxy, and must be disambiguated from the use of SF efficiency by e.g. Behroozi et al. (2013a), who use it to refer to the ratio of SFR to the rate at which baryons are accreted on to the host DM halo of a galaxy.
galaxies with the expected evolution in the halo baryon accretion rate, thus empirically constraining the redshift evolution of $\xi$.

In the following, we have adopted the parametrization of the median halo mass accretion rate (and by extension the baryon accretion rate) derived from the Millennium simulation given by equation (2) of Fakhouri et al. (2010), which takes the form

$$M_{\text{halo}} \propto M_{\text{halo}}^{1.1} g(z)$$

(14)

In addition, for the mutual stellar mass range of the FCS and GCS samples, and in particular for $M_* \approx 10^{10.3}$, i.e. the median stellar mass of the LFCS and LGCS samples, we have empirically shown in the previous Section 5.2 that $\xi \propto M_{\text{halo}}^{1.1}$ at fixed $z$. Accordingly, combining equations (14) and (13), one finds that, for this stellar mass range, one expects

$$\xi M_{\text{halo}} = \xi M_{\text{halo}}^{1.1} g(z) \approx C M_{\text{halo}}^{0.9} g(z),$$

(15)

with the constant of proportionality $C$ potentially depending on redshift at fixed $M_*$. As a result, under the standard paradigm, the evolution with redshift $z$ of the median $\psi - M_*$ relation at fixed $M_*$ should be largely independent of halo mass, being dominated by the redshift dependence of $g(z)$ and potential redshift dependence of $C$. Furthermore, any residual halo mass dependence may additionally be expected to be negligible, as numerical integration of equation (2) of Fakhouri et al. (2010) finds the expected mass growth of haloes in the mass range covered by our samples ($M_{\text{halo}} \lesssim 10^{13.5}$) over the redshift range considered to be $z \lesssim 3$ per cent. Therefore, we choose to make use of the expression for $g(z)$ provided by Fakhouri et al. in deriving the redshift-dependent change in the halo baryon accretion rate between the $z_1$, $z_2$, and $z_3$ sub-samples of the FCS sample.

Thus, using the expression for $g(z)$ given in Fakhouri et al. (2010), we expect the halo baryon accretion rate to decrease by 0.06 dex (0.02 dex, 0.04 dex) from $z_1 \to z_1$ ($z_3 \to z_2$, $z_2 \to z_1$), i.e. $M_{\text{b,halo}} \approx (1+z)^{2.2}$.

We can now compare this expected decrease in the halo baryon accretion rate with the measured decrease in the specific star formation rate (sSFR) over redshift at the fiducial mass $M_* = 10^{10.3} M_\odot$ (the median mass of the LFCS sample), as derived from our power-law fits of the $\psi - M_*$ relation for the subsamples of the FCS sample (tabulated in Table 1). We find the measured decrease in sSFR of the FCS disc galaxies at this stellar mass to be $0.14 \pm 0.03$ dex ($0.04 \pm 0.01$ dex, $0.1 \pm 0.03$ dex) from $z_3 \to z_2$ ($z_2 \to z_1$). This corresponds to an evolution $\psi_* \propto (1+z)^{0.9}$ with $\beta = 4.9 \pm 0.9$ at the fixed value $M_* = 10^{10.3} M_\odot$.\footnote{In Section 5.3, we are using $M_* = 10^{10.3} M_\odot$ as the fiducial stellar mass at which the redshift evolution is measured, as this is the median stellar mass of the LFCS and LGCS samples for which we have empirically established a significant discrepancy in host halo mass between the group and field central disc galaxies combined with a perfectly overlapping $\psi_* - M_*$ relation. In Section 3, we have normalized our power-law fits at $M_* = 10^{10.5} M_\odot$, the median redshift of the FCS sample. We find the normalization of our fits, corresponding to the evolution of galaxies with $M_* = 10^{10.2} M_\odot$, to decrease by $0.12 \pm 0.02$ dex ($0.03 \pm 0.01$ dex, $0.09 \pm 0.02$ dex) from $z_3 \to z_2$, $z_2 \to z_1$. This corresponds to an evolution $\psi_* \propto (1+z)^{0.9}$ with $\beta = 4.3 \pm 0.3$, or a comparable fit to an extrapolation of the Speagle et al. (2014) parametrization of the MS to the same redshift range finds $\psi_* \propto (1+z)^{0.9}$ with $\beta = 4.5 \pm 0.3$. Thus, our measured evolution of the $\psi_* - M_*$ relation is consistent with the data at higher redshifts, although with a slightly flatter slope, which can be understood from Fig. 3.}

Accordingly, in order for the expectation formulated in equation (11) to be consistent with our empirical results, we would require the fuelling efficiency $\xi$ to decrease as $(1+z)^{2.7}$ for galaxies with stellar masses of $M_* = 10^{10.3} M_\odot$, i.e. in the range over overlap between the FCS and the LGCS samples.

Given the novel, direct nature of our results, it is interesting to compare them to other more indirect data-driven considerations, as well as to the results of full cosmological hydrodynamical simulations.

Amongst the latter, van de Voort et al. (2011a) considered the rate of accretion of baryons into the ISM and on to the host DMH of galaxies in their simulations, finding the ratio between the two to decrease between $z \approx 2$ and 0 (see their fig. 2). In particular, at a fixed halo mass of $M_{\text{halo}} = 10^{11.9} M_\odot$, they find the ratio to decrease by approx 0.5 dex between $z = 2$ and 1, i.e. $\propto (1+z)^{1.04}$ if parametrized as a single power law over the full redshift range. Given our empirical results, for the model to remain consistent with the data, the evolution of the ratio in the model must vary with redshift. A more detailed comparison of the evolution, however, is not possible due to the lack of (published) simulation results at low(er) redshifts. We urge the simulation community to consider providing more finely sampled (in time/redshift) results at low(er) redshifts, and to divert some further focus to the question of accretion on to galaxies versus accretion on to haloes.

We can also compare our results to those of Behroozi et al. (2013a,e), who find the ratio of SFR to baryon accretion rate (i.e. $\xi \propto \tau$) to display a weak time dependence, decreasing with decreasing redshift below $z \approx 0.8$ (Behroozi et al. 2013a) based on a detailed, empirically constrained combination of halo abundance matching and halo merger trees from numerical simulations.\footnote{Although Behroozi et al. consider the full galaxy population, as disc galaxies represent the dominant galaxy population for the relevant range in stellar mass (e.g. Paper I), our samples can be considered to be similar.} In fact, for $M_{\text{halo}} \approx 10^{11.9}$, i.e. the weak-length-derived DMH mass for the LFCS sample, these authors find the ratio of SFR to halo baryon accretion rate to decrease by approx 0.08 dex ($\approx 0.03$ dex, $\approx 0.05$ dex) between $z_3 \to z_1$ ($z_3 \to z_2$, $z_2 \to z_1$), i.e. $\propto (1+z)^{2.7}$, entirely consistent with the evolution of $\xi$ required by our results.\footnote{Behroozi et al. (2013a) provide their data in electronic form. We have interpolated the data provided at $z = 0.125, 0.095$, and 0.05 using a cubic spline. From the interpolation, for $M_{\text{halo}} = 10^{11.9} M_\odot$, we obtain $\log(\text{SFE}) = -0.76, -0.71$, and $-0.68$, respectively, where SFE is defined as the ratio between SFR and halo baryon accretion rate, i.e. is equivalent to $\xi \propto \tau$ in equation (11).} In this regard, it is furthermore noteworthy that, because our sample is comprised of morphologically selected discs, our results imply that the fall-off of $\xi$ with redshift for the overall galaxy population deduced by Behroozi et al. cannot be solely driven by an evolution in morphology from discs to spheroids with redshift.

In conclusion, the cosmological hydrodynamical simulations of van de Voort et al. (2011a) are inconsistent with our results with regard to the halo mass dependency of $\xi$ (see Section 5.2) and it is unclear whether or to which degree they are consistent with our results with regard to the redshift dependency, possibly hinting that our physical prescriptions for galaxy growth remain incomplete. On the other hand, our data are consistent with the evolution of $\xi$ with $z$ found in the empirically constrained analysis of Behroozi et al. (2013a), and qualitatively consistent, in terms of the halo mass dependence, with the empirically constrained analyses of Behroozi et al. (2013a) and Mitra et al. (2015).
Overall, while our measurements can be made to be qualitatively compatible with the predictions of the picture of SF in field central disc galaxies being determined by a gradually evolving inflow-driven self-regulated baryon cycle, this, requires ζ to evolve (decline) as \( (1 + z)^{-3/2} \) for galaxies with \( M_\ast = 10^{10.3} M_\odot \), i.e. that \( \zeta \) is a strong function of redshift. We will return to this, potentially problematic, finding below. Furthermore, we note that for galaxies with \( M_\ast = 10^{10} M_\odot \), we find a preferred evolution of \( \zeta \propto (1 + z)^{-3} \), which, although the results are consistent within their uncertainties, may hint at a dependence of \( \zeta \) on \( M_\ast \).

In addition, given our empirical result of the lack of influence of host halo mass on the \( \psi - M_\ast \) relation of central disc galaxies, maintaining this paradigm requires the fuelling efficiency \( \zeta \) to be linearly antiproportional to the halo baryon accretion rate, and thus to be a strong declining function of \( M_{\text{halo}} \). While this is in general agreement with recent indirect derivations based on a consideration of the global galaxy population (Behroozi et al. 2013a; Mitra et al. 2015), our direct constraints for the morphologically selected samples of galaxy properties including with regard to the larger scale environment of the galaxy, which drive the evolution observed in our analysis.

6.2 Co-evolution of \( \zeta \) and galaxy properties
Under the initial assumption that the standard paradigm for the baryon cycle holds (at least for field central disc galaxies), the relative constancy of the ratio of SFR to halo baryon accretion rate, i.e. the product \( \hat{\tau} \zeta \), identified by Behroozi et al. (2013a), implies that \( \zeta \) must evolve with redshift in a fashion correlated with the evolution of outflows of gas from galaxies (i.e. anticorrelated with \( \hat{\tau} \), as the mass loading of these outflows is contained in \( \hat{\tau} \) and varies with redshift. Thus, given the dependencies of \( \zeta \) on \( M_{\text{halo}} \) and \( z \) implied by our results, this requires a tight co-evolution of processes linked to the scales of the galaxy and the host DMH, respectively.

6.3 Stellar mass and (the redshift dependence of) the fuelling efficiency
In Section 5.3, we have shown that maintaining the gas-fuelling paradigm requires \( \zeta \) to be a strong function of \( z \), to the extent that at \( M_\ast = 10^{10.3} \) our empirical results require \( \zeta \propto (1 + z)^{-3/2} \), i.e. making \( \zeta \) a stronger function of \( z \) than of \( M_{\text{halo}} \). We have shown in Section 5.2 that \( \zeta \propto M_{\text{halo}}^{1.1} \propto M_\ast^{1.1} \). With \( \zeta \) in the formulation of the standard paradigm representing processes regulating the link between the galaxy (its inflows) and the environment on the scale of the DMH and being considered as a function of \( M_{\text{halo}} \) and \( z \), this finding must be considered problematic, as it is entirely unclear why such processes should display such a strong redshift dependence, while at the same time changes in halo mass and baryon content are expected to be mild over the redshift baselines considered here – as are possible changes in galaxy-specific properties such as SF efficiency.

The difficulty inherent in this finding is further compounded by the fact that \( \zeta \) would have to evolve significantly with redshift over a wide range in \( M_{\text{halo}} \). Under these circumstances, it becomes difficult to accept an evolution such that \( \zeta M_{\text{halo}} = \text{const.} \) at a given \( z \), albeit that the constant of proportionality might vary. Alternatively, and also problematically, one would have to assume that the epoch of \( z \approx 0.1 \), i.e. the median redshift of our sample, is special in the sense that it just so happens to be the epoch at which we find \( \zeta M_{\text{halo}} = \text{const.} \).

Finally, although only with marginal significance, our empirical results on the evolution of the \( \psi - M_\ast \) relation do indicate an evolving slope of the relation, as was also observed by Speagle et al. (2014). This finding is further borne out by our direct consideration of the implied redshift evolution of \( \zeta \) at different values of \( M_\ast \), which indicates an evolution varying as a function of stellar mass \( M_\ast \). Our results, therefore, provide an indication that the fuelling efficiency \( \zeta \) may, in fact, not be adequately described as a function of \( M_{\text{halo}} \) and \( z \), i.e. \( \zeta (M_{\text{halo}}, z) \approx M_{\text{halo}}^{1.1} g(z), \) but instead may also depend on the stellar mass of the galaxy, i.e. \( \zeta (M_{\text{halo}}, z, M_\ast) \approx M_{\text{halo}}^{1.1} g(z, M_\ast) \). We will return to this question in future work, but note that a functional dependence of this type, while easily preserving the ability to capture the empirical halo mass dependence of \( \zeta \), may allow for a shallower redshift dependence.
6.4 Influence of the gravitational potential of the host DMH on $\zeta$

Fundamentally, any inflow into the ISM of a galaxy must be sourced from gas sufficiently cool to be accreted, agnostic of its origin. In this context, $\zeta M_{b, h}$ simply parametrizes the flow of cool accretable baryons to the central galaxy as a function of rate with which baryons are accreted on to the DMH.

As discussed in Section 5.2, in order to maintain the standard baryon cycle paradigm our results require $\zeta \propto M_{-1, \text{halo}} \propto M^{-1.1}_{-1, \text{halo}}$ resulting in inflow rates to the central disc galaxies being invariant as a function of halo mass. The differing ratios of stellar mass to DMH mass for the group and field central disc galaxies, and the corresponding differences in the gravitational potential wells of the host DMHs, however, have a range of implications for the availability of hot and cool gas in the host DMH haloes of the central galaxies.

On the one hand, the rate of accretion of baryons on to the DMH is expected to increase with the mass of the DMH, thus increasing the total available gas mass. Conversely, depending on its mass, the host DMH of a galaxy will be possessed of a hot pressure supported atmosphere and a shock at or near the virial radius heating the infalling IGM.

Theory predicts the threshold halo mass for the existence of a stable shock, and thus a hot atmosphere, to be $\sim 10^{11.7-10^{12}} M_\odot$, depending on redshift and metallicity (e.g. Birnboim & Dekel 2003; Kereš et al. 2005, 2009; van de Voort et al. 2011a). Above the threshold mass, an increasing fraction of the baryon mass accreted on to the DMH is expected to be shocked, requiring it to cool prior to being available for accretion into the ISM of the central galaxy, with the cooling efficiency decreasing with DMH mass. Similarly, the fraction of un shocked/unheated gas which can be accreted directly is expected to decline with increasing DMH mass above the threshold halo mass (e.g. Kereš et al. 2005, 2009; van de Voort et al. 2011c; Nelson et al. 2013).

A quantitative assessment of the impact of the differing gravitational potentials on the availability of cold accretable gas has recently been provided by Faucher-Giguère et al. (2011) who analysed a suite of cosmological hydrodynamical simulations and found, cast in the simpler framework of the baryon cycle formulation adopted here, $\zeta_{\text{grav}} \propto M_{\text{halo}}^{0.25}$ (Davé et al. 2012; Mitra et al. 2015) with an onset of this effect above $M_{\text{halo}} \approx 10^{11.75} M_\odot$, where $\zeta_{\text{grav}}$ describes the halo mass dependence of the impact of gravitational heating processes on the fuelling efficiency. Thus, our empirical result of $\zeta \propto M_{\text{halo}}^{-1}$ implies some additional process that reduces the rate at which gas is accreted on to the central disc galaxy beyond the impact of the gravitational potential of the host DMH considered above, but which nevertheless scales with the DMH mass in a manner resulting in comparable inflows for field and group central disc galaxies at fixed stellar mass.

Before discussing further physical implications of this finding, we first consider the impact of the assumptions of our analysis. In particular, we have assumed that $\tau_{\text{res}}$ and $\hat{k}$, i.e. the residence time of a unit mass of gas in the ISM and the efficiency with which stars are formed from the ISM, depend solely on galaxy properties and are independent of the environment of the galaxy. In combination with the expected difference in inflow to the disc central galaxies arising from the impact of the gravitational potential of the halo this gives rise to the tension and the requirement of additional processes highlighted above. However, it may be reasonable to relax this assumption which might suffice to ameliorate the tension arising from the observed similarity of the $\psi-M_*$ relation of field and group central disc galaxies without the requirement of further mechanisms – in particular, by allowing for similar SFRs arising from different inflow rates.

For central galaxies of groups, the greater DMH mass will result in a deeper potential well and a higher virial temperature, which may, in turn, result in the medium surrounding the galaxy being more pressurized than that surrounding a field galaxy of comparable stellar mass. However, this would likely act to suppress outflows from the galaxy leading to an increase, rather than a decrease in $\tau_{\text{res}}$. At fixed SF efficiency $\hat{k}$, this would serve to exacerbate the tension as it would serve to increase the ISM mass and the SFR.

In contrast to the possible impact of the group environment on $\tau_{\text{res}}$, its potential impact on $\hat{k}$ might indeed serve to lessen the tension implied by our observations. While stellar mass and SFR of star-forming galaxies are tightly correlated, both quantities are also correlated with the metallicity of the galaxy. In fact, a hyperplane in the space spanned by these parameters can be identified which minimizes the scatter from the plane beyond that achievable by the consideration of only two out of three of the parameters as shown by (e.g. Mannucci et al. 2010; Lara-López et al. 2010, 2013). These authors find the SFR at fixed stellar mass to be anticorrelated with the metallicity of the galaxy, possibly as a result of the weaker feedback from lower metallicity O and B stars resulting in a greater efficiency in the conversion of ISM into stars (Dib et al. 2011).

Thus, depending on the difference in metallicity between group and field disc centrals, the inflow required to sustain a self-regulated SF at a fixed level might be larger for the former compared to the latter.

For an environment dependence of $\hat{k}$, driven by a metallicity difference between field and group central disc galaxies, to consistently explain the similarity in SFRs at different estimated inflow rates, however, this difference would have to evolve smoothly and in a highly balanced manner anticorrelated with the difference in host DMH of field and group central disc galaxies, while simultaneously accounting for any changes in the value of $\tau_{\text{res}}$ as a function of DMH mass. While possible, in principle, this would require a very high degree of finely tuned covariance, for which no mechanism is readily apparent.

Therefore, under the assumption that $\tau_{\text{res}}$ and $\hat{k}$ are indeed independent of the environment of the galaxy or, as is likely to be the case, do have limited environmental dependencies which, however, are not sufficient to ameliorate the observed discrepancies by themselves, maintaining the paradigm of an inflow-driven self-regulated baryon cycle, unequivocally requires (an) other mechanism(s) beyond gravitational heating of the IHM to regulate the rate of accretion on to the central galaxy, with this/these mechanism(s) scaling with the mass of the host DMH.

For the global population of galaxies, the result that gravitational heating alone appears to be insufficient to regulate the supply of gas to the central galaxies of massive haloes to levels consistent with observations is well known (e.g. Croton et al. 2006). To accommodate this finding, the current baryon cycle paradigm invokes (i) mechanism(s) for preventive feedback, loosely linked to feedback from AGN although the physics remain unclear, reducing the rate at which gas is accreted on to the central galaxy. Indeed, the recent MCMC fit to the global galaxy population of a simple parametrized equilibrium model of the baryon cycle, closely related to the model adopted here, by Mitra et al. (2015) find a preferred strong halo mass dependence ($\propto M_{\text{halo}}^{-0.5}$) of the unspecific preventive feedback assumed to be loosely linked to AGNs, and a resulting preferred composite fuelling efficiency parameter $\zeta \propto M_{\text{halo}}^{0.75}$ for the halo mass range considered in our analysis.

Here, we have shown that for our morphologically selected samples of disc central galaxies, we, qualitatively consistently with the
work of Mitra et al. (2015), also require a strong dependence of the fuelling efficiency $\zeta$ on the mass of the DMH in order to maintain the baryon cycle paradigm. However, our empirical results, representing the first direct constraints on $\zeta$ in this halo mass range, prefer a steeper dependence $\zeta \propto M_{\text{halo}}^{-1}$ and accordingly, a halo mass dependence of the unspecified feedback mechanism $\propto M_{\text{halo}}^{0.75}$.

### 6.5 The role of AGN feedback

AGN feedback may limit accretion either by (re)heating the cooling IIM and/or by driving outflows of gas out of the galaxy. While we cannot make detailed statements on the basis of our data, a consideration of our sample construction may be informative for the role of AGN feedback in determining $\zeta$.

In the construction of our samples, we have selected against AGN host galaxies using the Kewley et al. (2001) BPT criterion. Based on the ratio of emission lines in the optical, the BPT classification efficiently identifies radiatively efficient ‘luminous’ AGN with efficient accretion. The rejection rate of disc centrals from our samples on the basis of AGN activity, i.e. the galaxy would have been included save for the classification as an AGN host, is 10 per cent for the both FCS and GCS samples. Thus, as a rough estimate, if all of the galaxies in our sample were to contain a central supermassive black hole which periodically enters a stage in which it is visible as a BPT classified AGN, the fraction of 10 per cent AGN over a baseline of ca. 1 Gyr implies a total active phase of $\lesssim 10^8$ yr. Accordingly, this limits the fraction of time over which luminous AGNs are injecting energy, and thus limits the relevant AGN feedback modes.

Our samples thus do not support a currently active luminous AGN as the relevant feedback mechanism. However, if the energy input into the IIM during the active phases is sufficient to impact accretion until the next active phase, feedback from luminous AGN may not be the less important. In regard to the importance of radiatively inefficient AGN, we can make no statement based on our data, but do note that the star-forming disc galaxies in our samples are not the stereo-typical massive, elliptical galaxies with low gas-to-stellar mass ratios generally associated with ‘maintenance mode’ feedback from radiatively inefficient AGN.

### 6.6 Gas fuelling: inferred properties and possible processes

Of foremost importance amongst our results, the smooth evolution over short time-scales observed for the $\psi_e$–$M_e$ relation, and the fact that it so closely traces, and is well parametrized by, the evolution of the halo accretion rate, implies that the IIM of the galaxy’s host DMH appears to serve as a buffer for SF only in a very limited capacity. This finding has significant implications for the physical mechanism(s) underlying $\zeta$.

Importantly, in the adopted formulation, $\zeta$ embodies the efficiency with which all baryons are accreted into the ISM of the central galaxy, i.e. both those newly accreted on to the DMH from the IGM and thus intrinsically linked to the halo accretion rate, as well as those already present in the DMH being recycled. To first order, these two ‘sources’ can be mapped to the cold and hot accretion modes, respectively. Conceptually, at any given time, (i) some fraction of in-falling baryons cools efficiently/remains cold and is rapidly accreted on to the galaxy (i.e. cold mode), and (ii) some fraction of the baryons contained in the IIM of the galaxy cools and is subsequently accreted (i.e. hot mode), thus constituting the total accretion.

As our FCS sample extends to halo masses $M_{\text{halo}} \gtrsim 10^{12.8} M_\odot$, i.e. from halo mass for which cold mode accretion is expected to be dominant to such systems for which a significant contribution to the fuel for recent SF from gas that has been heated and has subsequently cooled is expected (e.g. Kereš et al. 2005, 2009; van de Voort et al. 2011b), our empirical results entail that the mechanism(s) encoded in $\zeta$ link(s) the accretion efficiency of baryons into the ISM via both modes to the instantaneous halo baryon accretion rate.

For low-mass DMHs, which are expected to lack a virial shock and a virialized atmosphere, the dominant cold accretion mode ostensibly meets the formulated requirements, although even here, it is not clear that the current SFR of the galaxy should trace the instantaneous halo baryon accretion, i.e. the accretion of baryons at a distance of $\sim r_{200}$. However, the uncertainties in the SFR and accretion rate determinations, as well as the ensemble averaging in the determination of the median values, may blur out the anticipated lag.

For more massive DMHs, on the other hand, an appropriate mechanism is less apparent. One possibility, is that the dominance of cold mode accretion extends to larger halo masses in the local Universe than suggested by the results of van de Voort et al. (2011b) and Nelson et al. (2013). Indeed, using the Omega25 suite of cosmological simulations, Wetzel et al. (2014) find that cooling is highly efficient for haloes with $M_{\text{halo}} = 10^{10.5}$–$10^{12}$ and $10^{12}$–$10^{13} M_\odot$ and that the rate of baryon accretion at all radii from the virial radius $r_{\text{vir}}$ down to $\sim 40$ kpc traces that at $r_{\text{vir}}$. However, these authors only considered very limited feedback in their simulations.

A possible additional cooling mechanism enabling such a scenario might be the additional efficient cooling of the IIM by dust injected into it by feedback from the galaxy. As Montier & Giard (2004) have shown that dust cooling can exceed gas-phase cooling in the IMF for dust-to-gas ratios $\gtrsim 10^{-4}$ by mass (ca. 1 per cent of the ISM value), this may prove feasible. In addition, a mechanism of this type, could also potentially give rise to a two-phase IIM, thus meeting the requirement identified in Paper I in the context of the SFRs of satellite disc galaxies.

Alternatively, one might speculate whether the expected filamentary accretion of cold IGM on to the halo might provide the required mechanism even in higher mass haloes. Numerical experiments find the filamentary inflows of cold gas to penetrate the hot gas halo to a degree varying with the halo mass before breaking up (e.g. van de Voort et al. 2011b; Nelson et al. 2013). If hot halo gas could cool, condense, and be entrained in the wakes of the cold clumps formed by the disrupting penetrating filament, e.g. as suggested for the galactic fountain model (Fraternali & Binney 2008; Marinacci et al. 2010; Armillotta, Fraternali & Marinacci 2016), this would provide a mechanism linking the accretion of cold and hot gas. Again, this process could be supported and enhanced by outflows from the galaxy, enriching the IIM with metals, and in particular dust, possibly reducing the temperature of the hot halo and favouring the survival of cold clumps and the condensation of hot gas. A change in the halo accretion rate would then lead to a change in the effective number of seed clouds, coupling the accretion from the hot IIM component to that of the cold as required. Similarly, increasing the DMH mass would reduce the degree to which the cold streams might penetrate, regulating the prevalence of seed clouds and allowing for a natural halo mass dependence.

It is, however, unclear whether the efficiency of entrainment and condensation, given the temperatures and densities of the hot halo gas would be sufficient to make this mechanism viable. If this scenario were valid, though, one would expect the number of cold dense gas clumps in the circum-galactic medium (CGM) to scale as the product of the halo mass and the ratio of the SFR to the halo mass accretion rate. Ongoing and future studies of the CGM...
properties, could thus, in principle, provide a further independent test of this speculative mechanism.

6.7 Implications for rotational support of gas in the IHM

A further important aspect of the accretion efficiency that also remains puzzling, but is strongly constrained by our results, is the contribution/importance of angular momentum. For example, Wetzel et al. (2014) find that in their simulations, at radii below ~40 kpc, i.e. still much larger than the radial extent of the galaxy, the gas experiences significant rotational support. Nevertheless, our results suggest that the final transition of halo baryons through this phase must occur on time-scales which are short compared to that on which the halo baryon accretion rate changes in order to maintain the observed correlation between SFR and halo accretion rate.

6.8 Beyond merger quenching

Penultimately, it remains important to note that our result of a strongly negative halo mass dependence of the fuelling efficiency \( \zeta \) for samples of disc-dominated galaxies clearly demonstrates that mechanisms unrelated to the morphological transformation of galaxies via mergers can play a central role in regulating and potentially eventually quenching SF in galaxies. Further support for this result is provided by the population of higher stellar mass quenched disc galaxies in the FCS sample as discussed in Paper I and Section 3.

6.9 Testing the standard paradigm

Finally, we highlight a possible test of the standard paradigm based on the methodology and results presented in this work.

In the context of the standard paradigm, our empirical result that the \( \psi_*-M_* \) relations of group and field central disc galaxies coincide, while the host DMH masses are discrepant, requires \( \zeta M_{\text{halo}} \propto \text{const.} \) for a fuelling efficiency \( \zeta (M_{\text{halo}}, z) \), if the redshift range of our sample is not unique, in the sense that a similar result is obtained at a different redshift, this poses a strong constraint on the possible differential redshift evolution of \( \psi_* \) as a function of \( M_{\text{halo}} \), e.g. \( \zeta (M_{\text{halo}}) \approx \text{const.} \) would require almost no differential evolution given the near linearity of \( M_{\text{halo}} \) as a function of \( M_{\text{halo}} \). If however, the observed evolution of the \( \psi_*-M_* \) relation requires a differential evolution this would unequivocally entail further dependencies of \( \psi_* \) (provided it can be assumed to be constant).

Upcoming surveys such as the Deep Extra-galactic Visible Legacy Survey\(^21\) (DEVILS) and the Wide Area Vista Extra-galactic Survey (WAVES; Driver et al. 2016a) will provide the data required to determine the \( \psi_*-M_* \) relations of group and field central disc galaxies at higher redshift, thereby facilitating this test. A further test will also be enabled by, e.g. WAVES (Driver et al. 2016a) which will significantly increase the volume over which studies of this type are possible in the local Universe. This provides the unique opportunity of also probing to lower and higher DMH masses to fully cover the range over which a transition between fuelling modes is expected.

7 SUMMARY AND CONCLUSIONS

We have presented a detailed investigation of the \( \psi_*-M_* \) relation for central disc galaxies using purely morphologically selected samples drawn from the GAMA survey, focusing, in particular, on the evolution of the relation over short redshift baselines in the local Universe and on its dependence on the mass of the host DMH of the central galaxy. In determining DMH masses, we have made use of the high-resolution imaging data provided by the KiDS survey and the bespoke KiDS galaxy–galaxy weak-lensing pipeline. We present our results in detail as an empirical reference for current and future theoretical and numerical work aimed at understanding the baryon cycle of these objects. Our investigation has found that:

(i) The median \( \psi_*-M_* \) relation of field central disc galaxies is consistent in both normalization and slope with the extrapolation of the empirical parametrization of the main sequence of star-forming galaxies presented by Speagle et al. (2014) at the median redshift of the sample.

(ii) The redshift evolution of the \( \psi_*-M_* \) in the local Universe, even over redshift baselines of \( \Delta z \approx 0.04 \), is characterized by gradual, smooth evolution of the normalization (and possibly the slope) at constant scatter. The observed evolution is entirely consistent (both in normalization and slope) with that expected for the main sequence.

(iii) The median \( \psi_*-M_* \) relations for field and group central disc galaxies coincide over the full mutual range in stellar mass and are statistically indistinguishable, with no significant evidence of an offset between the two. This is mirrored in the distributions of observed SFRs relative to the median SFR at fixed stellar mass for field and group central disc galaxies split into two ranges of stellar mass.

(iv) By contrast, the average host DMH masses of field and group central disc galaxies differ by \( > 0.6 \) dex \( (M_{\text{halo}} = 10^{11.9} \text{ and } 10^{12.5-10^{12.8}} M_{\odot}, \text{ for field and group central, respectively}) \) in the low stellar mass range \( (10^{9.8} M_{\odot} \leq M_* < 10^{10.6} M_{\odot}) \), while in the high stellar mass range \( M_* > 10^{10.6} M_{\odot} \) the average DMH masses are much more comparable \( (M_{\text{halo}} = 10^{12.5} \text{ and } 10^{12.8} M_{\odot}, \text{ respectively}) \), and in fact compatible with no significant difference).

Making use of the methods developed in Grootes et al. (2017) and simple analytical models of the baryon cycle of galaxies we demonstrate that:

(v) The observed \( \psi_*-M_* \) relation for central disc galaxies (both field and group centrals) over the full redshift range of our sample \( (z \leq 0.13) \) can be made compatible with the picture of a supply-driven self-regulated baryon cycle determining the SFR of these galaxies, including, potentially, the inflow rate of baryons into the ISM being determined by the product of the halo baryon accretion rate \( M_{\text{halo}} \) and the gas-fuelling efficiency \( \zeta \).

(vi) However, attaining this compatibility not only requires the gas-fuelling efficiency \( \zeta \) to be a strong function of redshift, i.e. \( \zeta \propto (1+z)^{2.7} \text{ at } M_* = 10^{10.3} M_{\odot} \text{ for } z \approx 0-0.13 \), but also requires \( \zeta M_{\text{halo}} \approx \text{const.} \text{ as a function of DMH mass, i.e. with } M_{\text{halo}} \propto M_{\text{halo}}^{-1.1} \text{ for } z \approx 0.2 \) and is drawn by the same
processes on the scale of the surrounding environment constrained by our local Universe sample.

(viii) A joint consideration of the ratio of SFR to halo baryon accretion rate, the ψ−M∗ relation, and the DMH mass for group and field central disk galaxies over a redshift baseline extending to intermediate redshifts (z ≥ 0.4) provides a sensitive test/constraint of the standard paradigm for the baryon cycle of star-forming galaxies.

(ix) Under the standard paradigm, the gas-fuelling efficiency ζ must evolve with redshift in a manner correlated with the evolution of the strength of the outflows from the galaxy, requiring a link between galaxy scale and DM halo scale processes. The physical mechanisms underlying ζ, both with regard to the required link to between galaxy and DM halo scale processes, as well as driving the α(1 + z)^3/7 redshift dependency remain unclear. We note, however, that a functional dependency of ζ on M∗, z, and Mhalo (rather than just on z and Mhalo) may allow for a shallower redshift dependence of ζ.

(x) The reservoir of gas constituted by the IHN only acts as a buffer for SF in a very limited, largely negligible manner as the SFR so closely traces the instantaneous halo baryon accretion rate. In essence, this implies that the combined system of IHN and ISM is in an equilibrium state, with a time-scale on which the equilibrium adjusts that is short compared to the rate of change of the cosmological infall to the halo.

(xi) Either cold mode accretion remains the dominant process in delivering gas for star formation to the ISM to higher DMH masses than currently thought (\( \gtrsim 10^{12.8} \, M_\odot \)), or the processes determining ζ link hot and cold mode accretion to the instantaneous halo baryon accretion rate equally. In both contexts, we suggest that cooling of the IHN by dust injected via stellar feedback may serve to increase the cooling rate and decrease the temperature of the IHN leading to and aiding in the formation of a multiphase (at least two) ISM.

Overall, our analysis finds the SFR of central disc galaxies, and in particular field central disc galaxies, can be made to be compatible with the standard paradigm of the baryon cycle of these galaxies which dominate the MS relation being determined by an inflow-driven self-regulated baryon-cycle, with the inflow depending on the evolving halo accretion rate and gas-fuelling efficiency, albeit with a significant degree of tension. In particular, we find that, in order to be compatible, our results very strongly limit the possible influence of halo mass on the SFR of central disc galaxies, requiring the efficiency of gas fuelling to scale anti-proportionally to the halo baryon accretion rate. Furthermore our results would require a strong redshift of the fuelling efficiency. The underlying mechanisms of such dependencies, however, remain unclear.

The results of our analysis clearly indicate that a wide range of processes determining the cycle of baryons through galaxies remain poorly understood. Nevertheless, in this work, we have provided a number of detailed, both qualitative and quantitative, constraints for current and future theoretical and numerical work addressing the question.

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REFERENCES

APPENDIX A: SELECTION OF THE LFCS AND HFCS SAMPLES

For our comparative investigation of the impact of DMH mass on the $\psi<!--<sup>←</sup>--> on central disc galaxies and their corresponding $\psi<-M>$ relation of central disc galaxies and their corresponding distributions of $\Delta \log(\psi)$ we require samples of field and group central disc galaxies constructed in such a manner as to alleviate the impact of the very different stellar mass functions of these objects, i.e. mass-matched samples. However, the steeply declining mass function of the FCS sample simultaneously limits the maximum attainable sample of unique galaxies. In constructing our samples we have therefore adopted the approach outlined in the following.
We begin by splitting the sample of group central disc galaxies at its median stellar mass, creating a low-mass (LGCS) and a high-mass (HGCS) sub-sample. For each of these samples, we compute the relative frequency of sources in bins of 0.2 dex width in \(M_\ast\). From the FCS sample, we then select all galaxies which reside in the stellar mass range of the LGCS and HGCS samples, respectively. As for the group central samples, we determine the relative frequency in bins of 0.2 dex width in \(M_\ast\), and identify the least populous bin, which we refer to as the normalization bin. From this bin, we select all galaxies, and then proceed to select samples of galaxies from all other bins by randomly drawing (without replacing) a number of galaxies corresponding to the relative frequency of the LGCS or HGCS sample for that mass bin, multiplied by the number of galaxies in the normalization bin. This procedure results in the mass-matched LFCS and HFCS sub-samples which we make use of in our comparison. We note that in terms of sample size, the LFCS and HFCS sub-samples represent the maximum size mass-matched samples of unique sources that can be constructed from the FCS sample.

**APPENDIX B: STACKED WEAK-LENSING DMH MASS ESTIMATES USING THE KIDS GALAXY–GALAXY LENSING PIPELINE**

The GAMA survey area used in the analysis presented overlaps with the KiDS (de Jong et al. 2015; Kuijken et al. 2015; de Jong et al. 2017) ESO public survey using the VST, thus providing imaging of sufficient quality to allow for a stacked weak-lensing analysis of our samples of field and group central disc galaxies in both the low and high stellar mass ranges. This makes use of cosmic shear measurements from KiDS (Kuijken et al. 2015; Hildebrandt et al. 2017; Fenech Conti et al. 2017). The KiDS data are processed by THELI (Erben et al. 2013) and ASTRO-WISE (Begeman et al. 2013; de Jong et al. 2015). Shears are measured using LENSFIT (Miller et al. 2013), and photometric redshifts are obtained from PSF-matched photometry and calibrated using external overlapping spectroscopic surveys (see Hildebrandt et al. 2016).

In our analysis, we have made use of the bespoke KiDS galaxy–galaxy weak-lensing pipeline which encompasses the creation of an azimuthally averaged ESD profile. We refer the reader to the dedicated works of the KiDS collaboration on weak lensing (e.g. Viola et al. 2015; Sifón et al. 2015; Brouwer et al. 2016; van Uitert et al. 2016; Dvornik et al. 2017) for a detailed description of the process. In a second step, the pipeline enables a halo model to be fit to the stacked ESD profile making use of the affine invariant MCMC ensemble sampler proposed by Goodman & Weare (2010) and implemented in PYTHON by Foreman-Mackey et al. (2013). Given our relatively small sample sizes and our selection of central galaxies, we adopt a single NFW profile (Navarro, Frenk & White 1997) as a halo model, using the mass–concentration relation of Duffy et al. (2008), i.e. with the DMH mass as a free parameter. Here, we define the mass of the halo as \(M_{200}\), i.e. the mass contained within the radius \(r_{200}\) for which the average density within the radius is 200 times the mean background density at the median redshift of our sample \(z = 0.1\). For the fit we use 150 walkers with a chain length of 50 000 steps, discarding the first 2000 steps as burn-in. For the DMH mass, we choose a flat prior in log space with \(10 < \log(M_{200}/M_\odot) < 15\). We report our results as the mode of the distribution, and the boundaries of the 68th percent highest probability density (HPD) interval (surrounding the mode).

In modelling the mass distribution with single NFW profile, we ignore any contribution from the central stellar component, i.e. the visible galaxy. However, this is, at least partially accounted for by the lower limit on our prior of \(\log(M_{200}/M_\odot) = 10\). Furthermore, this assumption is generally found to be reasonable, at least at the level of \(\lesssim 0.1\) dex in terms of derived mass, and likely better (e.g. Mandelbaum et al. 2006; Han et al. 2015; van Uitert et al. 2016), in particular given the small size of our stacks and the according inherent low signal-to-noise ratio.

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