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Sensitivity of micromechanical actuation on amorphous to crystalline phase transformations under the influence of Casimir forces

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Nowadays, fluctuation induced electromagnetic (EM) forces between neutral bodies become increasingly important in microelectromechanical systems (MEMS). These forces between two objects arise due to perturbation of quantum fluctuations of the EM field as it was predicted by H. Casimir in 1948 assuming two perfectly reflecting parallel plates. Following Casimir’s calculation, Lifshitz and co-workers in the 50’s (Ref. 3) considered the general case of real dielectric plates by exploiting the fluctuation-dissipation theorem, which relates the dissipative properties of the plates (optical absorption by many microscopic dipoles) and the resulting EM fluctuations. The theory correctly describes the attractive interaction due to quantum fluctuations for all separations covering both the Casimir (long-range) and van der Waals (short-range) regimes.1,3

The dependence of the Casimir force on materials is an important topic since, in principle, one can tailor the force by engineering the boundary conditions of the electromagnetic field with a suitable choice of materials.5–12 The latter allows engineering the boundary conditions of the electromagnetic field with a suitable choice of materials.5–12 The latter allows the exploration of new concepts in actuation dynamics of MEMS. This is because MEM engineering is conducted at the micrometer to nanometer length scales. As a result Casimir forces become of increasing interest because MEMS have surface areas large enough but gaps small enough for the Casimir force not only to draw components together but also to lock them permanently.1,4,13–25 This effect is known as stiction causing device malfunction. On the other hand, the irreversible adhesion of moving parts resulting in general from Casimir and electrostatic forces can be exploited to add new functionalities to MEMS architectures.1 Therefore Casimir interactions will inevitably need to be faced with particular attention to the troublesome pull-in instabilities, for example, in microswitches.1,3–25

In fact, microswitches are essential MEMS components that are typically constructed from two electrodes of which one is fixed, and the other is suspended by a mechanical spring governed by Hooke’s law.10 The application of a bias voltage between the electrodes actuates them towards each other, but it is possible that the moving component to become unstable and collapse (pulls-in) onto the other.13,16 Residual stress and fringing field effects have also been shown to have great influence on the behavior of microswitches and strongly influence their failure characteristics.17,18 Recently, using the measured optical response and surface roughness topography as input;25 realistic calculations have been performed to account for Casimir and electrostatic forces on actuation dynamics of microswitches. It was found that surface roughness ensured that stable equilibrium can be reached more easily than in the case of flat surfaces stimulating further understanding of MEMS stability issues operating at separations ⩽ 100 nm.

So far, however, a detailed study of the sensitivity of actuation dynamics on a systematic variation of the measured optical properties of interacting materials without variation of their composition is missing. This motivated our attempts to explore MEMS actuation dynamics with phase change materials (PCMs),8,9 which are renowned for their use as active media in rewritable optical data storage (e.g., CD, DVD, and blue-ray disks), and their optical properties can be changed reversibly in response to a simple stimulus (e.g., local heating by a laser) leading to reversible switching between amorphous and crystalline phases. This is stimulated by the fact that we have already demonstrated that PCMs are promising to achieve significant force contrast ∼ 25%8,9 without composition changes, paving the way for a high repetition rate switchable force device with possible applications in MEMS.

II. FORCE THEORY AND MODELLING

As Fig. 1(a) illustrates, we consider for our study a moving sphere coated with gold (Au) interacting with a fixed plate coated with thick PCM film (optically bulk; thickness ⩾ 100 nm) with optical properties, as depicted in Fig. 1(b) those of AIST (Ag5In5Sb60Te30).8,9 The force in the sphere-plate geometry (widely used in force measurements by atomic force microscopy-AFM and MEMS9–10) is given by $F_{c}(z) = 2\pi R E_{c}(z)$ with $R$ being the sphere radius, $z$ is the sphere-plate separation (assuming $z \ll R$), and $E_{c}(z)$ is the Casimir energy in the parallel plate configuration that is calculated via Lifshitz...
theory. Therefore we have\(^3\)

\[
F_C(z) = k_b TR \sum_{n=0}^\infty \sum_{v=s,p} \int_0^\infty q \ln \left(1 - r_1^2 r_2^2 e^{-2|k_0|z}\right) dq.
\]  

(1)

The sum over the \(v\) index is for the transverse electric and magnetic field modes \((s = TE, p = TM)\). \(r_i^p (i = 1, 2)\) are the Fresnel reflection coefficients \(r_i^p = (k_0 - k_i)/(k_0 + k_i)\), \(r_i^n = (\varepsilon_i k_0 - \varepsilon_0 k_i)/(\varepsilon_i k_0 + \varepsilon_0 k_i)\), and \(k_m = \sqrt{\varepsilon_m (\omega^2/c^2) - q^2} (m = 0, 1, 2)\) with \(q\) an in-plane wave vector. The summation over the \(n\) index is over the Matsubara frequencies \(\omega_n = j(2\pi nkT)/h\) with \(n = 0, 1, 2, \ldots\), where the \(n = 0\) term is taken only half.\(^3\) The \(\varepsilon_{1(=\text{Au})}(\omega)\) and \(\varepsilon_{2(=\text{AIST})}(\omega)\) those of AIST\(^8,9\) \(\varepsilon_{\text{Au}} = 1\) since vacuum is the intervening medium. It should be mentioned also that in the sphere-plane geometry, we consider here the residual contact potential dependence on separation can lead to undesirable effects. Measurements of the contact potential difference vs. separation for PCMs\(^6\) indicated a residual electrostatic contribution 1–6\% for 50–150 nm. Therefore, for a force contrast of ø25\%,\(^8\) this is not expected to play significant role, however, one has to remain cautious concerning electrostatics.

The inset of Fig. 1(b) shows calculations of \(F_C(z)\) for both PCM phases. Tests with three different optical data sets of Au\(^11\) show also that the preparation conditions of the passive actuating material is playing minor role on the force contrast. To achieve, however, the force contrast with PCMs the area that undergoes phase transformation must be larger than the effective interaction area \(A_C \approx L_C^2\) of the Casimir force between sphere plate. For a sphere–plate separation \(z (\ll R)\), we have \(L_C \sqrt{(2/3)Rz}\).\(^26\) Moreover, the minimum thickness of the PCM film must be larger than the skin depth \(\delta\) in the IR range where the crystalline PCM has strong absorption due to free carriers and contribute ø50\% of the force contrast.\(^3\) For AIST, we obtain \(\delta = c/\omega_p \sim 100\) nm with \(c\) being the velocity of light and \(\omega_p\) the free carrier plasma frequency.\(^3\) For a minimum thickness \(d_{\text{PCM}} \approx \delta (\sim 100\) nm), the energy necessary for crystallization is given by \(E_{A \rightarrow C} = (L_C^2 d_{\text{PCM}}) \int_{T_m}^{T_c} C_p(T) dT\) with \(C_p\) the specific heat capacity, \(T_{RT} = 300\) K, and \(T_c = 451\) K the crystallization temperature for AIST.\(^27,28\) The energy necessary for amorphization (via melting at \(T_m = 807\) K) is given by \(E_{C \rightarrow A} = (L_C^2 d_{\text{PCM}}) \int_{T_m}^{T_c} C_p(T) dT + L_v\) where \(L_v\) is the latent heat released during the phase transformation. Using the data of Refs. 27 and 28 and a separation \(z = 50\) nm, which is comparable to the minimum separation in the force measurements with \(R = 10.1\) \(\mu\)m,\(^8\) we obtained respectively \(E_{A \rightarrow C} = 38\) pJ and \(E_{C \rightarrow A} = 337\) pJ. These energies are much larger than the work performed by the Casimir force over the closed path \(A \rightarrow C \rightarrow A\), \(\frac{1}{2} F_C(z) dz \sim 10^{-13}\) J, limiting the possibility to tap energy from vacuum fluctuations as the sole source to drive actuation.

For operation in air, an additional dissipative hydrodynamic force has to be taken into account.\(^29\) Here, we will consider motion in vacuum and ignore any dissipation via the support base of the actuating element [a high-quality factor system \(Q > 10^4\) (Ref. 30)]. Moreover, we consider actuators with resonance frequency \(\omega = 300\) kHz (typical for AFM cantilevers and other MEMS).\(^3\)

III. RESULTS AND DISCUSSION

In order to obtain the equilibrium points of motion from Eq. (2), we define the bifurcation parameter \(\lambda = F_C(A)(L_0)/KL_0\),\(^14,22,24\) which is the ratio of the minimal Casimir force (in the amorphous PCM) and the maximal elastic restoring force, representing the relative importance of one force competing to the other. The locus of equilibrium points “x” is obtained from Eq. (2) if we set \(F_T = -K(L_0 - z^*) + F_C(x) = 0,22,24,25\) The solution yields for the bifurcation parameter \(\lambda\),

\[
\lambda = (F_C(A)(L_0)/F_C(z^*)) (1 - z^*/L_0).
\]

(3)
FIG. 2. (Color online) (a) Bifurcation diagrams for the amorphous and crystalline phases of the AIST-Au system. For comparison, we show also the bifurcation diagram of the Au-Au system. For illustration purposes, we indicate two possible solutions if $\lambda < \lambda_{\text{max}}$ for AIST (A). (b) Phase portraits for AIST (A, C) and different (relatively weak) spring constants $K$. For all calculations we used $L_0 = 200$ nm, which is a typical surface separation for nanoscale actuation. (c) Phase portraits for AIST (C) states for different spring constants $K$ (N/m) as indicated, $R = 10.1 \mu$m, where the transition from stable (closed orbits) to unstable motion (open orbit) is shown.

The critical equilibrium points where stiction occurs are characterized also by the condition $dF_z/dz^* = 0$. The dependence of the parameter $\lambda$ on the locus of equilibrium points $z^*$ is shown in Fig. 2(a) for both PCM states, and in comparison to the Au-Au system that is widely used in Casimir force measurements. It is evident that the bifurcation parameter $\lambda$ is sensitive to phase transitions of the PCM from the amorphous to crystalline state.

The maximum of the bifurcation parameter $\lambda_{\text{max}}$ is approximately on the same location for both curves at $z_{\text{max}}^* \approx 0.75L_0$.

FIG. 3. (Color online) (a) Contour plots of the bifurcation parameter $\lambda$ (indicated by the color bar) for the crystalline phase. The radius and the spring constant are varied independently. (b) As in (a), for the amorphous phase. (c) Phase portraits for AIST (A, C) and two different sphere radii R that are used in Casimir force measurement systems. This is because the Casimir force shows an average power-law scaling $F_C(x) \sim x^{-p}$ with $p \approx 2.4 - 2.6$ (for $z < 200$ nm), and it is known that if a force-field scales as $\sim x^{-p}$ then the position of the maximum bifurcation parameter is given by $z_{\text{max}}^* \approx p/(1 + p)L_0$. Moreover, as Fig. 2(a) shows, if the spring constant is strong enough so that $\lambda < \lambda_{\text{max}}$, there will be two equilibriums: the stationary point closest to $L_0$ is a stable center around which periodic solutions exist. In Fig. 2(a), the locus of points for $z^* > z_{\text{max}}^*$ corresponds to stable actuation leading to closed orbits [see Figs. 2(b) and 3(c)]. However, if the spring constant is sufficiently weak so that $\lambda = \lambda_{\text{max}}$ then in this case there is only a single equilibrium, known as a center-saddle point, which is always unstable. For an even weaker spring constant $K$ so that $\lambda > \lambda_{\text{max}}$ the motion is unstable, which is an example of a saddle-node bifurcation.

The solutions of Eq. (2) can be further investigated with the so-called phase portraits, which are plots of the velocity $dz/dt$ of the actuating element versus the displacement $z$. In this case, we can have (i) a periodic orbit around an equilibrium point and (ii) unstable open orbit for a saddle point leading to pull-in instability or stiction [see Figs. 2(a) and 4(b)]. The existence of periodic solutions indicates that the spring is...
strong enough to counterbalance the attractive surface forces and prevent stiction. In this case, the stable center around which periodic solutions exist will be accompanied by an unstable saddle-point equilibrium. This is clearly manifested in Fig. 2(b) where closed orbits are shown for both amorphous and crystalline PCM, and soft spring constants $K \sim 10^{-3} - 10^{-4}$ N/m, which are used in ultrasonic systems. The difference between the amorphous and crystalline phases is amplified for the part of the orbit that comes in close proximity to the plate where the Casimir force is the strongest, thus enhancing the possibility for stiction to occur. This will happen if the spring constant weakens further (entering the regime of the saddle-node bifurcation) and stiction can no longer be avoided [see Fig. 2(c)]. For relatively large separations, $z/L_0 > 0.6$, the actuating component follows a stable movement, which changes to a rapid pull-in for $z < 0.6L_0$, having high sensitivity to small changes of the spring stiffness $K$.

Another parameter that can be varied independently of $K$ is the radius $R$ of the sphere. Figs. 3(a) and 3(b) are contour plots of the bifurcation parameter $\lambda \propto 1/K$ for the crystalline and amorphous phases, respectively. Since $F_C(z) \propto R$, the magnitude of the Casimir force can be modulated with the size of the sphere. It is clear that increasing the radius enhances the sensitivity to the phase transition, but the tradeoff is that this requires higher values of $K$ to prevent stiction. An example of solutions for a sufficiently large value of $K$ is shown in Fig. 3(c).

It should be noted that for a real system where the PCM undergoes a phase change from the amorphous to crystalline states a volume compression corresponding to $\sim 5$–8% of the PCM film thickness can occur, which translates to additional force changes with surface separation. As a result proper feedback is required to readjust the actuating components at the same separation as performed during the dynamic force measurements in Refs. 8 and 9. Moreover, explicit time dependence (e.g., forcing of the oscillations) would change the dynamics of the system considerably, because it would introduce an independent variable in phase space. The phase portraits and bifurcation diagrams presented in this manuscript would no longer be valid. Such a generalization would involve a different kind of mathematics, which is beyond the scope of this manuscript. However, qualitatively we can state that PCMs can be switched very fast $\sim 10^{-7} - 10^{-8}$ s, while typical actuation times for the phase maps shown here (see Figs. 2–4) are $\sim 10^{-6}$ s. Therefore it is possible to alter the system dynamics efficiently by phase change transformations.

Finally, up to now, we assumed absence of dissipation, or equivalently having a MEMS of high quality factor $Q > 10^4$ (dissipation $\sim 1/Q$). To investigate the effect of intrinsic dissipation, we considered in Eq. (2) the presence of a dissipative term of the form $(m\omega/Q)(dz/dt)$ with $K = m\omega^2$ (see Ref. 31) yielding $m(d^2z/dt^2) + (m\omega/Q)(dz/dt) = -K(L_0 - z) + F_C(z)$. Figure 4(a) shows that for $Q > 10^4$ the motion approaches that of a stable orbit, while as the $Q$ factor decreases [inset Fig. 4(a)] it attenuates drastically for the amorphous PCM state. However, it is intriguing to investigate what is happening if the spring constant is sufficiently weak (below a critical value $K_c$) to drive the system to stiction (S) under conditions of strong dissipation favoring attenuated motion (AM) towards stable equilibrium. This is shown in Fig. 4(b) where, as $Q$ decreases, the S $\leftrightarrow$ AM transition occurs rather sharply. For crystalline PCM, the $S$ $\leftrightarrow$ AM transition occurs for $Q_c \approx 480 \times 10^{-5}$ N/m, while for amorphous PCM at a lower $Q_c \approx 380$ [K(AM) $\approx 7.5 \times 10^{-5}$ N/M]. The critical $Q_c$ factor where the $S$ $\leftrightarrow$ AM transition occurs (at separation $z_{cr}$ just before the Casimir force becomes stronger than the elastic force) is given by

$$Q_c = \frac{(m\omega^2 L_0)}{|F_C(z_{cr})|} - K(L_0 - z_{cr}).$$

The latter yields for both PCM states $Q_{c(C)} = 498$ and $Q_{c(A)} = 392$, which compare well with the numerical results for $Q_{A,C}$ above.

IV. CONCLUSIONS

In conclusion, the reversible amorphous to crystalline phase transitions in PCMs can have strong influence on nanoscale actuation of MEMS under the influence of Casimir forces. Although we considered here flat surfaces, this is justified for actuation separations $> 100$ nm, since our former studies indicated morphology contributions only at lower separations.
The phase portraits that characterize the actuation dynamics show strong sensitivity to changes of the Casimir force as the stiffness of actuating component decreases, which can also lead to stiction. On the other hand, introduction of energy dissipation can prevent stiction by driving the system to attenuated motion towards equilibrium depending on the PCM state and system quality factor Q. Therefore the use of PCMs that allow modulation of their optical properties can provide new schemes of actuation, where introduction of dissipation can prevent stiction of soft components.

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