Abstract: The goal of this research was to appraise the effect of combined inoculation on the performance of anaerobic digesters treating hardly degradable material, and particularly the pressed fine sieved fraction (PFSF) derived from wastewater treatment plants (WWTPs). Batch tests were conducted in mesophilic conditions in order to examine the optimal mixing ratio of inoculums. Mixing ratios of 100:0, 75:25, 50:50, 25:75, and 0:100 of three different inoculums were applied in the batch tests. The findings indicated that the inoculation of digested activated sludge with digested organic fraction of municipal solid waste (MSW) in the ratio 25:75 resulted in a higher PFSF degradation and a higher biogas yield. The results from the kinetic analysis fit well with the results from the batch experiment.

Keywords: biogas; pressed fine sieve fraction; kinetic model; batch anaerobic treatment

1. Introduction

The incremental demand for energy and strict environmental regulations for waste management are the most crucial challenges faced by European countries [1,2]. Energy based on fossil fuels is regarded as non-environmentally friendly and unsustainable [3]. In contrast, renewable bioenergy is an alternative solution to meet the electricity and heat requirements of the country with a cost-efficient and beneficial for the environment technology. Netherlands generates a vast amount of sludge from the livestock biogas farms and the wastewater treatment plants (WWTPs). Several treatment methods are applied to treat agricultural and industrial biowaste, with anaerobic digestion (AD) technology, among others, being widely applied [4–6].

Four steps (hydrolysis, acidogenesis, acetogenesis, and methanogenesis) occur during the AD process. AD produces energy in the form of biogas with the approximate composition of 55–70% \( \text{CH}_4 \) and 30–45% \( \text{CO}_2 \) [7]. The biogas can be used for heating or electricity production, as well as for mobility after upgrading [8–11]. The AD technology has the potential for further improvement and application within the EU, as biogas can play a key role in the bioenergy field [12–15]. Co-digestion has been reported as an alternative technique treating two or more substrates [16–18]. The positive effect of co-digestion is due to the balanced carbon to nitrogen (C:N) ratio (ideal ratio ranges from 20:1 to 30:1) being achieved by treating different substrates simultaneously [19]. Co-digestion can also provide the necessary alkalinity and nutrients in order to confront the drawbacks of the mono-digestion of recalcitrant materials [20]. Nowadays, research efforts aim to reinforce sustainability through materials recovery and reduced energy consumption [21,22]. An alternative technique has been demonstrated in several WWTPs by extracting fiber-based materials with sieves (fine sieved fraction). This material is highly cellulosic, and cannot be digested by itself; thus, it can be sustainably reused by applying anaerobic digestion technology.
The choice of the inoculum is essential for the degradation of recalcitrant biomass. A suitable inoculum contains a high number of active microbes that convert the organic matter to biogas. Therefore, the source of inoculum will affect the digestion performance, as it alters the degradation rate, biogas composition, digestion time, and reactor stability [23–25]. It is reported [26] that the inoculum is not only used to provide microbial species but also serves as a source of nutrients enhancing the microbial activity, and thus an elevated amount of biogas is produced. Another study stated that the amount of inoculum-to-substrate ratio has an effect only on the kinetics and not on the cumulative biogas yield [27]. Interestingly, regarding the effect of inoculum on biomass degradation, studies have focused on the inoculum type but not on the combined inoculation. This work aims to introduce the combined inoculation (co-inoculation) concept and its effect on the AD performance of the hardly degradable material. Pressed fine sieved fraction (PFSF) was selected as the substrate, and three inoculums were used for the experimental test. Fine sieving can be applied in wastewater treatment plants to recover the cellulose-rich slurries from the raw sewage. The derived fine sieved fraction (FSF) can be pressed and then be used for on-site energy recovery through anaerobic digestion.

The biogas yield and several process parameters were the main indicators to evaluate the efficiency of co-inoculation. The specific objectives of this study were to (1) determine the biogas yield of PFSF in mono-inoculated reactors; (2) examine the influence of the combined inoculation on the PFSF degradation; and (3) predict the biogas production using first-order and cone kinetic models.

2. Materials and Methods

2.1. Inoculums and Substrate

The digestates used as inoculums in this study were obtained from three different sources and their characteristics are shown in Table 1. The digestate IN1 was obtained from an anaerobic digester treating the anaerobic activated sludge in the WWTP of Garmerwolde, Groningen. The digestate IN2 was collected from an anaerobic bioreactor treating the organic fraction of municipal solid waste (MSW) in the MSW treatment plant of Attero in Groningen. The digestate IN3 was obtained from a livestock farm digester in Groningen treating cow manure. All of the digesters have been stably operated for many years.

Table 1. Characteristics of the inoculums and substrate used in the batch tests.

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Unit</th>
<th>IN1</th>
<th>IN2</th>
<th>IN3</th>
<th>PFSF</th>
</tr>
</thead>
<tbody>
<tr>
<td>pH</td>
<td></td>
<td>7.56</td>
<td>7.21</td>
<td>6.72</td>
<td>ND</td>
</tr>
<tr>
<td>TS g kg⁻¹</td>
<td></td>
<td>48.2 (1.1)</td>
<td>117.7 (1.3)</td>
<td>82.6 (1.9)</td>
<td>193.2 (9.5)</td>
</tr>
<tr>
<td>VS g kg⁻¹</td>
<td></td>
<td>30.2 (0.8)</td>
<td>64.8 (1.6)</td>
<td>61.3 (1.3)</td>
<td>174.8 (8.8)</td>
</tr>
<tr>
<td>VS/TS</td>
<td></td>
<td>0.63</td>
<td>0.55</td>
<td>0.74</td>
<td>0.91</td>
</tr>
<tr>
<td>COD g kg⁻¹</td>
<td></td>
<td>47.2 (1.7)</td>
<td>83.9 (4.3)</td>
<td>82.4 (5.2)</td>
<td>ND</td>
</tr>
<tr>
<td>VS/COD</td>
<td></td>
<td>0.64</td>
<td>0.77</td>
<td>0.74</td>
<td>ND</td>
</tr>
</tbody>
</table>

IN1, digestate from the reactor treating activated sludge; IN2, digestate from the reactor treating organic fraction of municipal solid waste (MSW); IN3, digested cow manure; and ND, not determined. The values are the average of the three determinations. The values in parentheses denote the standard deviation.

To maintain freshness and microbial activity, all inoculums were stored at 6 °C and reactivated at 37 °C for two days prior to use. The PFSF used for digestion was collected from the sewage treatment plant, Blaricum, the Netherlands, and was stored in airtight bottles at 6 °C to prevent possible hydrolysis.

2.2. Batch Tests

Biogas potential tests were implemented to evaluate the effect of the combined inoculation on biogas production. Glass bottles (300 mL) with 240 mL working volume and 60 mL head volume were used as batch digesters. The PFSF was digested with three different inoculums and their mixtures in
the ratios 75:25, 50:50, and 25:75 (Table 2). The inoculum-to-substrate ratio (ISR) was set to 2 (based on VS basis) as it is considered optimal based on the previous studies [24–29]. The bottles were filled with the appropriate amount of substrate and inoculum, distilled water, flushed with nitrogen for 5 min, and sealed with butyl rubbers. Control reactors were used containing solely the individual inoculums to correct the biogas from the combined inoculation. All the bottles were placed in a rotating incubator (150 rpm) at 36 °C for 30 days. Triplicate bottles were used in all experiments, and all values were means of triplicate ± standard deviation.

Table 2. Process conditions applied in the batch tests.

<table>
<thead>
<tr>
<th>Reactors</th>
<th>IN1</th>
<th>IN2</th>
<th>IN3</th>
<th>Organic load (g VS\textsubscript{substrate}·L\textsuperscript{-1})</th>
<th>ISR</th>
<th>Temperature (°C)</th>
<th>Replicates</th>
</tr>
</thead>
<tbody>
<tr>
<td>R1</td>
<td>100</td>
<td>0</td>
<td>0</td>
<td>12</td>
<td>2</td>
<td>36</td>
<td>3</td>
</tr>
<tr>
<td>R2</td>
<td>0</td>
<td>100</td>
<td>0</td>
<td>12</td>
<td>2</td>
<td>36</td>
<td>3</td>
</tr>
<tr>
<td>R3</td>
<td>0</td>
<td>0</td>
<td>100</td>
<td>12</td>
<td>2</td>
<td>36</td>
<td>3</td>
</tr>
<tr>
<td>R4</td>
<td>75</td>
<td>25</td>
<td>0</td>
<td>12</td>
<td>2</td>
<td>36</td>
<td>3</td>
</tr>
<tr>
<td>R5</td>
<td>50</td>
<td>50</td>
<td>0</td>
<td>12</td>
<td>2</td>
<td>36</td>
<td>3</td>
</tr>
<tr>
<td>R6</td>
<td>25</td>
<td>75</td>
<td>0</td>
<td>12</td>
<td>2</td>
<td>36</td>
<td>3</td>
</tr>
<tr>
<td>R7</td>
<td>75</td>
<td>0</td>
<td>25</td>
<td>12</td>
<td>2</td>
<td>36</td>
<td>3</td>
</tr>
<tr>
<td>R8</td>
<td>50</td>
<td>0</td>
<td>50</td>
<td>12</td>
<td>2</td>
<td>36</td>
<td>3</td>
</tr>
<tr>
<td>R9</td>
<td>25</td>
<td>0</td>
<td>75</td>
<td>12</td>
<td>2</td>
<td>36</td>
<td>3</td>
</tr>
<tr>
<td>R10</td>
<td>0</td>
<td>75</td>
<td>25</td>
<td>12</td>
<td>2</td>
<td>36</td>
<td>3</td>
</tr>
<tr>
<td>R11</td>
<td>0</td>
<td>50</td>
<td>50</td>
<td>12</td>
<td>2</td>
<td>36</td>
<td>3</td>
</tr>
<tr>
<td>R12</td>
<td>0</td>
<td>25</td>
<td>75</td>
<td>12</td>
<td>2</td>
<td>36</td>
<td>3</td>
</tr>
</tbody>
</table>

IN1, digestate from the reactor treating the activated sludge; IN2, digestate from the reactor treating the organic fraction of MSW; IN3, digested cow manure; and ND, not determined.

2.3. Analytical Methods

Total solids (TS; g·kg\textsuperscript{-1}) and volatile solids (VS; g·kg\textsuperscript{-1}) were calculated according to the recommendations of the Standard Methods of Eaton et al. (2005) [30]. The pH value was measured using a pH meter (HI991001, Hanna Instruments, Woonsocket, RI, USA). The chemical oxygen demand (COD; g·kg\textsuperscript{-1}) was determined using assay kits (Hach Lange GmbH, Düsseldorf, Germany) according to the manufacturer’s instructions and was quantified by a spectrophotometer (DR/2010, Hach, Loveland, CO, USA). Total alkalinity (g CaCO\textsubscript{3}·L\textsuperscript{-1}) was determined using Nordmann titration method [31]. Technical digestion time is the time needed to produce 80% of the maximal digester biogas [32]. The biogas volume (mL·g VS\textsubscript{substrate}·day\textsuperscript{-1}) was measured with the water displacement method and was standardized according to DIN 1343 (standard conditions—temperature (T) = 0 °C and pressure (P) = 1.013 bar) [33]. The gas equipment used in this work was capable of providing biogas data with 5% accuracy [34]. The biogas volume was normalized according to the equation [35]

\[
V_N = \frac{V \times 273 \times (760 - p_w)}{(273 + T) \times 760}
\]

where \(V_N\) is the volume of the dry biogas at standard temperature and pressure (mL\textsubscript{N}), \(V\) = recorded volume of the biogas (mL), \(p_w\) = water vapor pressure as a function of ambient temperature (mmHg), \(T\) = ambient temperature (K). The water vapor pressure (\(p_w\)) was estimated according to the modified Buck equation [36]

\[
p_w = P(T) = 0.61121 \times 7.500617 \times \exp \left( \left( 18.678 - \frac{T}{234.5} \right) \left( \frac{T}{257.14 + T} \right) \right)
\]

where \(P(T)\) is the vapor pressure in mmHg, and \(T\) is the temperature at the ambient space (°C).
2.4. Kinetic Study

The first-order kinetic model and cone model were applied and their equations are [37,38]

\[ G(t) = G_O \times \left( 1 - e^{(-Kt)} \right) \]

\[ G(t) = \frac{G_O}{1 + (Kt)^{-n}} \]

\( G(t) \) is the cumulative biogas yield at the digestion time \( t \) days (mL biogas · g VS substrate\(^{-1}\)), \( G_O \) is the maximum biogas potential of the substrate (mL biogas · g VS substrate\(^{-1}\)), \( n \) is the shape factor, \( K \) is the biogas production rate constant (d\(^{-1}\)), and \( t \) is the time (days). The predicted data were plotted with the experimental biogas data. For the validation of the models, the statistical indicators root mean square error (RMSE) and correlation coefficient (\( R^2 \)) were calculated from the equations [39]

\[ \text{RMSE} = \left( \frac{1}{m} \sum_{j=1}^{m} d_j^2 \right)^{\frac{1}{2}} \]

\[ R^2 = \left[ \frac{m \left( \sum_{j=1}^{m} X_j Y_j \right) - \left( \sum_{j=1}^{m} X_j \right) \left( \sum_{j=1}^{m} Y_j \right)}{\sqrt{m \left( \sum_{j=1}^{m} X_j^2 \right) - \left( \sum_{j=1}^{m} X_j \right)^2} \left[ m \sum_{j=1}^{m} Y_j^2 - \left( \sum_{j=1}^{m} Y_j \right)^2 \right]} \right]^2 \]

where \( d_j \) is the deviation between the \( j \)th measured and the predicted values, and \( m \) is the number of data points; and

2.5. Statistical Analysis

Statistical significance of the data was determined by one-way ANOVA using Microsoft Office Excel (Microsoft, USA) with a threshold \( p \)-value of 0.05.

3. Results

3.1. Biogas Production

The cumulative biogas yield (mL·g VS substrate\(^{-1}\)) and the daily biogas production rate (mL·g VS substrate\(^{-1}\)·day\(^{-1}\)) were calculated in order to evaluate the effect of combined inoculation on the anaerobic digestion of PFSF. In the mono-inoculation, the biogas production rapidly began on the first day of digestion in all of the digesters (Figure 1).
The results in this study are lower to those of the methane derived from the anaerobic digestion of FSF at 35 °C [40]. Elbeshbishy et al. [42] concluded that the inoculum obtained from a digester treating food waste. Lignocellulosic fibers are often present in the organic fraction of MSW; therefore, the microorganisms and enzymes present in the sludge were likely to get adapted to a lignocellulosic substrate [43].

The high daily biogas production rate in R1 and R2 digesters were 79.4 mL·g VS_{substrate}^{-1} on the 5th day and 77.3 mL·g VS_{substrate}^{-1} on the 2nd day, respectively. As seen in Figure 1, the daily biogas amount in R1 and R2 remained above 25 mL·g VS_{substrate}^{-1} until the 7th and 10th day, respectively, and thereafter dropped to a lower level (<10 mL·g VS_{substrate}^{-1}·day^{-1}). The R3 digester treating the FSF with the digested cow manure sludge showed a biogas production rate of 51.8 mL·g VS_{substrate}^{-1} on the 3rd day of the digestion.

In order to enhance the degradation of the PFSF, a combined inoculation was applied in different mixtures ratios (75:25, 50:50, and 25:75) of the inoculums while operating the digesters R4 to R12 at the ISR of 2. A similar trend to R1 and R2 was shown by the reactors R4 to R6 with the mixing ratios 75:25, 50:50, and 25:75 reaching the maximum daily biogas yields of 82.4, 83.5, and 96.6 mL·g VS_{substrate}^{-1}, respectively (4th day). The daily biogas production was fluctuating during the time period of 1 to 8 days of digestion with the range of 30–80 mL·g VS_{substrate}^{-1}·day^{-1}, and then gradually declined in the range of 5–15 mL·g VS_{substrate}^{-1}·day^{-1}. The use of digested cow manure as co-inoculum (R8 to R12) resulted in a lower daily biogas yield.

After 28 days of digestion, the cumulative biogas production of R1 and R2 reached to 418.9 and 427.6 mL·g VS_{substrate}^{-1}, respectively, against 273.0 mL·g VS_{substrate}^{-1} achieved in R3 (Table 3). The results in this study are lower to those of the methane derived from the anaerobic digestion of FSF at 35 °C [40]. The inoculum source is crucial to ensure operational stability and to reinforce the performance of the anaerobic digestion [41]. Elbeshbishy et al. [42] concluded that the inoculum obtained from a digester treating municipal wastewater sludge was superior to the inoculum obtained from a digester treating food waste. Lignocellulosic fibers are often present in the organic fraction of MSW; therefore, the microorganisms and enzymes present in the sludge were likely to get adapted to a lignocellulosic substrate [43].
Table 3. Biogas yield, volatile solids (VS) removal, and technical digestion time for all the reactors.

<table>
<thead>
<tr>
<th>Reactor</th>
<th>Biogas Yield (mL·g VS\textsubscript{added}−1)</th>
<th>VS Removal (%)</th>
<th>T80 (day)</th>
</tr>
</thead>
<tbody>
<tr>
<td>R1</td>
<td>418.9 (26.4)</td>
<td>41.7 (3.9)</td>
<td>7</td>
</tr>
<tr>
<td>R2</td>
<td>427.6 (19.7)</td>
<td>43.5 (2.6)</td>
<td>12</td>
</tr>
<tr>
<td>R3</td>
<td>273.0 (12.9)</td>
<td>30.8 (2.8)</td>
<td>15</td>
</tr>
<tr>
<td>R4</td>
<td>468.2 (24.6)</td>
<td>45.4 (4.1)</td>
<td>6</td>
</tr>
<tr>
<td>R5</td>
<td>461.3 (26.8)</td>
<td>44.0 (3.9)</td>
<td>6</td>
</tr>
<tr>
<td>R6</td>
<td>479.7 (27.0)</td>
<td>48.2 (4.6)</td>
<td>8</td>
</tr>
<tr>
<td>R7</td>
<td>384.6 (17.2)</td>
<td>36.1 (2.5)</td>
<td>8</td>
</tr>
<tr>
<td>R8</td>
<td>377.1 (16.8)</td>
<td>35.6 (3.0)</td>
<td>12</td>
</tr>
<tr>
<td>R9</td>
<td>347.2 (16.3)</td>
<td>31.9 (2.7)</td>
<td>14</td>
</tr>
<tr>
<td>R10</td>
<td>374.8 (18.4)</td>
<td>37.5 (3.4)</td>
<td>9</td>
</tr>
<tr>
<td>R11</td>
<td>345.7 (20.3)</td>
<td>38.6 (2.9)</td>
<td>10</td>
</tr>
<tr>
<td>R12</td>
<td>340.2 (19.5)</td>
<td>35.3 (3.1)</td>
<td>8</td>
</tr>
</tbody>
</table>

Values are the average of three determinations; the values in parentheses denote the standard deviation.

Looking at the optimal mixing ratio, only R6 with an IN1/IN2 ratio of 25:75 showed a higher influence on the biogas yield. The R6 reached 479.7 mL·g VS\textsubscript{substrate}−1 over the 468.2 and 461.3 mL·g VS\textsubscript{substrate}−1 produced in R4 and R5, respectively (Figure 2). The IN1/IN2 mixing ratio of 25:75 increased the biogas yield approximately 18.5% in R6 in comparison to the mono-inoculation in R1 and R2 with the average biogas yield of 395.7 and 386.2 mL·g VS\textsubscript{substrate}−1, respectively. The combined inoculation can possibly support nutrient enrichment that is very important for the anaerobic digestion process. However, the ISR of 2 has been previously reported as an optimum for the biogas production [24–29].

![Figure 2](image-url)
higher than that achieved in R3 (Figure 1) indicating the enhanced activity of IN1 and IN2 resulting in sufficient organic mass degradation. The technical digestion time (T80—80% of the maximum biogas production) for all the reactors is given in Table 3. In general, the required periods (T80) observed in our experiments were considerably higher than the ones described in the literature.

3.2. pH and Alkalinity

The pH values in the reactors before and after digestion are shown in Figure 3. The initial and final pH values for most of the reactors ranged from 7.0 to 7.5, which were suitable for the anaerobic digestion process. The reactor with the inoculum of digested cow manure showed lower pH values, which has inhibited the biogas production. However, reactors inoculated with the digested cow manure ≥50% resulted in the final pH being lower than the starting pH. The optimal pH range for the anaerobic digestion is regarded 6.8–7.4, which is favorable for the microbes within the reactor [44]. However, hydrolytic and acidogenic bacteria prefer pH values within the range of 5.5–6.5. The pH of the digester influences the degradation of organic matter, as fluctuations cause disturbances in the microbial activities and the subsequent metabolomics pathways [45–47]. Low pH values can significantly inhibit the reactor operation and subsequently, the digester comes to a ‘sour’ situation. This is ascribed to the production and accumulation of volatile fatty acids (VFA) in the initial phase of anaerobic digestion [45–48].

![Figure 3. The pH value for reactors treating PFSF inoculated with three different inoculums and their mixtures.](image)

The total alkalinity of the mono- and co-inoculated reactors before and after the digestion is limned in Figure 4. No extra alkalinity was added in this study and the only source of alkalinity was the inoculum. Alkalinity represents the buffer capacity of the reactors and is a reliable parameter to evaluate the stability of the reactors [20].
The pattern of alkalinity showed a tendency similar to that of pH. The alkalinity of the reactors increased at the end of the experiment except the ones inoculated with the digested cow manure ≥50%. The reduction of pH may be countered by the produced alkalinity in the form of bicarbonate and carbon dioxide and ammonia; this alkalinity can offset the imbalance occurred from the pH reduction [49,50].

3.3. VS% Removal

In order to examine the degradation efficiency and correspondence with the biogas produced, the degradation of volatile solids was determined. The calculated VS removal of the reactors is given in Table 3. R6 showed the highest VS degradation rate of 48.2% following by R4 and R5 with degradation rates of 45.4% and 44.0%, respectively. The reactors with 25% IN3 revealed a more rapid biogas production in comparison to those with ≥50% IN3. This might be due to the fast release of the oligomers and monomeric sugars affecting the reactivity of the polymers.

Oligomer solubility could potentially play an important role in controlling the degradation in the hydrolysis of hemicellulose [51]. Li et al. [52] cited that high VS removal was ascribed to the sludge availability (ISR of 2) providing a buffering capacity and a sufficient microbial pool. The high FSF degradability can be justified by the low cellulosic fibers content [40]. Pommier et al. [53] stated that the heterogeneous biodegradability of different types of paper might be due to the lignin content and its structure that perchance burdens the degradation of hemicellulose components from the enzymes. From another aspect, the functional relationship of cumulative biogas yield and VS% removal was plotted in Figure 5.
A linear regression equation was established ($Y = 0.083X + 6.531$, $R^2 = 0.8699$) and as expected, the increment of cumulative biogas yield followed a pattern similar to the VS removal. The high correlation coefficient ($R^2$) indicated that there was a positive and significant correlation between the biogas yield and the degradation percentage of the organic material. The addition of the manure does not favor the biogas production as it contains a higher fraction of complex structured carbohydrates [54].

3.4. Kinetics Results

The kinetic parameters obtained by applying the first-order and cone models are summarized in Table 4 that gives a picture of the kinetics. The kinetic constants of each reactor were calculated based on the T80 (time needed for 80% biogas production) of itself. To validate the soundness of the results in the first-order model and cone model, the predicted values of biogas were plotted against the measured values (Figure 6).

### Table 4. Results of the study using first-order kinetic and cone models.

<table>
<thead>
<tr>
<th>Reactor</th>
<th>First-Order Model</th>
<th>Cone Model</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>$K$ (day$^{-1}$)</td>
<td>$R^2$</td>
</tr>
<tr>
<td>R1</td>
<td>0.2967</td>
<td>0.9244</td>
</tr>
<tr>
<td>R2</td>
<td>0.1421</td>
<td>0.9906</td>
</tr>
<tr>
<td>R3</td>
<td>0.0941</td>
<td>0.9292</td>
</tr>
<tr>
<td>R4</td>
<td>0.346</td>
<td>0.9692</td>
</tr>
<tr>
<td>R5</td>
<td>0.3066</td>
<td>0.9858</td>
</tr>
<tr>
<td>R6</td>
<td>0.3619</td>
<td>0.9738</td>
</tr>
<tr>
<td>R7</td>
<td>0.2239</td>
<td>0.9513</td>
</tr>
<tr>
<td>R8</td>
<td>0.1377</td>
<td>0.9779</td>
</tr>
<tr>
<td>R9</td>
<td>0.0969</td>
<td>0.9917</td>
</tr>
<tr>
<td>R10</td>
<td>0.2161</td>
<td>0.9292</td>
</tr>
<tr>
<td>R11</td>
<td>0.1992</td>
<td>0.9555</td>
</tr>
<tr>
<td>R12</td>
<td>0.2294</td>
<td>0.9838</td>
</tr>
</tbody>
</table>
which speed up the degradation of insoluble and complex particles. The fast acidification step should
possibly reduce the ammonia inhibition and further enhance the methanogenesis step. Reactors
co-inoculated with IN3 followed a lessening trend as the digested cow manure increased. This was
expected as the mono-inoculation with the digested MSW or anaerobic sludge (≈243.3 mL∙g VSsubstrate⁻¹) in
comparison to R1 and R2 (≈423.3 mL∙g VSsubstrate⁻¹). One possible reason for the improved hydrolysis
of the substrate is the synergistic effect of the different microbial species contained in the inoculums,
which speed up the degradation of insoluble and complex particles. The fast acidification step should
possibly reduce the ammonia inhibition and further enhance the methanogenesis step. Reactors
co-inoculated with IN3 followed a lessening trend as the digested cow manure increased. This was
expected as the mono-inoculation with the digested cow manure resulted in 273.0 mL∙g VSsubstrate⁻¹, significantly lower
(≈35.5%) than the mono-inoculation with the digested MSW or anaerobic sludge (427.6 and 418.9 mL∙g VSsubstrate⁻¹, respectively). Increasing the fraction of the digested cow manure from 25 to 75% resulted in a decrease (≈9.5%) on the biogas yield for R7 to R9 and R10 to R12, possibly due to the poor methanogenesis rate. Although the hydrolysis was slower in co-inoculated R4, R5, and R6, the microbial interactions from the inoculums possibly favored the whole process and yielded a high biogas amount.

**Figure 6.** Plots of the measured and the predicted biogas yields from the reactors treating PFSF
inoculated with three different inoculums and their mixtures (IN1, digestate from the reactor treating
the activated sludge; IN2, digestate from the reactor treating the organic fraction of MSW; and IN3,
digested cow manure).

The low values of RMSE reflect the models’ high ability to accurately predict the bioactivities.
An R-squared value equal to 1 implies that the model provides a perfect prediction, and 0 implies that
there is no relationship between the measured and the predicted value.

Based on the above results, the cone model had a better fit with the experimental results, and R6
and R5 showed the highest hydrolysis rate 0.3619 ($R^2 = 0.9738$) and 0.3755 ($R^2 = 0.9927$) in the first-order
and cone models, respectively. It is notable that the difference between the measured and the predicted
values of both the models was less than 5% for all the reactors.

The constant (K) was derived from the slope of the linear regression line plotted for the
accumulated biogas amount against time for the mono-inoculated and co-inoculated digesters.
The reaction rate coefficient (k) values were similar to those obtained by treating FSF in an ISR of 2
and at 35 °C [55]. The R1 and R2 inoculated with IN1 and IN2 showed significantly faster hydrolysis
degradation, and indicated a positive effect of the combined inoculation on the biogas production.
Reactors R4, R5, and R6 produced significantly higher biogas amount ($≈469.7$ mL∙g VSsubstrate⁻¹) in
comparison to R1 and R2 ($≈243.3$ mL∙g VSsubstrate⁻¹). One possible reason for the improved hydrolysis
of the substrate is the synergistic effect of the different microbial species contained in the inoculums,
which speed up the degradation of insoluble and complex particles. The fast acidification step should
possibly reduce the ammonia inhibition and further enhance the methanogenesis step. Reactors
co-inoculated with IN3 followed a lessening trend as the digested cow manure increased. This was
expected as the mono-inoculation with the digested cow manure resulted in 273.0 mL∙g VSsubstrate⁻¹, significantly lower
(≈35.5%) than the mono-inoculation with the digested MSW or anaerobic sludge (427.6 and 418.9 mL∙g VSsubstrate⁻¹, respectively). Increasing the fraction of the digested cow manure from 25 to 75% resulted in a decrease (≈9.5%) on the biogas yield for R7 to R9 and R10 to R12, possibly due to the poor methanogenesis rate. Although the hydrolysis was slower in co-inoculated R4, R5, and R6, the microbial interactions from the inoculums possibly favored the whole process and yielded a high biogas amount.
4. Conclusions

The PFSF was anaerobically treated in batch mode with different inoculums and their mixtures. The findings from the batch tests revealed that the combined inoculation can enhance the biogas production. Reactors with a mixing ratio 25:75 of the digestate from an anaerobic digester treating anaerobic activated sludge and the digestate from an anaerobic bioreactor treating the organic fraction of municipal solid waste (MSW) showed approximately 18.5% higher biogas yield in comparison to the mono-inoculated reactors. In addition, the kinetic models fitted well with the experimental data and showed that co-inoculation provided a lower hydrolysis rate.

Notwithstanding, the findings call into question if the combined inoculation represents an efficient solution for the anaerobic digestion as the microbiome of each inoculum impacts differently the final biogas yield and composition. Hence, we suggest an investigation of the underlying mechanisms such as the dominant microbiomes in the three inoculations, the synergistic effect between different dominant organisms, and the specificity of the substrate. In addition, financial and ecological evaluation would be interesting in order to assess factors other than the mixing ratio for full-scale applications.

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References

1. Sahajwalla, V. Green processes: Transforming waste into valuable resources. *Engineering* 2018, 4, 309–310. [CrossRef]
13. Wen-Wei, L.; Han-Qing, Y. Advances in energy-producing anaerobic biotechnologies for municipal wastewater treatment. *Engineering* 2016, 2, 438–446. [CrossRef]


