An agent-based dialogical model with fuzzy attitudes

Dykstra, Piter; Jager, Wander; Elsenbroich, Corinna; Verbrugge, Rineke; De Lavalette, Gerard Renardel

Published in:
Journal of Artificial Societies and Social Simulation

DOI:
10.18564/jasss.2813

IMPORTANT NOTE: You are advised to consult the publisher's version (publisher's PDF) if you wish to cite from it. Please check the document version below.

Document Version
Publisher's PDF, also known as Version of record

Publication date:
2015

Link to publication in University of Groningen/UMCG research database

Citation for published version (APA):

Copyright
Other than for strictly personal use, it is not permitted to download or to forward/distribute the text or part of it without the consent of the author(s) and/or copyright holder(s), unless the work is under an open content license (like Creative Commons).

Take-down policy
If you believe that this document breaches copyright please contact us providing details, and we will remove access to the work immediately and investigate your claim.

Downloaded from the University of Groningen/UMCG research database (Pure): http://www.rug.nl/research/portal. For technical reasons the number of authors shown on this cover page is limited to 10 maximum.
Abstract

This paper presents an extension to an agent-based model of opinion dynamics built on dialectic logic DIAL. The extended model tackles a pervasive problem in argumentation logics: the difference between linguistic and logical inconsistency. Using fuzzy logic, the linear ordering of opinions, used in DIAL, is replaced by a set of partial orderings leading to a new, nonstandard notion of consistency as convexity of sets of statements. DIAL allows the modelling of the interplay of social structures and individual beliefs, inspired by the interplay between the importance and the evidence of an opinion formulated in the Theory of Reasoned Action, but DIAL was restricted to argumentation about one proposition. FUZZYDIAL allows for a more natural structure of dialogues by allowing argumentation about positions in a multidimensional space.

Keywords:
Dialogues, MAS, Fuzzy Logic, Logic-Based

Introduction

1.1 Social systems involve the interaction between large numbers of people, and many of these interactions relate to the shaping and changing of opinions. The dynamics of these opinions elucidate other relevant phenomena such as social polarisation, extremism and pluralism. It is therefore important to develop models that capture interaction processes in a simple yet realistic manner.

1.2 Traditional opinion dynamics models take into account the social influence on opinion formation. Hegselmann & Krause (2002)'s Bounded Confidence Model explores the influence of a confidence interval $\epsilon$, i.e. an interval within which opinions are taken into account, on consensus and polarisation. Deffuant et al. (2002)'s Relative Agreement Model extends the Bounded Confidence Model by interpreting the confidence interval as an uncertainty factor of agent's regarding their opinion. Rather than a homogeneous $\epsilon$, agents are heterogeneous in their uncertainties.

1.3 These traditional opinion dynamics models have agents engage in opinion formation but do not also model social processes of group formation or segregation. An extension of the traditional opinion-dynamics framework is Jager & Ambillard (2005) which demonstrates that the attitude structure of agents determines the occurrence of assimilation and contrast effects, which in turn cause a group of agents to reach consensus, to bipolarise, or to develop a number of subgroups sharing the same position. In this model, agents engage in social processes. However, their framework does not have a logic for reasoning about the different agents and opinions.

1.4 Our modelling approach can be seen as a natural extension of these traditional opinion dynamics models. We follow Carley's social construction of knowledge (Carley 1986; Carley et al. 2003), according to which knowledge is determined by communication dependent on an agent's social group while the social group itself is determined by the agent's knowledge. Both DIAL (Dykstra et al. 2010) and FUZZYDIAL are models focusing on the feedback loop of group structuring and opinion formation using a simple argumentation game, reputation levels as payoffs from the game and movement in social space.

1.5 The paper is structured as follows. In Section 2 we discuss the relevant theoretical background to our extended model. In Section 3 we recap the important formal aspects of DIAL that will recur in FUZZYDIAL. In Section 4 we motivate the fuzzy extension by an example and describe FUZZYDIAL. In Section 5 the implemented model is presented. In Section 6 the actual experiments are outlined. We discuss the experimental results in Section 7 and in Section 8 we conclude and point to future work. This paper is a revised and extended version of Dykstra et al. (2010).

Theoretical Background

2.1 The theoretical background to our research is formed by theories combining beliefs and attitudes of individuals with the dynamic social environment an individual is situated in. DIAL (Dykstra et al. 2010; Dykstra et al. 2009; Dykstra et al. 2013) was strongly based on the Theory of Reasoned Action (Ajzen & Fishbein 1980; Ajzen 1991). The Theory of Reasoned Action defines an attitude as the sum of beliefs about the outcomes of a particular behaviour, weighted by the evaluations of these outcomes. Next to that, the subjective norm is defined as the perceived beliefs of important other people (normative beliefs) weighted by the motivation to comply to this norm. Whereas in this causal model there is a clear distinction between the individual attitude and social norm, it is also demonstrated that observing behaviour (descriptive norm) can lead to the development of an expectation of how other people would evaluate a certain behaviour (injunctive norm), and ultimately in personal beliefs (personal norm) (Cialdini et al. 1995). Hence in a causal model such as DIAL, social influences can have an impact on the attitude. Hence in DIAL an attitude is defined as a sum of opinions (beliefs), each having its own importance and level of evidence (weight), both importance and evidence being socially constructed.

2.2 DIAL essentially investigates the effects of different parameters on social outcomes such as group segregation and opinion rationalisation. Agent interactions are dialogue games in which agents gain reputation points on winning. Reputation can either be awarded for being in harmony with one's environment (normative redistribution) or by winning arguments (argumentative redistribution). It turns out that the distribution rule for reputation points is the most important factor influencing the simulation outcomes, with normative redistribution favouring segregated configurations and argumentative redistribution resulting in authoritarian societies in which some individuals hold almost all the reputation points.[3] These results are interesting and show how communicative intergroup dynamics influence opinion change as well as social structure.

2.3 However, DIAL has restrictions that are lifted in the fuzzy extension FUZZYDIAL:

1. In DIAL agents only argue about one opinion, in FUZZYDIAL they move in a multidimensional opinion space.
2. Agents have a linear ordering of the importance of other agents.
3. The concept of 'linguistic consistency' is introduced to define acceptable attitudes, that are sets of opinions that include all opinions which are intermediate between the most extreme opinions that the agents support.

2.4 These extensions go over and above the framework of the Theory of Reasoned Action. Two psychological theories are the main source for the formulation of FUZZYDIAL:

1. Social Judgement Theory (Sherif & Hovland 1961) describes the conditions under which a change of attitudes takes place, with the intention to predict the direction and extent of that change. The basic idea of Social Judgement Theory (Sherif & Hovland 1961) is that a change of a person's attitude depends on the position of the persuasive message that is being received. There exists a continuous ordering on statements. If the advocated position is close to the initial position of the receiver, it is assumed that this position falls within the receiver's latitude of acceptance. As a result, the receiver is likely to shift in the direction of the advocated position (assimilation).

2. If the advocated position is distant to the initial position of the receiver, it is assumed that this position falls within the latitude of rejection of the receiver. As a result, the receiver is likely to shift away from the advocated position (contrast). If the advocated position falls outside the border of the latitude of acceptance, but is not so distant that it crosses the border of the latitude of rejection, it will fall within the latitude of non-commitment; and the receiver will not shift its initial position.

2.5 If the advocated position is distant to the initial position of the receiver, it is assumed that this position falls within the latitude of rejection of the receiver. As a result, the receiver is likely to shift away from the advocated position (contrast). If the advocated position falls outside the border of the latitude of acceptance, but is not so distant that it crosses the border of the latitude of rejection, it will fall within the latitude of non-commitment; and the receiver will not shift its initial position.

2.6 Sherif & Hovland speculated that extreme stands, and thus wide latitudes of rejection, were a result of high level of ego-involvement. Ego-involvement is the importance of an issue to a person's life, often expressed by membership in a group. According to Sherif & Hovland (1961, p. 191), the level of ego-involvement depends upon whether the issue "arouses an intense attitude or, rather, whether the individual can regard the issue with some detachment as primarily a 'factual' matter". Religion, politics, and family are typical examples of issues that evoke a high level of ego-involvement.

2.7 Social identity theory is a social-psychological analysis of group processes, intergroup relations, and the self-concept (Tajfel & Turner 1979).

3. Norms are shared patterns of thought, feeling, and behaviour, and in groups, what people do and say communicates information about norms and is itself configured by norms and by normative concerns (Hogg & Reid 2006, p. 8).

2.8 Social identity theory focuses on prejudice, discrimination, and conditions that promote different types of intergroup behaviour – for example, conflict, cooperation, social change, and social stasis. An emphasis is placed on intergroup competition over status and prestige, and the motivational role of self-enhancement through positive social identity.

2.9 Social categorisation lies at the core of the social identity approach. It focuses on the basic social cognitive processes, primarily social categorisation, that cause people to identify with groups, construe themselves and others in group terms, and manifest group behaviours.
2.9 Individuals cognitively represent social categories as prototypes. These are fuzzy sets, not checklists, of attributes (e.g., attitudes and behaviours) that define one group and distinguish it from other groups. These category representations capture similarities among people within the same group and differences between groups. In other words, they accentuate intragroup similarities (assimilation) and intergroup differences (contrast) (Tajfel & Turner 1979).

2.10 Group representations are inextricable from intergroup comparisons – they are based on comparisons within and between groups. Specifically, we configure our intra-group representations so that they accentuate differences between a group and the relevant out-groups. For example, our representation of vegetarians will be different if we are comparing them to vegans or to carnivores. In this sense, group prototypes are context-dependent rather than fixed – they vary from context to context to function of the social comparative frame (situation, goals, and people physically or cognitively present).

2.11 In FUZZYDIAL, the concepts of latitude of acceptance and rejection are used to move the dialogue games from one to two dimensions and to implement linguistic rather than logical inconsistency.

2.12 This paper presents a descriptive study of the influence of normative agents on an artificial society. Agents can be considered as normative because they acquire their opinions in a prescriptive logic-based way: it is assumed that opinions are ordered in an extremism ordering which is either private to agents (which we call 'em categories) or shared by all agents ('standard categories). We will show how group norms emerge from private norms under both assumptions.

Quick DIAL

3.1 DIAL has been designed to help understand the social processes of opinion formation and group dynamics by multi-agent simulation, not by implementing group formation behaviour into individuals, but by providing agents with behavioural rules for communication and persuasion and the possibility of movement from an environment with which an agent is in discourse. In this section we briefly recap the formal details of DIAL that are also relevant for FUZZYDIAL.

3.2 Agents are located in a space where they form groups. They try to stay in tune with the opinions of their surrounding agents. Agents assume that the common opinion on a certain location is the accumulation of all utterances in that area that are not defeated in a debate. The real common opinion, however, is determined by the vote of the neighbourhood agents about atomic statements at the end of a debate. Agents want to gather status (operationalised as reputation points), which is possible by winning debates. They like to attach utterances of other agents about which they think that they can win a debate. They also like to make novel, previously unheard, utterances in order to align common opinion with their own.

3.3 The dialogue game is played as follows. An announcement consists of a statement $S$ and two numbers $p, r$ between 0 and 1. When an agent announces $(S, p, r)$, it says: I believe in $S$ and I want to argue about it: if I lose the debate I will pay $p$ reputation points, but if I win, I want to receive $r$ reputation points. See http://jasss.soc.surrey.ac.uk/16/3/4.html Par 3.16. Example 2, for a detailed example.

3.4 The values $p$ and $r$ are designed to be used in the dialogue game, and they are not very useful when we want to answer the question: "What will an agent learn from an announcement made by another agent?" To answer that question we introduce two more intrinsic concepts: the degree of belief (from evidence) an agent has in favour of a statement and the importance (of that statement). Evidence is the ratio between pro and con; an evidence value of 1 means "absolutely convinced of $S$". An evidence value of 0 means "absolutely convinced of the opposite of $S$". No clue at all is represented by 0.5. An importance value of 0 means unimportant and 1 means most important. Importance is expressed by the sum of both odds divided by 2.

\[ e = \frac{p}{p + r} \]

3.5 This means the more important an issue the higher the odds. The $(p, r)$-values can also be computed from an $(a, b)$-pair: $p = \frac{a}{a + b}$ and $r = \frac{b}{a + b}$. We call $a$ and $b$ the opinion values.

3.6 Agents learn from other agents by accepting a degree all utterances of other agents which are not attacked by some agents and by accepting all statements of the winner of a dialogue that are uttered as part of the dialogue. What do agents learn from utterances of other agents, once they accept those utterances? When an agent believing a statement with opinion values $(e_1, e_2)$. accepts an utterance of that same statement by another agent with opinion values $(e_1', e_2') \in [0, 1]^2$, it will acquire new opinion values defined by the functions $A_p: [0, 1]^2 \rightarrow [0, 1]$ and $A_r: [0, 1]^2 \rightarrow [0, 1]$.

\[ A_p(e_1, e_2) = 2e_1e_2 \]
\[ A_r(e_1, e_2) = 2e_1 - 2e_1e_2 - 1 \]
\[ = e_1 + e_2 - 0.5 \]
\[ \text{otherwise} \]

and:

\[ A_r(e_1, e_2) = 0.5(e_1 + e_2) \]
\[ + 0.125(2e_1 - 1)(2e_2 - 1)(e_1 + e_2) \]

See http://jasss.soc.surrey.ac.uk/16/3.html Appendix B for the technical details and justification of these formulas. http://jasss.soc.surrey.ac.uk/16/3.html Appendix C summarizes the exogenous and endogenous parameters of the simulation and offers a short explanation of their meaning. The next section is devoted to an extension of DIAL with fuzzy logic to enable dialogues about more than one statement.

FUZZYDIAL

4.1 In this section we discuss the fuzzy extension to the above dialogue game model. We first motivate the extension by discussing a communication scenario the kind of which FUZZYDIAL is supposed to model.

A Communication Example for FUZZYDIAL

4.2 As an example we consider the following situation:

Example 1 Four friends, Anna, Bob, Chris, and Daphne meet in a bar to celebrate the victory of their football club. When Bob confides to the others that he has lost a considerable amount of money on his Cypriot bank account, the talk changes to politics and the financial crisis. This is a subject they usually avoid, because all four have very different views on these issues, and they consider talking about such subjects as harmful to their friendship. Their preferred topics are the following:

- Anna is a socialist with a Keynesian view on economics. She is fully convinced that governments should invest to get out of the current crisis. The state should bail out companies because of the crisis. And the European Union should invest in national economies that suffer from the crisis.
- Bob has a monetarist view on macro-economics and believes that only a free market for goods and workers can free us from the crisis. The only goal for the European Union and the governments should be to keep the trust of the investors in the euro as high as possible. He values the EU as the protector of a large free market. National boundaries are bad.
- Chris and Daphne both have anti-European sentiments. Chris, who is a socialist like Anna, believes in the equality of all people and thinks that the richer countries should help the poorer ones, but his fear is that the current European Union is hijacked by a club of multinational companies and that the differences in the labour market are exploited to decrease the workers’ power by free exchange of workers.
- Daphne believes in the blessings of the free market economy. And in her opinion the European Union is turning the world into a village and she fears that other people will consider her national identity sentiments as ridiculous and irrelevant when globalisation progresses.

Daphne says that she feels sorry for Bob and she declares that she does not understand the anger of the Cypriots. They should be happy with the ten billion euros and not bite the hand that feeds them. But in the
4.10

We define:


utter their strongest convictions. On over the world. Thus keeping trust in the euro is worth a end Cyprus would have been better off if it were to conduct its own monetary policy. Thus ends the first round in the exchange of arguments. The loss of friendship was what they feared, but that did not happen. All persons have strongly opposing opinions, but they don’t utter their strongest convictions. On the one hand, they seek the support of one another for their opinion, on the other hand, they want to support one another. By uttering statements which are less extreme than what they really believe, their attitude has been interpreted by all as an attempt to stress what they have in common, and accentuates their friendship.

In another place at another time other players with the same set of opinions could start a debate to find reasons for hating each other. Uttering statements not only serves to inform other people, it also serves to establish a social network (make or break social ties).

4.3 In Figure 1 the named circles, A, B, C, and D represent the first utterances of the four people. Their position signifies their meaning in an ordering determined by two issues: pro versus anti the union of Europe, and Keynesian versus monetarist economics. The circles represent sets of states in which the uttered statements hold. Their colours symbolise their meanings, endorsing the idea that utterances can be made that are blends of more extreme opinions: blue-green for pro-European statements, red-yellow for anti-European statements; pink, orange and light-green circles labeled by E, F, and G respectively represent statements that are not uttered in the debate yet. They represent a neutral position in the pro-anti-European issue, but they differ in the economics issue. F is pro-Keynes and H is pro-Monetarist, while G is almost neutral in this issue. Their role will become clear in the in the examples of Subsection 4.2.

4.4 We want to model this type of exchange of arguments between agents in a dialogue game similar to DIAL. While DIAL only considers simulations in which agents argue about one statement, in this article, we introduce a simulation model with dialogues about more than one statement.

Conceptual Discussion of FUZZYDIAL

4.5 DIAL only implemented dialogues about one statement. We did not account for a relation between different statements S1 and S2, e.g. in the sense that S1 is more extreme than S2, on some extremeness scale. So in DIAL we cannot describe the change of a multidimensional opinion to a more (or less) extreme position.

4.6 In FUZZYDIAL we allow agents to have opinions about a set of statements. This is more in line with the theoretical notion that an attitude is composed of a set of beliefs (see e.g. Alpay 1991). For each belief a person can have an opinion that expresses to what extent the belief is accepted or rejected, and the importance and certainty of this belief (see e.g. Visscher et al. 2006). In FUZZYDIAL the agent’s attitude is formalised in terms of what statements it finds acceptable or not. Another interpretation of an attitude is that it represents a preferred statement, the statement with the highest e-value, of an agent joined with all semantically related statements that the agent consider as acceptable. Therefore sets of statements are referred to as the latitudes of acceptance (LOA), the latitude of rejection (LOR), and the latitude of non-commitment (LON). So (LOA, LDR, LON) is a partition of a set of statements.

4.7 In Fuzzy Logic, the membership of a fuzzy set S is described by a function \( \mu_S: X \rightarrow [0, 1] \), where X is the domain space or universe of discourse (see Figure 2). In FUZZYDIAL the universe of discourse is a possibly infinite set of statements S. Only atomic sentences and their negations, which are called literals, will be considered. A linguistic variable Y is a function which takes an element of a set of fuzzy predicates or linguistic modifiers as value, and produces a fuzzy set; for example, temperature is a linguistic variable for fuzzy predicates as cold, moderate, warm, etc. In our first example: the issues European Unionism and Monetarism are linguistic variables with pro, anti and moderate as their linguistic modifiers. For each agent a and each statement, we define the opinion function \( \mu_a \) similar to the membership function. We define the important concepts formally:

Definition 2 (Belief, importance and attitude) Let \( a \in \text{Agents} \). We have functions \( Bel_a, Imp_a: \text{Stats} \rightarrow [0, 1] \). We write \( \mu_a \) for \((Bel_a, Imp_a)\).

Definition 3 (Issue) An issue \( i \in I \) is an ordered set \( S_i \subseteq \text{Stats} \). We write \( \mu_{i,a} \) for \( \mu_a(S_i) \).

The minimal and maximal elements are the extreme statements. In our examples we will also attribute our statements with numerically valued issues in the interval [0, 1].

4.8 Normally, atomic statements are considered as unordered sets and in Social Judgement Theory there is a continuous ordering on statements. We assume a set of partial orderings on statements, one for each issue. A literal is an atomic statement or its negation. By \( s_1 < s_2 \) we mean that statement \( s_2 \) is closer to some positive extreme of issue \( i \) than \( s_1 \) is. In our experiments, we assume for the sake of simplicity, that the ordering on statements in an issue is either the same for all agents (standard categories) or all agents have their own ordering (own categories) (Sherif & Hovland 1961).

Definition 4 (Latitude of acceptance, latitude of rejection, latitude of non-commitment) Let \( S \subseteq S \leq s \leq s \leq S \).

We define:

- \( \text{LOA}_i = \{ b \in S_i | \mu_{i,b} > \mu_{i,0} \} \)
- \( \text{LOR}_i = \{ b \in S_i | \mu_{i,b} < \mu_{i,0} \} \)
- \( \text{LON}_i = \{ b \in S_i | \mu_{i,b} = \mu_{i,0} \} \)

4.9 A most preferred statement (MPS) is one of the statements with the highest e-values of the LOA (see Figure 2).

4.10 The LOA is determined by an interval of a certain size around a preferred statement. This interval is surrounded by the latitudes of non-commitment, which border on their other side to the area with the statements that are rejected (see Figure 2).

4.11 If an agent believes two statements with different positions on the scale of extremeness, it also has to believe all intermediate statements. This principle will be called linguistic consistency (LC). A logically consistent agent cannot believe a statement and its negation, but in order to be linguistically consistent, an agent a, who believes \( s_1 \) and \( s_2 \), also has to believe all the positions \( s_2 \) that are intermediate between \( s_1 \) and \( s_2 \). So when \( s_1 < s_2 < s_2 \) holds for any issue i also has to believe \( s_2 \).

4.12 To express this property, the acceptability function \( A \) on statements needs to be extended to a similar function on attitudes. Typical (fuzzy-) set operations such as union and intersection can be defined in terms of operations on their elements, e.g. union in terms of max:

\( (\mu_{A \cup B}(x)) = \text{max}(\mu_A(x), \mu_B(x)) \). In the same way we can extend our concepts for opinion acceptance to attitudes. Acceptance of the opinion \( \mu_{A \cup B}(x) \) of agent b by an agent a who has opinion \( \mu_a(x) \) on x can be defined as:

\( \mu_{a \cup b}(x) = \max(\mu_a(x), \mu_b(x)) \).
4.13 See http://jasss.soc.surrey.ac.uk/16/3/4.html Appendix B for the full definition of acceptance.

4.14 A notion similar to linguistic consistency in fuzzy logic is known as: convexity. A fuzzy set $\tilde{A}$ is convex if for all $x < y < z$ holds: $\tilde{A}(x) \geq \min(\tilde{A}(y), \tilde{A}(z))$ (Pedrycz & Gomide 1998).

4.15 We call $X \subseteq \mathbb{R}$ convex with respect to issue $i$ when we have:

$$\forall x, y \in X, \forall s \in [i < j \iff x \in X]$$

Definition 5 (Linguistic Consistency) An opinion function $\tilde{B}_i$ is linguistically consistent if the following holds:

$$\forall s, t \in S, i \leq j \iff \min(\tilde{B}_i(s), \tilde{B}_j(t)) \leq \tilde{B}_i(s)$$

or equivalently:

$$\tilde{B}_i(s) = \min(\tilde{B}_i(s), \tilde{B}_j(t)) \mid i \leq j, \sup(\tilde{B}_i(s) \mid x \leq d) \leq \sup(\tilde{B}_j(t) \mid x \leq d) \quad (*)$$

Proposition 6 If $\tilde{B}_i$ is convex w.r.t. issue $i$ then $LOA_i$ is convex.

Proof Let $x, y \in LOA_i$ and $x \subseteq S$ with $x < y$. We must show that $x \in LOA_i$. We have $x, y \in LOA_i$, so

(1) $\tilde{B}_i(x) > a_i$ and $\tilde{B}_i(y) > a_i$.

By $x < y$ and linguistic consistency of $\tilde{B}_i$, w.r.t. $i$, we have

(2) $\min(\tilde{B}_i(x), \tilde{B}_i(y)) \leq \tilde{B}_i(y)$.

Now by (1) and (2) we get $\tilde{B}_i(x) > a_i$. But this is equivalent with $x \in LOA_i$.

4.16 A problem is that the acceptance function as defined in http://jasss.soc.surrey.ac.uk/16/3/4.html Appendix B does not preserve convexity. It will not always be the case that an agent $A_i$ with an opinion function $\tilde{B}_i$, who believes statement $x_1$ with opinion values $(a_1, 1)$ and accepts the utterance of another agent $A_j$ on $x_2$ with opinion values $(a_2, 2)$, will end up with a new opinion function $\tilde{B}_i$, that is still linguistically consistent.

4.17 It however possible to make an opinion function linguistically consistent by increasing the opinion values of the statements that violate the linguistic consistency constraint sufficiently:

Definition 7 (Convexification) The convexification, $\tilde{B}_i^c$ of an opinion function $\tilde{B}_i$ is:

$$\tilde{B}_i^c(x) = \min(\sup(\tilde{B}_i(x) \mid y \leq d), \sup(\tilde{B}_i(x) \mid x \leq d))$$

From (*) it follows that: $\tilde{B}_i^c$ is convex, $\tilde{B}_i^c \leq \tilde{B}_i^c$, if $\tilde{B}_i$ is convex then $\tilde{B}_i^c + \tilde{B}_i$, from $\tilde{B}_i$ is convex and $\tilde{B}_i \leq \tilde{B}_i$, follows $\tilde{B}_i^c \leq \tilde{B}_i$.

4.18 In Table 1 a list is given with the standard fuzzy logic terminology and its counterparts in the FUZZYDIAL model.

<table>
<thead>
<tr>
<th>Fuzzy Logic</th>
<th>FUZZYDIAL</th>
</tr>
</thead>
<tbody>
<tr>
<td>element</td>
<td>statement</td>
</tr>
<tr>
<td>domain, universe, $X$</td>
<td>set of all statements: Stats</td>
</tr>
<tr>
<td>linguistic variable</td>
<td>issue, e.g., European unionist, monetarist</td>
</tr>
<tr>
<td>membership function $\mu$</td>
<td>belief functions: $\tilde{B}_i$, $\tilde{B}_j$</td>
</tr>
<tr>
<td>linguistic modifier</td>
<td>e.g.: pro, moderate, anti</td>
</tr>
<tr>
<td>fuzzy inference</td>
<td>opinion acceptance: $A_i$, $A_j$</td>
</tr>
<tr>
<td>fuzzy set</td>
<td>e.g.: attitude</td>
</tr>
<tr>
<td>fuzzy set operation, e.g.</td>
<td>union of attitude acceptances: $A_i$, $A_j$</td>
</tr>
<tr>
<td>convexity</td>
<td>linguistic consistency</td>
</tr>
</tbody>
</table>

Figure 2. The membership function of a fuzzy set.
4.19 The examples in Figure 3 show how the acceptance operator on opinion functions produces opinions as predicted in Social Judgement Theory and The Theory of Reasoned Action. According to Social Judgement Theory (Griffin 2011, p. 194), if an agent hears opinions that belong to its latitude of acceptance (LOA), a process of assimilation results in perceiving a message that is closer to the own opinion than it actually is. Accepting such misrepresented messages narrows the LOA.

4.20 Figure 3a shows that the acceptance of a similar opinion enlarges certainty. The resulting LOA is higher and narrower. Messages in the latitude of non-commitment (LON) have a higher probability of being accepted as desired by the sender, which results in a larger latitude of rejection (LOA).

4.21 In Figure 3b, the acceptance of two related opinions results in one with a greater tolerance with less certain opinions. Finally, Figure 3c shows that the acceptance of more unrelated messages, which fall in the LOR, results in one with less certainty and less tolerance. The effect is reinforced by a contrast-misrepresentation which causes the perception of the message to appear more different from the preferred statement than it really is.

4.22 In social epistemology, the group of agents which tend to reinforce an agent's opinion is called an 'echo chamber'. The agents which communicate with each other in FUZZYDIAL function as an echo chamber (Baumgaertner 2014). 'Echo chambers' reinforce the agents' opinions when they are echoed by other agents. Baumgaertner studies the factors which might dismantle echo chambers (Baumgaertner 2014).

![Graph 1](http://jasss.soc.surrey.ac.uk/18/3/3.html)

**Figure 3.** The result of the acceptance operator (the circled A) on two opinion functions $\Delta_b^0$ and $\Delta_b^1$. Horizontal axis: statements (a). Vertical axis: [0, 1]. The resulting attitude is in red. (a) Similar opinions enlarge certainty. (b) Two related opinions result in one with a greater tolerance. (c) Unrelated opinions result in one with less certainty and less tolerance.

![Graph 2](http://jasss.soc.surrey.ac.uk/18/3/3.html)

**Figure 4.** A 2-dimensional representation of two LOA's of Bob.

![Graph 3](http://jasss.soc.surrey.ac.uk/18/3/3.html)

**Figure 5.** The LOA's of Anna and Bob are different.

Example 8 In Figure 4, the graphs of the partial ordering of the two issues of Example 1 are represented: the Europeanism issue (left) with the vertical orientation and the Keynesian-Monetarist issue (right) horizontally oriented. The extreme statements in both issues are represented by the thick-lined circles, the statements A, B, C, and D, corresponding to the preferred statements of Anna, Bob, Chris, and Daphne, respectively. The ordering on both issues is not the same:

$$\text{Europeanism} = \{ (C, A), (C, B), (E, A), (C, F), (F, A), (F, B), (D, F), (D, G), (G, B) \}$$

and

$$\text{Keynesian-Monetarist} = \{ (C, B), (A, B), (C, F), (E, F), (F, D), (F, G), (F, B) \}.$$
The LOA of Anna is \( \{A, F\} \), which is not convex because it should contain statement E since A \( <_{\text{KeynesianMonetarist}} \) F and by definition 5, \( \text{LOA}(E) \) should be at least as high as \( \text{LOA}(A) \) and \( \text{LOA}(F) \), so E should be in \( \text{LOA}_{\text{KeynesianMonetarist}} \).

If all agents share the ordering on the Keynesian-Monetarist issue, as is displayed in Figure 4 and Figure 5 (standard categories), any agent who discovers that Anna does not believe E may attack her because of her linguistic inconsistency.

“Do all agents have the same ordering of statements?” If all agents have to be able to interpret the utterance of another agent to check whether that agent is approaching them or moving away from them in the opinion space, they need a shared or standard ordering of statements.

4.23 When a group of agents shares an ordering of statements, the next question in that case is: “How do agents acquire a shared extremeness ordering?” If it would be innate, there could not be any dynamics of opinion. If it is learned by communication, then it is unlikely that all will have the same extremeness ordering.

Example 10 Suppose that the displayed ordering in Figure 5 is only accepted by Bob and not by Anna, and suppose that LOA_{\text{KeynesianMonetarist}} is the same as LOA_{\text{Bob}}. LOA_{\text{KeynesianMonetarist}} but missing one of the edges (A, E) or (E, F). Now Anna is Linguistically consistent according to her own statement ordering, which is fine for her. But what about Bob? How will he know that Anna's statement ordering is not the same as his? Will he accept that other agents adopt a different statement ordering?

Example 11 Suppose that in Example 10, Bob believes that being monetarist is a position in the European scale close to the Monetarist extreme, and Bob believes that he shares his statement ordering with the other agents. Suppose furthermore that Bob knows about the European viewpoint on politics of Anna, but he knows nothing about her Keynesian standpoint. Now based on Bob's belief about the shared statement ordering and his assumption about the linguistic consistency of Anna, he might believe that Anna is monetarist. If all agents do have the same (standard) statement ordering, and Anna would utter her Keynesian opinions, Bob might rightfully accuse her of being inconsistent.

4.24 If all agents have their own ordering of statements, Bob will only be able to detect a linguistic inconsistency in another agent's utterances if he knows its private ordering. When agents have no information about one another's statement ordering, they cannot detect any linguistic inconsistency in the utterances of other agents.

4.25 An interesting refinement of this model is to allow agents to have beliefs about the statement orderings of other agents. Learning each other's statement orderings would be a necessity to acquire information about the attitude of other agents on the basis of announcements. And acquiring a common ordering by alignment would make agent communication simpler. This type of misunderstanding between agents who report incorrect and incomplete beliefs about one another's statement ordering is much harder to receive than getting an agreement about a particular statement. Robust networks of echo chambers (see Subsection 4.2) are considered hazardous for society as a whole (Sunsnien 2003; Bishop 2008) because they inhibit agents to come to a consensus in the context of society as a whole.

4.26 In this article we will not explore this refinement further. It would complicate our communication model seriously because of its higher-order epistemic consequences (What would agent say if he believes that other agents might not have a correct knowledge of agents 's statement ordering? How would agent come to believe that other agents have an incorrect view of its statement ordering? See Verbrugge (2009) for the exciting relation between cognition and epistemic logic.).

4.27 For our experiments we introduce two types of linguistic consistency:

1. Standard categories. There exists an extremeness ordering of statements which is the same for all agents. All agents know the statement ordering and are capable of detecting linguistic inconsistency and will repair their inconsistent attitudes.

2. Own categories. Each agent has its own extremeness ordering of statements on the set of statements. Agents do not know the statement ordering of other agents. And having a linguistically inconsistent attitude has no consequence in the social debate.

4.28 In both cases, agents will not utter statements that are linguistically inconsistent, because the acceptance function keeps their attitude linguistically consistent. Own categories' are more related to personal choices, which links them to the 'laid-back' in the Theory of Reasoned Action and in contrast standard categories' depend more on group opinions and group influence, which they have in common with the 'subjective norms' in the Theory of Reasoned Action (Ajzen & Fishbein, 1980).

Implementation of FUZZYDIAL

5.1 Making an announcement causes a chain of events. An announcement may change the opinion of other agents indirectly in a dialogue game where the direct effect is on the reputation of agents, but there is also a direct effect through learning and assimilation and contrast effects. The way these mechanisms are implemented in the NetLogo simulation program is described in the sequence diagram of Figure 14.

5.2 The reputation status of agents can be determined by two different mechanisms (Dykstra et al., 2013):

1. Force of Norms: The reputation status is determined by similarity with the environment. When an agent is more successful than others in establishing social contacts with similar-minded agents, it will increase its reputation status.

2. Force of Arguments: The reputation status is the account of the agent's argumentation score, because reputation points are the currency in which pays and rewards are balanced.

The relative influence of both mechanisms on reputation status is determined by two exogenous parameters: respectively force-of-norms and force-of-arguments. In Dykstra et al. (2013), experiments were performed with different combinations of both parameters. In the following section we consider just two cases: reputation status is either determined by force-of-norms or by force-of-arguments. Three categories of experimental parameters are used in our experiments (see Table 5).

<table>
<thead>
<tr>
<th>Table 5 Categories of experimental parameters</th>
</tr>
</thead>
<tbody>
<tr>
<td>Reputation</td>
</tr>
<tr>
<td>is the combined parameter which is low when reputation status is determined by high force-of-norms (and low force-of-arguments) and it is high in case reputation status is determined by high force-of-arguments.</td>
</tr>
<tr>
<td>MOAC</td>
</tr>
<tr>
<td>Assimilation and Contrast forces. These force parameter opinion changes: agents have to accept or reject the opinions of others. The parameter values are either zero and have no effect at all, or 0.4.</td>
</tr>
<tr>
<td>SOC</td>
</tr>
<tr>
<td>Standard versus Own categories. The standard categories option prohibits opinion changes that are linguistically inconsistent.</td>
</tr>
</tbody>
</table>

5.3 Announcements affect the opinions of the listeners directly. Utterances which agree/disagree sufficiently with the opinion of the listener (determined by the attraction and rejection parameters) are considered by the reader for acceptance or rejection, according to the mechanism of assimilation and contrast (MOAC) (Jager & Ambühl, 2009). MOAC is implemented by accepting those statements that belong to the latitude of acceptance (LOA) and rejecting statements (which means: accepting the negation) that are in the the latitude of rejection (LOR).

5.4 With own categories (OC), the ordering between the least and most preferred opinion is simply the evidence ordering. LOA is implemented as the set of statements with an evidence higher than 1 - tolerance, LOR has evidence between tolerance and 1 - tolerance.

5.5 When agents have standard categories (SC), all agents know and obey the same ordering between two (or more) extremes. The LOA is the part of the statements that have evidence above 1 - tolerance.

5.6 The details of the flow of consequences of agents' actions, as performed in the procedure act, is explained in Appendix D.

Simulation experiments

6.1 How do announcements affect opinions of other agents? And how do the just named experimental parameters support the propagation of moderate or extreme opinions? Do they affect tolerance or ego-involvement? What is their influence on social networks, and how does the social structure in its turn influence the opinion dynamics? These are the questions we try to answer with our experiments. In Subsection 6.1 we summarise the effects of force-of-norms and force-of-arguments. In Subsection 6.2 we extend the simulation by allowing more statements to the social debate, which forces a choice between two types of extremeness orderings (SOC). We study both own categories and standard categories. And finally in Subsection 6.3, we investigate how a combination of Reputation, SOC and MOAC contributes to the emergence of a latitude of acceptance.

6.2 In simulation runs we studied their effect on a number of parameters that give an impression of the type of opinion and social dynamics. A simulation run is a number of rounds of the simulation. At the start, agents are placed randomly in the world and they are assigned with random opinion- and reputation-values.

6.3 A run of our experiment can be interpreted as a period of social interaction about an issue. During a round every agent gets the opportunity to perform one of the following actions: announce, attack, reply, change their social network by walking to another place. The actual values of these exogenous parameters are given in Table 3.

Effects of Norms and Argumentation

6.4 In Dykstra et al. (2013) we studied the effect of norms and argumentation on opinion dynamics and the social structure. Cases concerning only one statement were studied. Typical results of a simulation in which reputation is determined by force-of-norms and force-of-arguments are shown in Appendix B.

6.5 Based on these simulations, we concluded in Dykstra et al. (2013) that argumentation prevents the emergence of extreme opinions and severe segregation. But do these results persist if we extend our simulation to the case where agents debate about more than one statement? We will answer this question in the next subsection.
6.6 The Figures 6 to 8 represent pictures of the distribution of opinions in the world the agents live in. For the meaning of the colors of the circles and the background, we refer to Appendix A.

Effects of Own and Standard Categories

6.7 Figures 6 and 7 show the maps of evidence of ten statements of two simulations after nearly 1700 rounds. The maps are a screenshots of the world window of the FUZZYDIAL simulation program in NetLogo. In each column the same agents occupy the same place, because both columns represent the same stage in a simulation, but they show the belief values for different statements (A to J). For a description of the meaning of the colours we refer to Appendix A. The world has no borders: the world wraps horizontally and vertically, so its shape is toroidal.

6.8 The left column shows the resulting maps of the simulation with own categories and the right column shows the resulting maps of the standard categories simulation. The reputation of an agent (size) is the same in every map, but their evidence values differ for the different statements. The reputation is only determined by force-of-arguments. So in essence this simulation only differs from the one of which results are shown in Figure 13 by the fact that the number of propositions is 10 instead of 1. Figure 8 shows the importance maps for half of the statements for both simulations. How the degrees of evidence (Figure 9) and importance (Figure 10) are distributed over the agent population is shown in bar charts. Each bar represents a subinterval of the interval [0, 1].

6.9 The most remarkable difference in the Figures 6 to 8 is that the distribution of reputation (size) is more egalitarian in the standard categories column compared to the own categories column. Furthermore the standard categories columns in these figures show a kind of evolving pattern when we compare the maps from statement A to J. In the own categories column the sequential statements appear unrelated. If the statement ordering is private, every agent has its own categories. This explains why no pattern can be found in the evidence and importance values of the agents for the different statements in the left column of the Figures 6 to 8. Neither is there a pattern in the evidence values of the patches.

6.10 The most important difference between both columns is however that the extreme statements in the standard categories simulation (statements A and J) also have the most extreme believers. This can be observed in all Figures 6 to 10. In the maps in Figure 6 and Figure 7 of statements A and J, the agents with the colours black and white (representing the evidence values 0 and 1) are more frequent than in the other maps. The agents also perceive a more extreme environment. The colours black and white are more represented in the background than the colour blue (with evidence values around 0.5).

6.11 The right columns of Figures 6 and 7 reveal an extra property. For each agent we can now actually see what its latitudes of acceptance, non-commitment and rejection are. When we pick an agent and count the number of successive maps where that agent is black, we measure its latitude of acceptance. And similarly, the number of successive maps where an agent is white determines its latitude of rejection. We can verify that all agents have a convex attitude. As a consequence, the majority of the patches has a convex attitude, although they are not punished for being inconsistent.

6.12 In the right column of Figure 8 the number of white agents is larger for the maps of the statements A and J and the background is darker, meaning that the agents do not want to talk about these statements despite the fact that they have the strongest opinions about it. The left column does expose any pattern.

6.13 The bar charts of Figure 9 and Figure 10 tell the same story: in the right column the peaks on the left and right side in Figure 9 for statement A and J denote the high number of agents with strong opinions, while for the statements between A and J the moderate opinions dominate. In the right column of Figure 10 the leftmost bar for A and J has a peak (high number of agents who find this statement not important to talk about) and for the statements between A and J the central bars take up most of the agents.

6.14 In the left column there is no difference between the bar charts of A and J and the bar charts of the in-between statements for both Figure 9 and Figure 10.

6.15 In the left column there is no radicalisation in the evidence values of the agents as in the simulation of Figures 6 to 8. The distribution of evidence is practically random. Importance values converge to 0.5 in all but the fourth statement, which is caused by the forgetting mechanism. This indicates that the dialogue is about other statements.

6.16 The inequality in reputation is lower in the right column, compared to the left in Figure 6 to Figure 10. This is not surprising since the agents are more strongly constrained to align to others compared to the own categories simulation. When agents talk about more than one statement, while they ‘stay on the same place’ in their social network, they have to align to another agent on some statements. This may lead to different coalitions for different statements. The consequence of this is twofold: on the one hand, it prevents the formation of firm and stable groups, on the other hand, it also prevents the emergence of a few opinion leaders who take all the reputation points.
Figure 7. The map of evidence of the statements F to I with high force-of-arguments.
Figure 8. The importance map of the statements A, C, E, H, J with high force-of-arguments.

<table>
<thead>
<tr>
<th></th>
<th>A</th>
<th></th>
<th>B</th>
<th></th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

Figure 9. The bar charts and the map of evidence of 5 statements with own categories and high force-of-arguments. For the standard categories A, C, E, H, J are ordered from A to J.

<table>
<thead>
<tr>
<th></th>
<th>A</th>
<th></th>
<th>B</th>
<th></th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

http://jasss.soc.surrey.ac.uk/18/3/3.html 21/10/2015
6.17 For the extreme statements A and J only one side has to be considered in the convexity test. That gives them more freedom to change. This can be noticed in the upper and bottom maps and bar charts in the standard categories column of Figure 6 to Figure 10. Agents do not need to talk about A and J anymore; they are certain about their opinion (pro or con).

6.18 This is unlike the other statements, where evidence is randomly distributed and importance converges to 0.5. Agents do want to talk about the moderate statements of which they have moderate importance values. This property makes the dialogue game an effective and goal-oriented communication device. By talking only about statements of which they are uncertain, agents learn to draw a line between what they believe and what they reject in a small number of actions.

6.19 The desire not to talk about their true opinions is also sometimes the case in real life. People may perceive the fact that other people do want to talk about those statements as something that weakens their opinion.

How Latitudes of Acceptance emerge

<table>
<thead>
<tr>
<th>Assimilation and contrast:</th>
<th>Without assimilation and contrast:</th>
</tr>
</thead>
<tbody>
<tr>
<td>Reputation Distribution</td>
<td>Reputation Distribution</td>
</tr>
<tr>
<td>Spatial Distribution</td>
<td>Spatial Distribution</td>
</tr>
<tr>
<td>LOA</td>
<td>LOA</td>
</tr>
<tr>
<td>Importance Distribution</td>
<td>Importance Distribution</td>
</tr>
<tr>
<td>PDF Average Belief</td>
<td>PDF Average Belief</td>
</tr>
<tr>
<td>Force of Norms</td>
<td>Force of Norms</td>
</tr>
<tr>
<td>Force of Arguments</td>
<td>Force of Arguments</td>
</tr>
</tbody>
</table>

6.20 We compare the simulations of different combinations of the Reputation, MOAC and SOC parameters (see Table 6). For simplicity reasons, for all parameters only two values are considered. In a simulation, reputation is determined either by force-of-norms or by force-of-arguments. The attraction and rejection forces are either low or high (0 or 0.47), and we never considered more than two options for the extremeness ordering. The timelines of the 8 possible states are shown in Figure 11. To express the degree of inequality in the distribution of properties, as reputation evidence and importance, we use the Gini-coefficient (Deaton, 1997). The endogenous parameters that are measured to characterise the social network and the types of opinion dynamics are:

2. Spatial Distribution. The clustering coefficient on the relation defined by the agents that are in each other’s visual horizon.
3. LOA. Latitude of Acceptance. The average size of the latitude of acceptance of all agents divided by the number of statements.
All experimental parameters have a similar effect on the endogenous parameters, if we order the dimensions conveniently (see Table 2). The ordering of the experimental parameters is:

<table>
<thead>
<tr>
<th>Parameter</th>
<th>MOAC</th>
<th>SOC</th>
<th>Reputation</th>
</tr>
</thead>
<tbody>
<tr>
<td>Reputation Distribution</td>
<td>-</td>
<td>0</td>
<td>-</td>
</tr>
<tr>
<td>Spatial Distribution</td>
<td>0</td>
<td>+</td>
<td>-</td>
</tr>
<tr>
<td>LOA</td>
<td>+</td>
<td>+</td>
<td>+</td>
</tr>
<tr>
<td>LON</td>
<td>-</td>
<td>-</td>
<td>-</td>
</tr>
<tr>
<td>Distribution of Pop</td>
<td>-</td>
<td>-</td>
<td>-</td>
</tr>
<tr>
<td>Opinion Distribution</td>
<td>+</td>
<td>+</td>
<td>+</td>
</tr>
<tr>
<td>Importance Distribution</td>
<td>-</td>
<td>0</td>
<td>0</td>
</tr>
</tbody>
</table>

When all parameters have a similar effect, this is because they influence a common cause. All three parameters contribute to faster changes of opinion as a result of changes in the agent's environment.

An idea of the magnitude of the correlations between the parameters is shown in Table 2. All experimental parameters are positively correlated to Spatial Distribution, LOA and Opinion Distribution (except for LOA and spatial distribution). With the other endogenous parameters the experimental parameters are negatively correlated (see two combinations).

For an explanation of the results, the LOA is the most important endogenous parameter. It expresses gain of certainty or the loss of uncertainty, gain in ego-involvement. The other endogenous parameters are strongly correlated with this parameter. LOA as a consequence of forces cancels extreme opinions, which speeds up the growth of the LOA.

There is a very strong negative correlation between LOA and LON. This is not very surprising, because LOA behaves very similarly to LOR, which is in fact the LOA of its negation. And since LON = LOA + LOR = 1, the correlation can only be strongly negative.

Of special interest in the timelines are the points in time when the LOA and LON lines cross (when the certainty about the agent's attitude becomes larger than its uncertainty). When all experimental parameters work in cooperation, the combined effect is much stronger and the point where LOA and LON equal is, reached earlier.

The mean evidence of the Preferred Opinion (Opinion Distribution) is correlated with the strength of the attraction and rejection forces. So the larger the LOA, the more agents prefer extreme opinions! We already saw in the one-statement case of Figure 12 and 13 (see Appendix A) that mean evidence is negatively correlated to importance distribution, similar to the negative correlation between Reputation and Spatial distribution.

Discussion

In Example 1 on Subsection 4.1, we suggested that agents could not understand the social implications of the utterances of other agents, if agents do not know the categories of other agents. The experiments show that this is not true, but that for growth of the limitation of acceptance. When agents are not constrained in changing their opinion, they acquire certainty about statements more quickly than when they have to be linguistically consistent, which is the case when agents share standard categories. Other categories thus help to gain certainty.

In Dijkstra et al. (2013) we already showed that for a single statement, high certainty and strong social ties (spatial distribution) is correlated with force-of-norms determined reputation. Our new experiment affirms this result also for sets of statements. Argumentation does not help to gain certainty. Simplicity of their environment (force-of-norms) is much more effective than winning debates (force-of-arguments).

Furthermore, own categories stimulate the formation of social clusters, despite the fact that mutual understanding is better under standard categories. Under own categories, agents are not inhibited by consistency constraints when they want to change their opinion. So they can adapt their attitude faster to a socially desirable attitude than agents with standard categories, who have to remain linguistically consistent. A remarkable consequece is that better understanding does not improve social coherence.

In Dijkstra et al. (2013), it has been shown that in the case of a single statement, clustering of agents leads to radicalisation of opinions. In this article, we conclude that a community of agents who share a statement ordering also enhances the emergence of agents with extreme opinions. In human society both aspects are closely connected. When people form a stable community, they do so because they share a statement ordering or otherwise they will be stimulated to develop such an ordering. This enhances their mutual understanding which, in turn, leads to happiness, because it enhances the group stability. But this coin has a downside too: the coming up of actors with nasty ideas is inherent to this situation. In Example 1: once Anna, Bob, Chris and Daphne all agree on one extreme statement, they will be happy about the reached consensus, but they are no more inhibited to develop even more extreme statements.

However in the Examples B-11 the multi-dimensionality of issues, which is common in real social debates, shows that it is very hard for agents to acquire sufficient information about the statement orderings of other agents. In the presence of multi-dimensional complicated social debates, the construction of standard categories and the establishment of stable communities will be harder. Luckily the upside of this coin is that the inability to really understand each other, also inhibits the radicalisation of opinions.

The choice of the definition of the experimental and endogenous variables is of great importance to the meaning(usefulness) of the simulation. Do the variables cover the "real" phenomena? One of the hardest phenomena to catch until now is the clustering of agents and the characterisation of the groups they form as "open" or "closed". The definition of clustering in social network analysis of Watts & Strogatz (1998) is simple and has a clear meaning. They define the degree of saturation of the social relations in a group as a measure of the degree of clustering. But such a measure does not cover properly what is going on in the model at the level of agent interactions because most of the change in social relations takes place in a very small part of the measuring scale (the (0.95, 1) interval) and an exponential transformation of the measure is of no help because the curve is too noisy.

Conclusion

We have extended our dialogical logic-based simulation model DIAL to deal with more than one statement. We introduced fuzzy logic to represent agent attitudes as the sets of statements that are believed by the agent, while the degree of belief is used as the fuzzy membership function. In the resulting model FUZZYDIAL, we introduced a set of partial orderings on statements, which serves as the domain of the linguistic variables for the corresponding fuzzy sets. The fuzzy set membership function also determines the preferred opinion and the tolerance level (latitude) on which agents decide on the truth of statements. To capture the notion of latitudes in Social Judgement Theory, we introduced the notion of linguistic consistency, which constrains the agents' reasoning. With this extension, changes of opinions can be expressed in accordance with Social Judgement Theory.

The experimental observations show that in our model, LON and LOA are not only determined by the mechanism of assimilation and contrast, but also by the lack of validity of standard categories and most of all the determination of reputation by normative forces. A small LON (and a large LOA) corresponds to high ego-involvement and is the result of strong attraction and rejection forces. So the social interaction in our model leads to a higher degree of ego-involvement. In that respect our dialogical model is in line with the Theory of Social Judgement. In addition to that, it predicts that the stronger the attraction and rejection forces are, the more extreme the preferred opinion is. This result is partly inhibited by the convexity constraint.

We set out to develop simulation models to understand opinion radicalisation in society. We have shown that the latitudes of acceptance of individual agents can be adjusted by the outcome of their interactions with other agents in dialogue games (downward causation). This architecture allows the social-opinion dynamics according to the Theory of Reasoned Action in simulations with reasoning and debating agents to emerge. Future work is the implementation of a fuzzy reasoning engine into the simulation framework. The importance to debate about a statement will also depend on the fact whether that statement is correlated with the statements that are accepted by almost all group members.

In the description of the results of our experiments, only the existence of correlations between parameters are named without the specification of the statistical details. The reason for this qualitative presentation is that we actually are interested in the causal relations between parameters, and the relation between the statistical information as given in correlation matrices and causality, is too complicated to be treated in this article. We will deal with this subject in a subsequent article by extending our simulation model with instruments that measure directly the forces that change endogenous parameters.
Notes

1 We recap some of the DIAL’s formal framework in Section 3.

2 A short description of the modal can be found in Dykstra et al. (2009) whilst the full description and analysis of DIAL can be found in Dykstra et al. (2013).

3 An ordering is connected if and only if its symmetric and transitive closure is the total relation.

4 In the Social Judgement theory literature ‘most preferred statement’ is usually called: ‘anchor position’ Griffin (2011); Sherif & Hovland (1951).

5 The term linguistic consistency is introduced to emphasise the fact that convexity is not the same as logical consistency, but in the dialogical context an agent who utters a linguistically inconsistent statement is treated the same as an agent who utters a logically inconsistent statement.

6 In a NetLogo simulation program, a 3-valued logic has been used to demonstrate the effect of impartiality (Baumgaertner 2014).

Appendix A: Social configurations resulting from different reputation functions

A.1 In both Figures 12 and 13 the bar charts on the left show the distribution of agents over the evidence- (upper chart) and importance-values (lower chart). The parameter values are divided into 20, respectively 10, intervals. In Figure 12 we see that by far the most agents belong to the most extreme evidence-value intervals of (0, 0.5) and (0.95, 1). The great majority of the agents belongs to the rank that has importance value in the (0, 1) interval. So in a society with strong norms, by far the most agents have extreme opinions and they do not want to talk about them.

A.2 The two maps of the agents world on right side will provide an explanation for this observation. The upper map shows the height of the accumulated evidence values (with the accepte function) of the utterances regarding a certain statement (current-prop) most recently made in the neighbourhood. The values range from 0 (black) via 0.5 (blue) to 1 (white). The circles represent agents; the diameter represents their reputation and their colour ranges from white (0) via yellow (0.5) to black (1). We see that the agents are clustered in a number of groups. In the centre is a group with high positive opinions. There are four smaller groups with strong negative opinions. But there is also a group with intermediate opinions (yellow agents). The clustering is the cause that agents hear mostly the same opinion as they have themselves, which makes them believe that they have the right opinion. Furthermore under high force-of-norms most agents have about the same reputation.

A.3 The lower map represents the accumulation of the importance values of the recent utterances in that neighbourhood. The colours range from black (0) via green (0.5) to white (1). And the agents’ colours range from white via red to black over the same interval of their importance values concerning the same statement.

A.4 This is in strong contrast to Figure 13, where large differences between the reputation values of the agents exist. On the one hand, force-of-arguments enlarges reputation distribution; on the other hand, it prevents the formation of groups (spatial distribution) and the emergence of extreme opinions (opinion distribution and importance distribution - see both bar charts). Explanation: large reputation make global announcements possible. So most of the agents hear different sounds from different directions, which prohibits the formation of niches for agents with extreme opinions, and – according to the bar chart for importance, which shows that almost all ranks except the lowest have more members than in the case of high force-of-norms – agents are inclined to talk about their opinions.

Appendix B: Exogenous parameters

B.1 The actual values of these exogenous parameters of all runs of the simulation program are as shown in the table below.

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Range</th>
<th>Value</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>force-of-arguments</td>
<td>0-1</td>
<td>0</td>
<td>Determines the degree in which the agent’s reputation is determined by winning and losing debates.</td>
</tr>
<tr>
<td>force-of-norms</td>
<td>0-1</td>
<td>0</td>
<td>The degree in which the reputation is determined by the similarity with its environment.</td>
</tr>
<tr>
<td>chance-announce</td>
<td>0-100</td>
<td>0.34</td>
<td>Utter an announcement.</td>
</tr>
<tr>
<td>Parameter</td>
<td>Range</td>
<td>Value</td>
<td>Description</td>
</tr>
<tr>
<td>--------------------</td>
<td>-------</td>
<td>-------</td>
<td>------------------------------------------------------------------------------</td>
</tr>
<tr>
<td>loudness</td>
<td>0-20</td>
<td>2.5</td>
<td>Determines the distance that a message can travel for anonymous communication. Anonymous communication affects the environment (patches) and indirectly its inhabitants through the learn-by-environment action.</td>
</tr>
<tr>
<td>chance-walk</td>
<td>0-100</td>
<td>16</td>
<td>Movement in the topic space.</td>
</tr>
<tr>
<td>stepsize</td>
<td>0-2</td>
<td>1.3</td>
<td>Maximum distance traveled during a walk.</td>
</tr>
<tr>
<td>visual-horizon</td>
<td>0-20</td>
<td>5</td>
<td>Determines the maximum distance to other agents who's messages can be heard (including the sender, which is necessary for attacking).</td>
</tr>
<tr>
<td>forgetspeed</td>
<td>0-0.005</td>
<td>0.00106</td>
<td>The speed the evidence- and importance-values of the agents’ opinion converges to neutral values (typically 0.5).</td>
</tr>
<tr>
<td>undirectedness</td>
<td>0-45</td>
<td>19</td>
<td>Randomness of the direction of movement.</td>
</tr>
<tr>
<td>chance-attack</td>
<td>0-100</td>
<td>12</td>
<td>Attack a recently heard announcement. (The most different one from the own opinion with the highest probability)</td>
</tr>
<tr>
<td>chance-learn-by-neighbor</td>
<td>0-10</td>
<td>0.2</td>
<td>Learn from the nearest neighbour.</td>
</tr>
<tr>
<td>chance-learn-by-environment</td>
<td>0-10</td>
<td>1</td>
<td>Learn from the average opinion on the agents’ location.</td>
</tr>
<tr>
<td>inconsistency</td>
<td>0-1</td>
<td>0</td>
<td>Penalty for having inconsistent opinions.</td>
</tr>
<tr>
<td>attraction</td>
<td>0-1</td>
<td>0.47</td>
<td>The largest distance in the evidence value of an uttered proposition and the evidence value of the same proposition of a receiving agent for which the receiver is inclined to adjust its opinion.</td>
</tr>
<tr>
<td>rejection</td>
<td>0-1</td>
<td>0.47</td>
<td>The shortest distance in the evidence value of an uttered proposition and the evidence value of the same proposition of a receiving agent for which the receiver is inclined to attack the uttered proposition.</td>
</tr>
</tbody>
</table>

Appendix C: The Actions of the Agents

C.1 The flow of consequences of agents’ actions, as performed in the procedure act, is shown in an UML sequence diagram in Figure 14. The numbers in the enumeration refer to the text labels on the right side of the sequence diagram.

![UML sequence diagram](http://jasss.soc.surrey.ac.uk/18/3/3.html)

Figure 14. UML sequence diagram of the influence of opinions. The vertical bars represent the time lines of the relevant objects. The horizontal lines represent the events of sending messages (Synchronous messages are followed by a dashed line with an arrow in the opposite direction, when the receiver returns the control back to the sender).

1. Agents utter their most important opinions most frequently. We consider the case that agent ag1, represented by the grey bar (which represents a thread – different threads are denoted by different colours) on the left, announces a statement. That event is communicated to other agents in the neighbourhood by the message update-announcement.

C.2 Whether a considered utterance will be accepted/rejected depends on its effect on the agent’s attitude. If its attitude remains linguistically consistent after acceptance, then the agent will accept the utterance (or its negation in case of a rejection). In case the agent’s attitude will become inconsistent, the agent will have to pay a penalty.

C.3 There is a possibility that an agent will learn from an utterance. In that case consistency of the resulting attitude determines what will happen with the agent’s opinions and reputation.

C.4 To form a latitude (interval), the statements have to be ordered in the degree of extremism and that order is fixed during the simulation, so the evidence assignment to the set of statements needs to be convex at the start. An initial convex set of opinions remains convex by forbidding the acceptance of statements that would result in a non-convex opinion state. Instead of adding acceptance events as in the ‘own categories’ model to enforce assimilation and contrast, we now decrease the number of acceptance occasions.

C.5 This functionality is implemented in the update-announcement procedure:
if \( \text{agreement} > 1 \) - attraction

then \( \text{setopinion announcement} \)

else if \( \text{agreement} < \text{rejection} \) - 1

then \( \text{setopinion negation of announcement} \)

C.6 The announcement is communicated to the patches in the environment (the World) by the message announce. This message applies the accept-function on the opinion values of the announcement and the patches.

2. Announcements start a sequence of attacks and defences in the dialogue game. The yellow thread represents another agent who launches an attack on the announcement \( \$ \) just heard. The attack itself is in red. The likelihood of this event is determined by the difference of the agent's opinion and the message. The reputation of the agent needs to be high enough to pay the reward in case the attacker loses the dialogue.

3. At the end of a round, the reputation of all agents is adjusted for their similarity with their environment. It will be increased when the similarity is high and otherwise reputation will be decreased. The degree depends on the value of force-of-norms.

4. After the adjustments of the reputation of the agents for similarity, agents, who have been attacked on a recently made utterance, get the opportunity to defend themselves. The verdict comes from the environment patches. If the opinion of the proponent is more similar to the environment than its negation, then the proponent wins: the reward is subtracted from the reputation of the opponent and added to the reputation of the proponent. Otherwise the opponent wins: the reputation of the proponent is subtracted by the pay and the same value is added to the opponent's reputation.

5. The last task in a round is the adjustment of the reputation of the winner and the loser. The winning statement is sent to the environment. And forgetting takes place.

C.7 The procedure Setopinion. When agents determine an extremeness ordering privately (own categories) they do not have to account for their choice. But when agents share a common extremeness ordering, they can only make opinion adjustments that are linguistically consistent. In the case they cannot change their opinion, they will suffer reputation damage.

C.8 The final consistency check is implemented in the procedure setopinion for the standard categories; for own categories this procedure does nothing and calls the accept new opinion code:

\[
\begin{align*}
\text{if } & \text{ newly acquired opinion results in a linguistically consistent attitude} \\
& \text{then accept new opinion} \\
& \text{else pay inconsistency penalty}
\end{align*}
\]

References


