Scaling behavior of the magnetocapacitance of YbMnO₃

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Abstract
We observe a seemingly complex magnetic field dependence of the dielectric constant of hexagonal YbMnO₃ near the spin ordering temperature. After rescaling, the data taken at different temperatures and magnetic fields collapse on a single curve describing the sharp anomaly in nonlinear magnetoelectric response at the magnetic transition. We show that this anomaly is a result of the competition between two magnetic phases. The scaling and the shape of the anomaly are explained using the phenomenological Landau description of the competing phases in hexagonal manganites.

(Some figures in this article are in colour only in the electronic version)

1. Introduction
The recent interest in multiferroic materials was triggered by the discovery of the giant magnetocapacitance (MC) and magnetically-induced rotations of electric polarization in orthorhombic rare earth manganites [1–3]. This multiferroic behavior is rooted in magnetic frustration, which gives rise to non-centrosymmetric spin orderings that induce electric polarization [4]. Furthermore, the presence of competing spin states in these frustrated magnets results in a strong sensitivity of the magnetically-induced electric polarization to applied magnetic fields. In this respect multiferroics are similar to colossal magnetoresistance manganites and high-temperature superconductors [5].

In this paper we study the effects of critical magnetic fluctuations and the competition between different magnetic states on the nonlinear magnetoelectric response of the hexagonal YbMnO₃ by measuring the magnetic field and temperature dependence of its dielectric constant. Ferroelectricity in hexagonal manganites RMnO₃ (R = Ho–Lu, Y) appears well above the magnetic transition and is of nonmagnetic origin: an electric dipole moment along the c axis is spontaneously induced by tilts of manganese-oxygen bipyramids and buckling of rare earth-oxygen planes at $T_C > 600$ K [6–9], while the ordering of Mn spins occurs at a much lower temperature $T_N < 120$ K. However, the spin ordering in hexagonal manganites results in a surprisingly strong lattice relaxation, which affects the spontaneous electric polarization [10].

The Mn ions in hexagonal manganites form well-separated triangular layers parallel to the ab-plane with antiferromagnetic exchange interactions between nearest-neighbor spins [11], which makes the Mn spin subsystem low-dimensional and frustrated and results in enhanced spin fluctuations observed well above $T_N$ [12]. Frustration and rare earth magnetism are responsible for a rich variety of magnetic phases observed at low temperatures and in applied magnetic fields [13]. Due to magnetoelectric coupling each magnetic transition gives rise to a singularity of the dielectric constant [16, 14, 6, 15], which is more pronounced than the corresponding singularity in magnetic susceptibility.

We find that close to the Néel temperature $T_N = 81$ K the MC of YbMnO₃ measured as a function of magnetic field and temperature obeys a scaling behavior and has a very sharp anomaly. The detailed comparison with results of model calculations led us to a conclusion that the effect of magnetic fluctuations is completely overshadowed by the magnetic field dependence originating from the competition between two antiferromagnetic states, one of which is weakly...
ferromagnetic. Using a mean field Landau expansion of free energy in powers of two competing order parameters, we reproduce the shape of the anomaly as well as the changes in the behavior of MC observed in the wide range of magnetic fields and temperatures.

2. Experimental details

Polycrystalline samples of YbMnO$_3$ were prepared by solid state synthesis. A single crystal was grown from this powder by the floating zone technique. The magnetization $M(T)$ of the samples was measured up to 5 T. The capacitance of the samples was measured in a commercial system (PPMS4 Quantum Design) using a home-made insert and a Andeen-Hagerling 2500A capacitance bridge operating at a fixed measurement frequency of 1 kHz as well as using an Agilent 4284A LCR meter up to 1 MHz. Electrical contacts were made using Ag epoxy.

3. Results and discussion

The temperature dependence of the capacitance $C(T)$ proportional to the in-plane dielectric constant $\varepsilon_{||}$ is shown as an inset of figure 1(a). Below the Néel temperature $T_N = 82$ K, the capacitance is somewhat suppressed by the emergence of magnetic order [16]. The MC, $\frac{C(H) - C(0)}{C(0)}$, where $H$ is magnetic field along the $c$ axis, for a set of temperatures between 76.5 and 95 K, is shown in figure 1(a). In this small temperature interval around $T_N$ the behavior changes dramatically: at 76.5 K only a positive curvature is observed. With increasing temperature a high-field downturn appears, and at 80 K only a negative curvature can be observed, which changes back to positive above 90 K.

This unusual behavior is a consequence of the fact that by varying temperature and magnetic field we force the system to pass through a magnetic transition. The critical behavior becomes apparent when we plot $\frac{C(H) - C(0)}{C(0)H^2}$ versus temperature (see figure 1(b)). The procedure to evaluate $\Delta C$ at fixed magnetic fields versus temperature i.e. replotting the rescaled changes of the dielectric constant in magnetic field versus temperature, effectively reveals the magnetic field dependence of $C$. The strong temperature dependence of $C$ masks the magnetic field dependence when $C(T)$ is measured at fixed magnetic fields. The MC data evaluated at $H \leq 7$ T remarkably fall onto a single curve with a very sharp anomaly at $T_N$ where the temperature derivative of MC becomes large and positive while its magnitude shows an almost discontinuous jump from a positive to a negative value. The observed scaling behavior of MC can be understood in terms of the anomalous nonlinear magnetoelectric response, described by the term $\kappa(T)(E_0^2 + H_0^2)H_0^2$ in free energy, where $\kappa(T)$ has a singularity at the magnetic transition temperature. The scaling implies that the dependence of magnetic susceptibility for $H \parallel c$ on electric field $E \parallel a$ has the same anomaly at $T_N$.

The nonlinear magnetoelectric response of antiferromagnets usually originates from the fourth-order couplings, $\frac{2}{3} P^2 L^2$ and $\frac{4}{3} H^2 L^2$, of the electric polarization $P$ and the magnetic field $H$ to the magnetic order parameter $L$. The first term results in a correction to the bare dielectric susceptibility $\chi_0$, $\delta \chi = -g \chi_0^2 (L)^2 \propto (-\tau)^{2\beta}$ for $\tau = \frac{L}{T_T} < 0$, which accounts for the observed dielectric constant anomaly below $T_N$ (see the inset of figure 1(a)). The second coupling gives rise to the magnetic field dependence of Néel temperature, $T_N(H) \approx T_N(0) - \lambda H^2$, which makes $\delta \chi$ dependent on $H$. The resulting discontinuity of MC at $T_N$ and its anomalous behavior below $T_N$ are roughly consistent with our data. However, the most prominent feature of the observed anomaly—the long negative tail for $T > T_N$ (see figure 1(b))—cannot be explained in this way and is unusual.

This tail may result from magnetic fluctuations coupled to fluctuations of polarization, which become critical close to the Néel temperature. The lowest-order contribution of spin fluctuations to dielectric susceptibility (see figure 2(a)) is $\delta \chi^{(1)} = -g \chi_0^2 (\langle L^2 \rangle - \langle L \rangle^2) \propto \tau^{1-\alpha}$, where $\alpha$ is the exponent describing the critical behavior of magnetic specific heat [6, 17]. The corresponding singularity in MC (see figure 2(b)) is proportional to $g \lambda \text{sgn}(\tau) |\tau|^{1-\alpha}$. For $g, \lambda > 0$, this term is positive above $T_N$, in disagreement with our data. The fluctuational contributions to MC $\propto g^2 \lambda$ also do not explain the shape of the anomaly.

From this we conclude that the observed anomaly is unrelated to magnetic fluctuations and originates from a different physics. Below we show that the shape and scaling
behavior of MC can be explained within a mean field theory by the competition between the antiferromagnetic and weakly ferromagnetic state.

Hexagonal manganites show a number of magnetic phases with the 120°-angle between Mn spins in triangular $ab$ layers [18]. These phases differ by orientation of the spins with respect to the crystallographic axes and spins in neighboring layers, as well as by the ordering of rare earth spins [19–22]. The magnetic phase diagram of YbMnO$_3$ studied by a variety of different experimental techniques includes the low-field B$_2$ phase (magnetic space group $P6_3cm$) and the high-field A$_2$-phase (magnetic space group $P6_3cm$) [18, 23]. The symmetry of the latter state allows for a net magnetization in the $c$ direction (largely due to the rare earth spins and therefore small near the Mn spin ordering temperature), which is why the A$_2$ phase is stabilized by $H \parallel c$.

The competition between the A$_2$ and B$_2$ phases was discussed in [24] using the phenomenological free energy expansion in two order parameters:

$$f = \sum_{y=A,B} \left[ \frac{\alpha_y}{2}(T - T_y^{(0)}) + \lambda_y H^2 L_y + \frac{b_y}{4} L_y^4 \right] + \frac{d}{2} L_A^2 L_B - H \left( \phi L_A + \frac{\phi_y}{3} L_A^3 + \frac{\phi_y^2}{2} L_AL_B \right)$$

where $L_A(L_B)$ is the order parameter describing the A$_2$(B$_2$) phase, $H$ is the magnetic field along the $c$ axis, $T_A^{(0)}(T_B^{(0)})$ is the temperature of transition to the corresponding phase in zero magnetic field and in the absence of coupling between two magnetic orders (proportional to $d$), and $\lambda_A(\lambda_B)$ is the strength of the coupling of the antiferromagnetic orders to $H^2$, resulting in a field dependence of the Néel temperature. Furthermore, the spontaneous magnetization present in the A$_2$ phase allows for coupling to $H$ (the last three terms).

The typical phase diagram for $T_B^{(0)} > T_A^{(0)}$ (when the $B_2$ phase is energetically more favorable than the A$_2$ phase at zero field) is shown in figure 3. Due to the linear coupling between $H$ and $L_A$, the latter order parameter is nonzero for an arbitrarily weak magnetic field, so that for $H \neq 0$ the transition occurs between the $A_2$ phase and the $B_2$ phase with some admixture of the A$_2$ phase.

The MC for this model, shown in figure 4(c), is calculated by adding to the free energy equation (1) the terms describing the coupling of the magnetic order parameters to the in-plane electric polarization and the dielectric response of the nonmagnetic state,

$$f_{mc} = \frac{P^2}{2} \left( \sum_{y=A,B} g_y L_y^2 + g_A L_A H \right).$$

(2)

The last term resulting from the magnetization in the A$_2$ phase has the same shape as the one observed in YbMnO$_3$ and obeys the observed scaling. This behavior can be understood by noting that the main contribution to the magnetic field dependence of the dielectric susceptibility comes from $L_A$, which is linearly coupled to $H$. This field-induced order parameter grows as $T$ approaches the $T_N$ from above (see figure 4(a)), which gives rise to the ‘high-temperature’ negative MC tail, as $\Delta \chi_{fe} \propto -L_A^2$. In the weak-field regime $L_A \propto H$, so that $\chi(N) = \chi(T=0)$ is approximately field independent, which explains the observed scaling.

As the magnetic field increases, the character of the transition in the two-parameter model changes: in low fields the transition is of second order (red dashed line in figure 3), while in high fields and low temperatures it becomes a first-order transition (blue line) (see also figures 4(a) and (b)). The first- and second-order transition lines are separated by the

4 Another contribution to MC comes from an additional increase of $L_B$ below $T_N$ due to the suppression of $L_A$, which leads to the discontinuity and the sign change of MC at $T_N$. This contribution is also proportional to $H^2$. 

Figure 2. The lowest-order diagrams describing the contributions of magnetic fluctuations (wavy lines) to (a) dielectric susceptibility and (b) magnetocapacitance.

Figure 3. The magnetic phase diagram of the model equation (1) for $T_B^{(0)} > T_A^{(0)}$. The lilac region is the $B_2$ phase with admixture of the $A_2$ phase. The critical point (CP) separates the first-order transition (solid line) from the second-order transition (dashed line).
critical point. This change in the nature of the transition is also clearly seen in the experiments by comparing the field dependence of MC at low temperatures (see figure 5(a)) to that at high temperatures (see figure 1(a)). At 2 K the MC shows a distinct cusp at the first-order transition, which is well reproduced within our model (see figure 4(d)). In YbMnO₃ the changes in the order of the transition are made more dramatic by the fact that at low temperatures and high magnetic fields magnetic response is dominated by Yb spins, which below 3.8 K order ferrimagnetically [23]. This leads to a strong decrease of the critical magnetic field at low temperatures \( (H_c \sim 3 \, \text{T at 2 K}) \) and gives rise to the sharp discontinuity in magnetization, which is of first order in nature as demonstrated by specific heat measurements (see figure 5(b)) [25]. The slight upturn in the MC at 2 K, while approaching 0 T correlates with the step-like increase in the magnetization (see figure 5(b)) at similar fields and originates from the ferrimagnetic Yb spin ordering [22, 23, 25]. We also note that the field-induced magnetic transitions are observed at slightly different critical fields in magnetization and capacitance measurements. This can be explained by the fact that the two measurements were performed on crystals from different batches and, possibly, by a small misalignment of the crystals.

Finally, since the shape of the MC anomaly may be affected by the motion of antiferromagnetic domain walls separating different antiferromagnetic phases, we measured the frequency dependence of the dielectric constant. We found no frequency dependence in the interval from 1 kHz to 1 MHz, suggesting that the contribution of the domain walls in YbMnO₃ is negligible. Nevertheless, we cannot completely rule out effects originating from domain wall dynamics, as the coupling magnetic and ferroelectric domain walls may result in a high relaxation frequency.

**Figure 4.** (a) The temperature dependence of order parameters \( L_A \) (dashed blue line) and \( L_B \) (solid red line) near the second-order transition and (b) the magnetic field dependence of these order parameters near the first-order transition. Panel (c) shows the anomaly in rescaled magnetocapacitance at the second-order transition temperature. The magnetocapacitance anomaly at the first-order transition is shown in panel (d).

**Figure 5.** (a) MC of YbMnO₃ at \( T < T_N \) for \( E \parallel ab \)-plane and \( H \parallel c \); (b) field dependence of magnetization at 2 and 5 K.

**4. Conclusions**

To summarize, we observed a sharp anomaly in nonlinear magnetoelectric susceptibility of the hexagonal rare earth mangan-
ite YbMnO$_3$ at the Néel temperature. We discussed theoretically possible sources of the anomaly and showed that it results from the competition between two antiferromagnetically ordered states of YbMnO$_3$, one of which has a small spontaneous magnetic moment. Even though this weakly ferromagnetic phase becomes the ground state only in rather high magnetic fields or at very low temperatures, its admixture to the non-ferromagnetic phase determines the shape of the MC anomaly along the whole critical line of magnetic phase transitions. The competition between different magnetic phases, some of which may have a weak ferromagnetic moment is very common for frustrated magnets: similar phase diagrams were found for hexagonal HoMnO$_3$, which shows four competing states [18] and for Ni$_3$V$_2$O$_8$ [26]. Thus many other systems should show an anomaly in nonlinear magnetoelectric response, although its shape, which depends on parameters of the Landau free energy, may vary from material to material.

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