Filament hunting: integrated H\textsc{i} 21 cm emission from filaments inferred by galaxy surveys

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ABSTRACT

Large-scale filaments, with lengths that can reach tens of Mpc, are the most prominent features in the cosmic web. These filaments have only been observed indirectly through the positions of galaxies in large galaxy surveys or through absorption features in the spectra of high-redshift sources. In this study, we propose to go one step further and directly detect intergalactic medium filaments through their emission in the H\textsc{i} 21 cm line. We make use of high-resolution cosmological simulations to estimate the intensity of this emission in low-redshift filaments and use it to make predictions for the direct detectability of specific filaments previously inferred from galaxy surveys, in particular the Sloan Digital Sky Survey. Given the expected signal of these filaments, our study shows that H\textsc{i} emission from large filaments can be observed by current and next-generation radio telescopes. We estimate that gas in filaments of length \(l \gtrsim 15\ h^{-1}\) Mpc with relatively small inclinations to the line of sight (\(\lesssim 10^\circ\)) can be observed in \(\sim 40–100\ h\) with telescopes such as Giant Metrewave Radio Telescope or Expanded Very Large Array, potentially providing large improvements over our knowledge of the astrophysical properties of these filaments. Due to their large field of view and sufficiently long integration times, upcoming H\textsc{i} surveys with the Aperif and Australian Square Kilometre Array Pathfinder instruments will be able to detect large filaments independently of their orientation and curvature. Furthermore, our estimates indicate that a more powerful future radio telescope like Square Kilometre Array can be used to map most of these filaments, which will allow them to be used as a strong cosmological probe.

Key words: intergalactic medium – cosmology: theory – diffuse radiation – large-scale structure of Universe.

1 INTRODUCTION

Observations of the local Universe have revealed that most galaxies reside in a complex network of filamentary structures known as the cosmic web (Bond, Kofman & Pogosyan 1996). Within the \(\Lambda\) cold dark matter framework, these structures are an expected result from non-linear gravitational evolution. According to this picture, the dark matter haloes within which galaxies reside are connected to each other through a patchwork of filaments and sheets that constitute the structure of the intergalactic medium (IGM; e.g. Cen & Ostriker 1999). Whereas galaxies reside in high-density regions, the diffuse gaseous component, if observed, gives an alternative view into filaments and their baryonic component. Furthermore, it potentially gives a more faithful tracer to the spatial distribution of the IGM than galaxies by themselves, which in turn allows for the study of the connection between galaxies and the filaments of gas.

Outside galaxies most baryons are expected to be in the relatively dense circumgalactic medium, which is mostly ionized and warm to hot. The remaining gas is in a filamentary structure with gas heated and ionized due to gravitational collapse and the UV and X-ray backgrounds. However, shielding from ionizing radiation due to recombinations in the denser pockets of gas still allows some of this gas to have a higher neutral fraction and emit potentially observable H\textsc{i} 21 cm radiation. Generally, the neutral fraction in these regions is well below a per cent of the total gas content (Popping & Braun 2011; Takeuchi, Zaroubi & Sugiyama 2014). None the less, its existence has been proved observationally through Lyman alpha forest absorption in the spectra of high-redshift quasars (Gunn & Peterson 1965). However, meaningful Lyman alpha absorption requires neutral gas above a given density threshold. Moreover, the technique is limited by the lines of sight to the available quasars and the matter content inferred from it depends on several assumptions about the gas conditions that are deduced from comparisons with simulations (e.g. Borde et al. 2014).

Thus far, large-scale filaments have mostly been detected through tracing the spatial distribution of galaxies in large galaxy surveys,

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such as the Sloan Digital Sky Survey (SDSS; York et al. 2000; Aihara et al. 2011), the 2-degree Field Galaxy Redshift Survey (Colless et al. 2001) and the Two Micron All-Sky Survey (Skrutskie et al. 2006). In such surveys, the larger structures of the cosmic web can be easily identified. Indeed, some effort has been made to catalogue filaments traced by SDSS galaxies, and many filaments with lengths ranging from a few to tens of $h^{-1}$ Mpc and diameters of $\sim 0.5-2$ $h^{-1}$ Mpc have been found (e.g. Sousbie et al. 2008; Jasche et al. 2010; Smith et al. 2012; Tempel et al. 2014).

In recent years, some effort has been devoted to tracing the large-scale structure of the cosmic web through the gas distribution. In a groundbreaking work, Chang et al. (2010) used H i 21 cm intensity maps obtained from the Green Bank Telescope (GBT), to constrain the large-scale structure at a redshift of $z \sim 0.8$ by cross-correlating with data from galaxy surveys. The same group followed this work up with a more significant detection using the WiggleZ galaxy survey data together with GBT 21 cm data (Masui et al. 2013). At higher redshifts, evidence for filamentary structures was found in the spectra of background sources due to scattering of Lyman alpha photons by the neutral IGM along the line of sight (e.g. Rollinde et al. 2003; D’Odorico et al. 2006; Cappetta et al. 2010; Finley et al. 2014). Recently, a cosmic web filament at $z \sim 2-3$ illuminated by a bright quasar was detected due to its Lyman alpha fluorescent emission (Cantalupo et al. 2014). At lower redshifts, however, the gas in the IGM is on average more ionized and the Lyman alpha line is observed in the UV, and so it is much more challenging to detect it in emission.

Takeuchi et al. (2014) explored the possibility of using the H i 21 cm line to directly observe IGM filaments. By estimating the integrated H i 21 cm line intensity from simulated filaments, they found that filaments with a length of $\sim 100$ Mpc can be detected in a 100 h of integration by reasonably sensitive telescopes, such as the Giant Metrewave Radio Telescope (GMRT) or the Five-hundred-meter Aperture Spherical Telescope (FAST). They also found that the signal from filaments aligned along the line of sight can be more easily detected. Obviously, detection of such a signal would allow for the study of both the baryonic content of the filament and the ionization state of the gas. This would in turn help constrain the UV background, since this radiation is the main agent responsible for the thermal ionization state of the gas.

Recently, Horii et al. (2017) performed a similar exercise, but then for the warm–hot intergalactic medium (WHIM). Their simulations include strong feedback, resulting in very high temperature filaments. This in turn leads to a large ionization fraction and an H i 21 cm signal that is more difficult to observe.

In this work, we go one step further by directly linking the properties of cosmic web filaments in our simulations to those that have previously been identified from observational galaxy catalogues. Specifically, we use the filament catalogue by Tempel et al. (2014), obtained from SDSS data, to find real filaments that are aligned along the line of sight and extract similar filaments from the simulation. With this identification, we then employ the simulations to calculate the neutral gas fraction in these specific filaments and predict their observability by current and future radio telescopes. To do this, we use a high-resolution cosmological N-body simulation and apply a semi-analytical prescription to the density field to estimate the temperature and ionization state of the IGM, from which we determine the H i 21 cm signal from these filaments.

The content of the paper is organized as follows. We begin by describing the model that is used to determine the thermal and ionization states of the IGM in Section 2. The method to calculate the 21 cm brightness temperature signal is shown in Section 3. The simulation details are presented in Section 4. We then describe how we selected the observed filaments and how we estimated their integrated H i 21 cm signal in Section 5. In the same section, we introduce the instruments that are considered for possible observations and compare their sensitivity to the signals of the filaments. We explore the advantages of survey instruments with large field of view (FoV) in more detail in Section 6, and finally the removal of contamination due to emission from galaxies in the H i 21 cm line is discussed in Section 7.

Throughout this work, we assume the Planck Collaboration XIII (2016) cosmological parameters ($\Omega_m = 0.3089$, $\Omega_{\Lambda} = 0.6911$, $\Omega_b h^2 = 0.0223$, $H_0 = 67.74$ km s$^{-1}$ Mpc$^{-1}$ and $Y_p = 0.249$).

2 MODEL: IONIZATION AND THERMAL STATE IN THE IGM

The conditions in the IGM drive the observed H i signal. This depends on the complex interplay between the different ionization, recombination, heating and cooling processes in the gas. The thermal and ionization state of the cold IGM is mainly set by the strength of the UV/X-ray background and can be estimated by assuming both thermal and ionization equilibrium. The equilibrium assumptions are a good approximation for most of the gas in filaments, given that the relevant time-scales for ionization and recombination are relatively short. However, they break down in very low density regions, where the gas cannot efficiently cool through recombination and collisional emission, and in the vicinity of galaxies or active galactic nuclei, where the ionizing radiation is much stronger and therefore the gas is highly ionized. Here we describe the full details of the model used to determine the ionization and thermal states of the IGM.

The ionization state of the IGM is governed by the balance between ionization and recombination processes. Even at low redshift, the gas in filaments far from local sources is expected to be very metal poor and so the cooling and heating processes in this medium are dominated by reactions involving only hydrogen and helium. The fractions of the different states of hydrogen and helium can be found by solving the following set of balance equations (Fukugita & Kawasaki 1994):

$$\frac{dx_{\text{H}i}}{dt} = \Gamma_{\text{H}i}x_{\text{H}i} + \beta_{\text{H}i}n_e x_{\text{H}i} - \alpha_{\text{H}i}n_e x_{\text{H}i},$$

$$\frac{dx_{\text{He}}}{dt} = \Gamma_{\text{He}}x_{\text{He}} + \beta_{\text{He}}n_e x_{\text{He}} - (\alpha_{\text{He}} + \xi_{\text{He}i}) n_e x_{\text{He}i} - \beta_{\text{He}i}n_e x_{\text{He}i} - \Gamma_{\text{He}i}x_{\text{He}i} + \alpha_{\text{He}i}n_e x_{\text{He}i},$$

$$\frac{dx_{\text{He}i}}{dt} = \Gamma_{\text{He}i}x_{\text{He}i} + \beta_{\text{He}i}n_e x_{\text{He}i} - \alpha_{\text{He}i}n_e x_{\text{He}i}.$$
Evolution of the ionization fractions for hydrogen (left) and helium (right). The width of the line denotes the density for which the calculation was performed.

From energy conservation of the IGM in an expanding universe, the gas temperature \( T_g \) follows

\[
\frac{dT_g}{dt} = -2H(z)T_g + \frac{2}{3} \left( \frac{H - \Lambda}{n k_B} \right),
\]

where \( H(z) \) denotes the Hubble parameter, \( H \) the heating rate, \( \Lambda \) the cooling function and \( n \) the baryon number density defined as \( n = n_{H_1} + n_{He_1} \). The first term on the right-hand side accounts for the adiabatic cooling due to the Hubble expansion of the Universe. For the heating function, we adopt the values corresponding to the Haardt & Madau (2012) ionizing background. Our cooling function includes collisional ionization/excitation, (dielectronic) recombination, free–free emission and Compton scattering of the cosmic microwave background (CMB) photons. A detailed description of the adopted cooling rates can be found in Appendix B.

As mentioned above, we solve these equations assuming ionization and thermal equilibrium, namely that the LHS of the equations is zero. Due to the dependence of equations (1), (2) and (3) on the gas temperature, they need to be solved together with equation (4), which we do iteratively. Our code solves for the ionization fractions and the gas temperature for a given hydrogen density and redshift. The redshift evolution of the ionization fractions of hydrogen and helium for different densities, relevant for filaments \((\Delta_b = 10 \text{ and } \Delta_b = 100)\), are shown in Fig. 1 and the evolution of the gas temperature in Fig. 2. The gas temperature will thus be \( \sim 1-3 \times 10^3 \) K for most of the gas in a filament. At redshift \( z = 3.5 \), our temperature–density distribution matches the median equilibrium solution in the hydrodynamical simulations with radiative transfer by Puchwein et al. (2015). These simulations also use the evolving Haardt & Madau (2012) UV background, and were shown to reproduce the IGM temperature as predicted by Lyman alpha forest observations. The computed neutral hydrogen fraction and gas temperature are stable for small variations of the ionizing background. For overdensities of 100 and higher, the H I fraction would be high enough to make a significant contribution to the cosmological mass density of neutral hydrogen \( \Omega_{HI} \) (e.g. fig. 12 in Crighton et al. 2015).

### 3 H I 21 cm BRIGHTNESS TEMPERATURE SIGNAL

Instead of directly measuring the intensity, radio telescopes measure the contrast between the brightness of the observed object and that of the CMB. This signal is expressed as the differential brightness temperature and is given by

\[
\delta T_0^X(z) = \frac{T_0^X(z) - T_r(z)}{1 + z} \cdot \left( 1 - e^{-\tau_z(z)} \right),
\]

where \( T_r \) is the CMB temperature and \( T_0^X \) and \( \tau_z \) are the spin temperature and the optical depth of species \( X \) (i.e. H I), respectively. So if the spin temperature is lower than that of the CMB, the signal will appear in absorption and if it is higher, it will be in emission. In general, the optical depth is given by (Furlanetto, Oh & Briggs 2006)

\[
\tau_z(z) = \frac{g_1 c^3 A_{10} h_0 v_{10} n_X(z)}{g_0 + g_1} \frac{1}{8 \pi v_{10}^2 k_B T_r} \frac{1 + z}{d \nu \ell / d \nu},
\]

where \( h_0 \) is the Planck constant, \( A_{10} \) is the transition probability, \( k_B \) is the Boltzmann constant, \( g_0 \) and \( g_1 \) are the statistical weights of the ground and excited states, \( v_{10} \) is the frequency at which the hyperfine transition occurs (for neutral hydrogen \( A_{10} = 2.867 \times 10^{-15} \) s\(^{-1}\)), \( g_1/g_0 = 3/1 \) and \( v_{10} = 1420.4 \) MHz, \( n_X(z) \) is the physical number density of species \( X \) and \( d \nu \ell/d \nu \) is the comoving radial velocity.
gradient along the line of sight. When including peculiar velocities, the latter is given by $\frac{dv}{dr} = 1/(1+z)[H(z) + \frac{dv}{dr}]$, where $\frac{dv}{dr}$ is the comoving gradient of the line-of-sight component of the comoving velocity. In the optically thin limit, the differential brightness temperature becomes

$$\delta T_b^X(z) = \frac{g_1}{g_0} \frac{c^3 h_p A_{10}}{8 \pi k_B v_0^2 (1+z)} H(z) \times \left(1 - \frac{T_j(z)}{T_e}\right) \left[1 + H(z)^{-1} \frac{dv}{dr}\right]^{-1}. \tag{7}$$

So the signal depends on the general properties of the line, the density of the medium and the cosmology, but it is then modified by the peculiar velocity term of order unity and by the spin temperature term. The latter becomes important when the spin temperature is close to the CMB temperature. In general, in studies of galaxies, the spin temperature is much higher than $T_e$ and is therefore safe to ignore. However, for the lower density IGM that is not always the case and so it needs to be properly estimated.

### 3.1 Spin temperature

The spin temperature $T_s$ determines the relative abundance of the exited state versus the ground state through the Boltzmann equation as

$$\frac{n_1}{n_0} = \exp \left( \frac{-h v_1}{k_B T_s} \right), \tag{8}$$

where $n_1$ and $n_0$ are the number of particles in the excited and ground state, respectively. The spin temperature is governed by absorption of CMB photons, collisions with hydrogen atoms, free electrons and protons and by scattering of UV photons (Wouthuysen–Field effect; Wouthuysen 1952; Field 1958), which couple the spin temperature to the CMB photons and to the gas (Furlanetto et al. 2006). Therefore, the spin temperature can be written as (Field 1958)

$$T_s^{-1} = \frac{T_e^{-1} + x_e T_e^{-1} + x_p T_p^{-1}}{1 + x_e + x_p}, \tag{9}$$

with $T_e$ the kinetic temperature of the gas and $T_p$ the colour temperature. The collisional de-excitation factor $x_e$ and the Wouthuysen–Field coupling factor $x_p$ are given by

$$x_e = \frac{C_{10}}{A_{10}} T_e, \quad x_p = \frac{P_{10}}{A_{10}} \frac{T_e}{T_p}. \tag{10}$$

where $A_{10}$ is the spontaneous decay rate from state 1 to state 0, which for neutral hydrogen has a value of $2.867 \times 10^{-53} \text{s}^{-1}$, $C_{10}$ is the collisional de-excitation rate and $P_{10}$ is the de-excitation rate due to absorption of a Lyman alpha photon. The equivalent temperature $T_e$ is defined as $T_e = h v_1 / k_B$. When calculating the spin temperature, we assume that the kinetic and colour temperatures follow the gas temperature: $T_e \sim T_k \sim T_s$. The collisional de-excitation rate for neutral hydrogen can be expressed as a sum over the collision processes with electrons, protons and other neutral hydrogen atoms,

$$C_{10}^{\text{HI}} = \kappa_{10}^{\text{HH}} (T_e n_H) + \kappa_{10}^{\text{HI}} (T_e) n_e + \kappa_{10}^{\text{IP}} (T_e) n_p. \tag{11}$$

Here $\kappa_{10}^{\text{HH}}, \kappa_{10}^{\text{HI}}$ and $\kappa_{10}^{\text{IP}}$ denote the collision rates for each process. Expressions for these can be found in Zygelman (2005), Sigurdson & Furlanetto (2006) and Furlanetto & Furlanetto (2007a,b).

The de-excitation rate for the Wouthuysen–Field effect equals

$$p_{10}^{\text{HI}} = \frac{16 \pi e^2 f_{\text{HI}}}{27 m_e c} J_{\text{Ly}, \text{HI}}, \tag{12}$$

where $e$ is the electron charge, $f_{\text{HI}}$ the oscillator length of the Lyman alpha transition ($f_{\text{HI}} = 0.4162$ for neutral hydrogen), $m_e$ the electron mass and $c$ the speed of light. For the Lyman alpha photon angle-averaged specific intensity $I_{\text{Ly}, \text{HI}}$, a model of the Lyman alpha emission that interacts locally with the IGM is required.

We assume three sources of Lyman alpha photons: collisional excitations, recombinations and high-energy background photons that redshift into the Lyman alpha line. The full details of our calculation can be found in Appendix C and the resulting evolution of the spin temperature is shown in Fig. 3, where we also show the evolution of the gas temperature and the CMB temperature. For the high densities, the spin temperature quickly couples to the kinetic temperature, but at low densities and low redshift the spin temperature approaches the CMB temperature, therefore suppressing the brightness temperature signal.

### 3.2 Test: slab model

To test the effect of the spin temperature correction term on the resulting signal of a filament, we assume a simple constant density slab model. The signal from such a slab is calculated through a small adjustment of equation (7), giving (Takeuchi et al. 2014)

$$\delta T_b^X(z) = \frac{g_1}{g_0} \frac{c^3 h_p A_{10}}{8 \pi k_B v_0^2 (1+z)} \left(1 - \frac{T_j(z)}{T_e}\right) \Delta r \Delta v, \tag{13}$$

with the width of the slab $\Delta r = 1 \text{ Mpc} h^{-1}$ and its proper line-of-sight velocity $\Delta v = 300 \text{ km} \text{s}^{-1}$. The resulting differential brightness temperature evolution of $H_1$ is given in Fig. 4. The red dashed lines show the signal in the saturated limit ($[1 - T_e/T_s] \sim 1$) and the blue solid lines show the corrected signal. As can be seen, the spin temperature correction becomes significant with a factor of a few for the lower density filaments at low redshifts and therefore needs to be included in these calculations.

### 4 COSMOLOGICAL SIMULATIONS

In order to predict the signal from more realistic filaments, we make use of high-resolution simulations that make it possible to resolve different filament morphologies and allow for differences in the gas properties along a filament.
Integrated H\textsc{i} 21 cm emission from filaments

Figure 4. Differential brightness temperature evolution for the slab model. The density is denoted by the width of the lines and the dashed lines show the signal in the saturated limit ([1 − T\textsc{i}/T\textsc{s}] ∼ 1).

We start by running the parallel Tree-Particle Mesh code GADGET2 (Springel 2005) with 1024\(^3\) particles and a volume of (200\,h\(^{-1}\)Mpc\(^3\)). This corresponds to a mass resolution of 6.514 × 10\(^8\)M\(_\odot\)\,h\(^{-1}\).

We then use cloud-in-cell interpolation to divide the simulation particles into a grid of \(N = 600\)\(^3\) cells, corresponding to a spatial resolution of \(\sim 0.33\,h\,Mpc\). This is enough to properly resolve the filament morphology. Then we determine the density contrast \(\delta = \rho/\langle \rho \rangle − 1\) for each cell of the simulation and, assuming that the spatial distribution of the baryons follows that of the dark matter, we compute the gas temperature, ionization state and differential brightness temperature following the prescriptions described in Sections 2 and 3.

Because we are interested in the emission of the IGM and not from galaxies, we mask the cells that are above the virialized limit determined through the scaling relations by Bryan & Norman (1998). For \(z = 0.1\), this critical overdensity is \(\Delta_c \approx 297\). Fig. 5 shows a slice of the simulation at \(z = 0.1\), with a thickness of 0.33\,h\(^{-1}\)Mpc, where several large filaments can be visually identified.

Additionally, we constructed a catalogue with the positions and masses of dark matter haloes using the Amiga halo finder (Gill, Knebe & Gibson 2004) on the initial particle catalogue. At low redshift, the most massive haloes are expected to have more than one galaxy. However, most of the luminosity of a halo usually originates in a single bright galaxy. This is also the only galaxy that a modest galaxy survey would probably detect, so it is reasonable to assume that each of these haloes would correspond to a single galaxy when comparing with SDSS detected galaxies.

5 21 CM EMISSION FROM SDSS FILAMENTS

In this section, we select gas filaments indirectly detected through the SDSS galaxies and estimate their integrated H\textsc{i} intensity. Given that SDSS surveys, such as the SDSS, do not probe the gas in filaments, we estimate the properties of the filamentary gas from similar length filaments found in our cosmological N-body simulations, which contain a similar number of galaxies. We start with a description of the catalogue and the criteria that were used to select the filaments and follow with the estimation of the H\textsc{i} 21 cm line intensity. The estimates are then used to determine the detectability of these filaments by current and future telescopes.

5.1 Filament catalogue

Since we are interested in targeting filaments inferred from galaxy catalogues, a complete sample of galaxies, covering a relatively large volume and down to a relatively low magnitude threshold, is required to identify large-scale filaments, the largest of which, currently available, was obtained by SDSS. The sample includes 499 340 galaxies and goes up to a redshift of \(z = 0.155\) with a lower limit of \(z = 0.009\). The lower magnitude limit \(m_r = 17.77\), imposed by the limits of the spectroscopic sample (Strauss et al. 2002).

We therefore use the filament catalogue by Tempel et al. (2014). This catalogue is obtained by statistically inferring the filamentary pattern in the SDSS Data Release 8 sample through the Bisous model. The model assumes a fixed maximum distance to which galaxies can be separated from the filament spine and still belong to it, which in this case was chosen to be 1\,h\(^{-1}\)Mpc. In Fig. 6,
we show the length distribution of the filaments from the catalogue. Most filaments are short (less than 10 h^{-1} Mpc) and would therefore result in a low signal-to-noise in most observations. However, a sample of ~4000 long filaments, reaching lengths of ~10 to ~50 h^{-1} Mpc, is also found. Within this sample of longer filaments, we choose the most suitable candidates to be targeted by observations, taking into account not only their lengths, but also their galaxy densities. It should be noted here that, given the spatial density of galaxies in the SDSS catalogue, the Tempel et al. (2014) method tends to fragment the filaments and assign smaller lengths to them than in reality.

The signal from a filament is highest when it can be observed directly along the line of sight, because then a larger part of the filament can be integrated over with a single pointing of the telescope. Therefore, we select the larger filaments with the smaller alignment angles (θ) with the line of sight. For simplicity, we define the inclination by assuming a straight line between the endpoints of the filaments. This method might exclude long filaments whose endpoints are not aligned along the line of sight, but that in between do have large parts that are aligned. However, we still find a number of useful filaments. In Table 1, we give the properties of the seven selected filaments.

Filaments 4, 5 and 6 are the most aligned along the line of sight. They have lengths of l ~ 15 h^{-1} Mpc, are all relatively straight spatially and are therefore ideal candidates for observations.

### Table 1. Properties of SDSS filaments with small alignment angles.

The parameter l is the length of the filament, θ is the alignment angle and Ngal is the number of galaxies associated with the filament.

<table>
<thead>
<tr>
<th>ID</th>
<th>z</th>
<th>d_center (h^{-1} Mpc)</th>
<th>l (h^{-1} Mpc)</th>
<th>θ (°)</th>
<th>Ngal</th>
</tr>
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<td>23.5</td>
<td>5.02</td>
<td>44</td>
</tr>
<tr>
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<td>5.70</td>
<td>32</td>
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<td>40</td>
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</tr>
<tr>
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<td>0.06</td>
<td>180</td>
<td>19.2</td>
<td>5.42</td>
<td>21</td>
</tr>
</tbody>
</table>

5.2 Signal estimation

Ideally, one would like to directly link current observables (galaxies) to the gas density in the filaments. Some work has been done to find a relation between the luminosity density of galaxies and the WHIM using simulations (Nevalainen et al. 2015). However, there are no similar relations between galaxy luminosity and the properties of the cold gas in filaments. Here we do a similar exercise in combining observations with simulations by looking for similar filaments to the ones found by SDSS. From the simulated box, we visually identify a number of long filaments that, after a careful selection, can be used to estimate the expected H\textsc{i} signal of the SDSS filaments. Although most of the selected filaments, in the Tempel et al. (2014) catalogue, have lengths of ~15 h^{-1} Mpc, the real gas filaments can be more extended, or the catalogue model can identify smaller parts of a larger filament as separate ones. Consequently, the observed signal can be higher than what would be expected by assuming the length inferred from the galaxy distribution. Therefore, in the simulations, we search for filaments that are longer (~50 h^{-1} Mpc, similar to the maximum length found in the filament catalogue) and, by comparing to the haloes in the simulation, determine what part of the filament would be detected by the SDSS.

Although our simulation box is at a redshift of z = 0.1, the relevant properties of the gas in the filaments are not expected to vary by much for the redshift range covered by the SDSS selected filaments.

Figure 7 shows the extracted filaments from the simulation box. They each have a length of ~50 h^{-1} Mpc and a radius of ~1 h^{-1} Mpc and are thus comparable to the filaments that can be detected by SDSS. We now analyse in more detail three filaments that cover the diversity of the selected filaments and the expected range in their intensities. Filament 2 is relatively straight along the line of sight, compared to the other two and is therefore the optimistic case. Filament 3, on the other hand, is relatively faint at the top and middle sections and therefore most of the signal arises from the bottom part of the filament as shown in Fig. 7. This is our pessimistic case. Filament 1 is somewhere in between the other two in terms of their expected signal strengths.

The signal of the simulated filaments is determined by taking a cylindrical skewer centred on the filament, which represents the

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**Figure 6.** Distribution of the length of the filaments found in the Tempel et al. (2014) catalogue.

**Figure 7.** The density fields of the selection of filaments from the simulation. The blue lines denote the observational skewer, whereas the magenta line shows what part would be preferentially detected by SDSS. The colour bar denotes the mean overdensity over the slices in the z-direction.
beam of the telescope and then the signal of the filament is calculated as follows:

\[ \delta T_b^{\text{fil}} = \frac{\sum_{i,j} \delta T_{i,j}^{\text{fil}}}{\Delta R - \pi r_b^2}, \]  

where \( \delta T_{i,j}^{\text{fil}} \) is the signal per cell within the skewer, \( \Delta R \) is the length of the skewer, which depends on the observed bandwidth, and \( r_b \) is the radius of the skewer, which is determined by the angular resolution. We set \( \Delta R = 50 \, h^{-1} \, \text{Mpc} \) (corresponding to a frequency bandwidth of \( \sim 15 \, \text{MHz} \)) and the radius to \( r_b = 1 \, h^{-1} \, \text{Mpc} \) (or an angular resolution of 10 arcmin). The blue lines in Fig. 7 indicate the observational skewer. By comparing to the simulated halo map previously obtained with the Amiga halo finder, we find that most of the massive haloes are located in the region between the magenta lines and a galaxy survey like SDSS would therefore most likely observe the regions between these lines.

### 5.3 Observability

In order to check the observability of these filaments, we compare the signal we obtain with the sensitivity of multiple instruments for the same conditions. In general, the noise in the measurement of a radio telescope can be written as (Furlanetto et al. 2006)

\[ \delta T_N \approx \frac{c^2 (1 + z)^2}{v_0^2 \Delta v^2 \epsilon_{\text{ap}} A_{\text{tot}} / \Delta v_{\text{obs}}} - \frac{T_{\text{sys}}}{\Delta v_{\text{obs}}}, \]  

where \( \epsilon_{\text{ap}} \) is the aperture efficiency, \( A_{\text{tot}} \) the total (illuminated) surface area of the array, \( \Delta v \) the frequency bandwidth and \( t_{\text{obs}} \) the observation time. The system temperature \( T_{\text{sys}} \) of a radio telescope has two components, one due to the sky that dominates at low frequencies and another due to the receiver, dominant at high frequencies. The brightness temperature uncertainty (sensitivity) \( \delta T_N \) is thus also a combination of the two contributions, where in the case of an interferometer the noise drops by the square root of the number of baselines \( (N_b = N_{\text{dish}}(N_{\text{dish}} - 1)/2) \), giving

\[ \delta T_N = \left( \delta T_{N,\text{sky}}^{\text{rec}} + \delta T_{N,\text{rec}}^{\text{rec}} \right) \times \begin{cases} 1 \quad & \text{single dish} \\ 1 & \sqrt{N_b} \quad & \text{interferometer} \end{cases}. \]

Ideal instruments would be those that have both a large FoV and good sensitivity in order to be able to probe the extended low-surface-brightness \( \text{H} \) emission. We consider both single-dish telescopes and interferometers. The single-dish telescopes are Arecibo and FAST. For interferometers, we consider Aperif on the Westerbork Synthesis Radio Telescope (WSRT), the Expanded Very Large Array (EVLA), GMRT, the Australian Square Kilometre Array Pathfinder (ASKAP), the Karoo Array Telescope (MeerKAT) and the second phase of the Square Kilometre Array (SKA-2). The relevant parameters for each of them are given in Table 2.

In Fig. 8, we show the brightness temperature uncertainties for each of the instruments as a function of the observation time. Each plot gives a comparison with the signal of one of the filaments, previously shown in Fig. 7, where the blue shaded region gives the signal of the full simulated filament and the white striped region denotes the signal from the filamentary region that we expect to be detected from SDSS data. The minima and maxima of these regions denote the minimum and maximum signal that arises when rotating the observational skewer from \(-5^\circ\) to \(+5^\circ\) with respect to the filament spine. This uncertainty accounts for a possible misalignment of the telescope beam and the filament spine, which we need to account for, given that this spine has to be defined without information on the gas content of the filament.

Depending on the morphology of the filament, the small rotation of \( \pm 5^\circ \) can change the signal of the filament by more than an order of magnitude. Since the regions corresponding to the SDSS filaments also contain the brightest parts of the filaments, the difference between the signal from either just that region or the full filaments is usually small. As can be clearly seen in Fig. 8, a number of instruments should be able to observe the \( \text{H} \) signal within \( \sim 100 \, h \). All of them can detect the upper limit of the signal of the three filaments; however, a misalignment of the beam could potentially render the signal too low and Aperif and Arecibo would have very low signal-to-noise. Instruments like EVLA, GMRT and MeerKAT are still promising for the signals of filaments 1 and 2. Only in the most pessimistic case of filament 3 is the signal too low for almost all of the instruments to detect it with good signal-to-noise within 100 \( h \). None the less, in all cases, SKA-2 should be able to easily observe the \( \text{H} \) signal with high signal-to-noise.

There is some uncertainty in the amount of heating that goes into the IGM. Since we do not include a prescription for shock heating in this medium, we might be underestimating the amount of heating and as a consequence also underestimate the ionization fractions. The amount of shock heating predicted by simulations differs a lot, depending on the assumptions on the feedback and on how it is implemented. According to the EAGLE simulation (Schaye et al. 2015), this is, however, not a crucial effect in the gas we target and so most of the gas in the EAGLE simulation follows the same temperature–density relation we use in our simulation (Crain et al. 2017). Nevertheless, we account for an extra source of heating by manually increasing the heating and photoionization rates of the Haardt & Madau (2012) background by a factor of 4. The resulting signal from the filaments reduces by a factor of \( \sim 5 \), as shown by the orange lines denoting the maximum signal under these conditions in Fig. 8. Even in this pessimistic case, the maximum signal from the filaments would be detectable by a large selection of the instruments. For strong filaments, such as filament 2, it would still be possible to get a good detection with all the instruments.

### Table 2. Telescope parameters. Arecibo and FAST are single-dish instruments, whereas the others are interferometers. The parameter \( D_{\text{dish}} \) is the dish diameter, \( N_{\text{dish}} \) denotes the number of dishes, \( A_{\text{tot}} \) is the total (illuminated) surface area, \( \epsilon_{\text{ap}} \) gives the aperture efficiency, \( T_{\text{sys}} \) is the system temperature for the observed frequency band, \( D_{\text{max}} \) is the maximum baseline length, \( \theta_{\text{res}} \) is the angular resolution and \( v_{\text{res}} \) is the minimum possible frequency resolution.

<table>
<thead>
<tr>
<th>Telescope</th>
<th>( D_{\text{dish}} ) (m)</th>
<th>( N_{\text{dish}} )</th>
<th>( A_{\text{tot}} ) (m²)</th>
<th>( \epsilon_{\text{ap}} )</th>
<th>( T_{\text{sys}} ) (K)</th>
<th>( \Delta v ) (GHz)</th>
<th>( D_{\text{max}} ) (km)</th>
<th>( \theta_{\text{res}} ) (arcmin)</th>
<th>( v_{\text{res}} ) (kHz)</th>
<th>FoV (deg²)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Arecibo</td>
<td>205</td>
<td>–</td>
<td>32 750</td>
<td>0.7</td>
<td>30</td>
<td>0.047–10</td>
<td>0.3</td>
<td>3.24</td>
<td>12.2</td>
<td>0.17</td>
</tr>
<tr>
<td>FAST</td>
<td>300</td>
<td>–</td>
<td>70 700</td>
<td>0.55</td>
<td>25</td>
<td>0.070–3</td>
<td>0.5</td>
<td>2.9</td>
<td>( \lesssim 0.5 )</td>
<td>0.36</td>
</tr>
<tr>
<td>Apertif (WSRT)</td>
<td>25</td>
<td>12</td>
<td>58090</td>
<td>0.75</td>
<td>55</td>
<td>1.13–1.75</td>
<td>2.7</td>
<td>0.36</td>
<td>12.2</td>
<td>8</td>
</tr>
<tr>
<td>EVLA</td>
<td>25</td>
<td>27</td>
<td>13 300</td>
<td>0.45</td>
<td>26</td>
<td>1–50</td>
<td>25</td>
<td>0.04</td>
<td>31</td>
<td>0.13</td>
</tr>
<tr>
<td>GMRT</td>
<td>45</td>
<td>30</td>
<td>47 720</td>
<td>0.4</td>
<td>75</td>
<td>0.05–1.5</td>
<td>25</td>
<td>0.04</td>
<td>31</td>
<td>0.13</td>
</tr>
<tr>
<td>ASKAP</td>
<td>12</td>
<td>36</td>
<td>4072</td>
<td>0.8</td>
<td>50</td>
<td>0.7–1.8</td>
<td>6</td>
<td>0.5</td>
<td>18</td>
<td>30</td>
</tr>
<tr>
<td>MeerKAT</td>
<td>13.5</td>
<td>64</td>
<td>9160</td>
<td>0.8</td>
<td>20</td>
<td>0.580–14.5</td>
<td>20</td>
<td>0.05</td>
<td>( \lesssim 18 )</td>
<td>1.44</td>
</tr>
<tr>
<td>SKA-2</td>
<td>15</td>
<td>1500</td>
<td>30 000 000</td>
<td>0.8</td>
<td>30</td>
<td>0.070–10</td>
<td>5 (core)</td>
<td>0.19</td>
<td>( \lesssim 18 )</td>
<td>1.17</td>
</tr>
</tbody>
</table>
Figure 8. The expected signal of the three filaments in this study (see Fig. 7) together with the noise temperatures for the different instruments being considered. The shaded blue area shows the signal for the full filament, where the top and bottom denote the minimum and maximum signal when rotating the observational skewer $-5^\circ$ to $+5^\circ$. The white striated shaded area shows the same, but for the case where the filament is only as long as expected from SDSS data. The coloured lines denote the noise level of the instruments described in Table 2 for $\Delta \theta = 10$ arcmin, $\Delta \nu = 15$ MHz. The orange solid line shows the maximum signal of the filament after increasing the heating and the photoionization by a factor of 4.

6 THE APERTIF AND ASKAP H I SURVEYS

In the previous sections, we studied the detectability of the H I gas in IGM filaments for the case where the filaments are aligned along the line of sight and so their signal can be integrated over a single pointing, even by instruments with a small FoV. However, some of the considered instruments (i.e. Apertif, ASKAP and SKA) have a very large FoV and so they can, with a single pointing, also detect filaments with different alignments or even curved filaments. Furthermore, Apertif and ASKAP have a number of planned deep H I surveys in the near future.

For Apertif, there will be a medium deep survey\(^1\) covering 450 deg\(^2\) with 84 h integration for each pointing. ASKAP will have the Deep Investigation of Neutral Gas Origins (DINGO) survey.\(^2\) DINGO will cover two fields on the Southern hemisphere, smaller but with longer integration times than the full ASKAP field: the DINGO-Ultradeep field of 60 deg\(^2\) with pointings of 2500 h and the less deep, but larger DINGO-Deep field of 150 deg\(^2\) and 500 h pointings. The areas covered by these surveys are larger than the ones in our simulation and so they are likely to contain filaments at least as bright in H I as the ones considered here.

In this section, we present the feasibility of detecting curved filaments by such surveys. We assume that the spatial location of the filament can be inferred through the positions of the bright galaxies previously observed by the same instrument or by other instruments. In this case, it is possible to follow the spine of the filament for the integration.

We extract a curved filament from our simulation, as can be seen in Fig. 9 and estimate its detectability. Filament 4 is similar in density and length as the previously discussed aligned filaments. In order to calculate a curved filament signal, we consider that each

\(^1\) http://www.astron.nl/radio-observatory/apertif-surveys

\(^2\) http://askap.org/dingo

Figure 9. The density field of the selected curved filament from the simulation. The magenta lines show the observational skewer over which the integration was performed with an angular resolution of 10 arcmin and a frequency bandwidth of 0.6 MHz, corresponding to a filament radius of $\sim 1$ $h^{-1}$ Mpc. The colour bar denotes the mean overdensity over the filament in the $z$-direction.
Integrated $\text{HI} \, 21 \text{ cm emission from filaments}$

7 CONTAMINATION FROM GALAXIES

Besides the IGM, another source of $\text{HI} \, 21 \text{ cm}$ emission in filaments is the galaxies. These are brighter than the IGM itself and will thus contaminate the integrated signal. Fortunately, the $\text{HI}$ signal from galaxies is largely dominated by a few bright galaxies, which can be directly observed by current instruments, such as Arecibo or WSRT, and certainly by SKA-2. Also, these galaxies are relatively small compared to the width of the filament, given that typical sizes of $\text{HI}$ discs are of the order of $\sim 30-60 \text{kpc}$ (e.g. Ruo & Briggs 1993). In the above sections, we have calculated the signals by masking all cells in our simulation box with a density above the critical density for collapse. This corresponds to 0.4 per cent, 0.6 per cent, 0.1 per cent and 0.4 per cent of the pixels in the skewer for the proposed pixel size of $(0.33 \text{h}^{-1} \text{Mpc})^3$ for filaments 1, 2, 3 and 4, respectively. We note that the resolution available from the proposed instruments is usually even higher. This means that, assuming that all dark matter haloes contain galaxies, the emission from all galaxies in the filament could be masked, without losing much of the IGM filamentary emission. In reality, it is only necessary to know the positions of the brightest galaxies and mask the corresponding pixels in the observation. This requires deep galaxy surveys and instruments that have high resolution, both spatially and in frequency. The instruments that were considered in Section 5.3 all have the necessary resolution to be able to mask the most luminous foreground galaxies, without erasing the target signal. In most cases, these surveys can also detect the position and the brightness of these galaxies. In the case of the filaments detected by SDSS, the positions of the galaxies are already known from the survey itself and they only need to be masked.

To check the level of contamination to the signal by galaxies, we make a conservative upper estimate of how much $\text{HI}$ would be contained by them and compare it to the $\text{HI}$ content of the IGM in the filaments in the simulation. The halo finder provides the masses of the dark matter haloes. We can convert these masses to $\text{HI}$ masses by using the fitting function to the $\text{HI}$ mass–halo mass relation determined through abundance matching by Padmanabhan & Kulkarni (2016):

$$M_{\text{HI}} = 1.978 \times 10^{-2} M_h \left( \frac{M_h}{4.58 \times 10^{11} M_\odot} \right)^{-0.90} + \left( \frac{M_h}{4.58 \times 10^{11} M_\odot} \right)^{0.74} \left( \frac{M_h}{4.0 \times 10^{13} M_\odot} \right)^{-1}.$$  

(17)

$M_h$ denotes the mass of the halo and $M_{\text{HI}}$ gives the mass of the $\text{HI}$ expected to be inside the halo. The total $\text{HI}$ masses in galaxies in the simulated filaments are $2.8 \times 10^{11}, 5.5 \times 10^{11}, 2.1 \times 10^{11}$ and $4.0 \times 10^{13} M_\odot$ for filaments 1, 2, 3 and 4, respectively. Their total $\text{HI}$ masses contained by the IGM are, respectively, $3.5 \times 10^{12}, 5.2 \times 10^{12}, 1.7 \times 10^{12}$ and $4.7 \times 10^{12} M_\odot$.

Galaxy surveys can only find the locations of the brightest galaxies. The flux limit of the survey constrains which fraction of the contaminating galaxies can be masked from observations. In order to get an estimate of the amount of $\text{HI}$ mass that could be inferred from SDSS data, we convert the flux limit of SDSS ($m_{\text{lim}} = 17.77$) to a minimum galaxy $\text{HI}$ mass ($M_{\text{HI}}^{\text{min}}$) in three steps. We connect the SDSS magnitude limit to the typical colour of galaxies using the colour–magnitude diagram of Jin et al. (2014). In this case, the highest limit (thus the least effective in removing the contamination by galaxies) comes from assuming a blue galaxy, giving a colour of $(u - r)_0 = 1.85$. Using this colour, we then find the appropriate mass-to-light ratio for these galaxies from Bell et al. (2003), corresponding to $\log(M_\star/L) \approx 0.33$, which, for the luminosity limit of SDSS, corresponds to a stellar mass of $M_{\star} \approx 9.62$. Finally, we convert the stellar mass into an $\text{HI}$ mass by applying the stellar mass-to-gas mass relation found by Rodríguez-Puebla et al. (2011), which...
results in a limiting H\textsc{i} mass for SDSS of $M_{\text{H\textsc{i}}}^{\text{lim}} \approx 2 \times 10^8 M_\odot$. By masking all the haloes in our simulated filaments with H\textsc{i} masses above this threshold, we then estimate the remaining contamination. Table 3 gives a summary of the results for each of the four filaments. As can be seen, the remaining contamination due to galaxies is two orders of magnitude smaller than the H\textsc{i} content in the IGM of the filaments. A survey like SDSS will thus be sufficient for dealing with the most severe contamination due to galaxies.

8 CONCLUSIONS

In this work, we explored the possibility of observing the integrated H\textsc{i} 21 cm line emission from large-scale filaments in the IGM. Directly mapping this emission is a potential new avenue to probe the spatial distribution of the filaments, and their gas content, ionization state and temperature. The properties of the filaments can be useful to construct more realistic models of galaxy formation and evolution, given the constant exchange of gas between galaxies and their surrounding medium, which is usually a large-scale IGM filament. Moreover, since the thermal and ionization state of the gas far from strong local sources is dominated by the UV background, these properties can be used to constrain this radiation field.

Our study mainly focused on filaments at $z = 0.1$, primarily because that is the average redshift at which good galaxy catalogues are available. The new generation of surveys will, however, also provide good galaxy catalogues at higher redshifts, and the proposed SKA-2 survey can be used to probe their emission. This would make it possible to constrain the evolution of the UV background even further.

In this study, we took observed filaments inferred from SDSS data and estimate their integrated H\textsc{i} 21 cm signal and its detectability by current and upcoming surveys. By selecting the largest filaments with the smallest inclination to the line of sight, we determined the intensity of the easier to observe filaments to be of the order of $10^{-6} - 10^{-5}$ K. We check the observability of these signals for an integration time of up to 100 h and found that a number of the radio surveys considered could detect some of these filaments in less than 50 h. In particular, GMRT and MeerKAT are good candidates to detect the signal. Furthermore, with SKA we would not only be able to detect a few filaments with a high signal-to-noise in just a few hours but we could also map many of the larger filaments in a relatively large area on the sky and/or smaller filaments. This would allow these filamentary structures to be used to constrain cosmological models of structure formation.

The upcoming H\textsc{i} surveys for instruments with large FoV, such as Apertif and ASKAP, could furthermore remove the need for observing spatially straight filaments aligned along the line of sight. We find that the integration times of the planned surveys for these two instruments will be sufficient to make the detection of the IGM gas in filaments feasible and opening up an interesting avenue to explore with these instruments.

Contamination to the signal from galaxies has to be taken into account, given that the bulk luminosity at the 21 cm line emanates from galaxies and not from the IGM gas we are targeting. We used the observational luminosities of the galaxies obtained by SDSS and compared them to simulated luminosities. This allowed us to safely conclude that this emission is dominated by a small number of sources, whose position can be determined by galaxy surveys and masked from observations before the signal is integrated. We note that these filaments inferred from SDSS data are biased towards the most luminous galaxies and should therefore have considerably more galaxy contamination than most IGM filaments. Our estimates also show that this masking procedure would bring the contamination down to a negligible level compared to the total signal of the filament, without erasing the target signal, even when attributing more H\textsc{i} mass to the remaining galaxies than what they are expected to have.

ACKNOWLEDGEMENTS

We would like to thank Marc Verheijen and Adi Nusser for interesting discussions on the subject presented here. We also thank the Netherlands Foundation for Scientific Research support through the VICI grant 639.043.00.

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Field G. B., 1958, Proc. IRE, 46, 240

Table 3. H\textsc{i} masses of the simulated filaments. $M_{\text{H\textsc{i}}}$ is the H\textsc{i} mass in the IGM of the filament, $M_{\text{H\textsc{i}}}$\textsuperscript{gal} gives the total H\textsc{i} mass contained by the haloes in the filaments and $M_{\text{H\textsc{i}}}$\textsuperscript{cut} gives the remaining H\textsc{i} contamination after removing the haloes with masses above the SDSS flux limit. All masses are given in $M_\odot$.

<table>
<thead>
<tr>
<th>Filament</th>
<th>$M_{\text{H\textsc{i}}}^{\text{IGM}}$</th>
<th>$M_{\text{H\textsc{i}}}$\textsuperscript{gal}</th>
<th>$M_{\text{H\textsc{i}}}$\textsuperscript{cut}</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>$3.5 \times 10^{12}$</td>
<td>$2.8 \times 10^{11}$</td>
<td>$4.5 \times 10^{10}$</td>
</tr>
<tr>
<td>2</td>
<td>$5.2 \times 10^{12}$</td>
<td>$5.5 \times 10^{11}$</td>
<td>$5.9 \times 10^{10}$</td>
</tr>
<tr>
<td>3</td>
<td>$1.7 \times 10^{12}$</td>
<td>$2.1 \times 10^{11}$</td>
<td>$4.3 \times 10^{10}$</td>
</tr>
<tr>
<td>4</td>
<td>$4.7 \times 10^{12}$</td>
<td>$4.0 \times 10^{11}$</td>
<td>$5.1 \times 10^{10}$</td>
</tr>
</tbody>
</table>
APPENDIX A: RECOMBINATION AND COLLISIONAL IONIZATION RATES

The ionization states of hydrogen and helium depend on the detailed balance between recombinations, ionizations and excitations. Below we list all the rates we adopted following Fukugita & Kawasaki (1994).

(i) Collisional ionization rates:

(a) H I → H II:

$$\beta_{HI} = 5.85 \times 10^{-11} T_1^{1/2} \left(1 + T_5^{1/2}\right)^{-1} \exp(-1.578/T_5) \, \text{cm}^3 \, \text{s}^{-1};$$  \hfill (A1)

(b) He I → He II:

$$\beta_{HeI} = 2.38 \times 10^{-11} T_1^{1/2} \left(1 + T_5^{1/2}\right)^{-1} \exp(-2.853/T_5) \, \text{cm}^3 \, \text{s}^{-1};$$  \hfill (A2)

(c) He II → He III:

$$\beta_{HeII} = 5.68 \times 10^{-12} T_1^{1/2} \left(1 + T_5^{1/2}\right)^{-1} \exp(-6.315/T_5) \, \text{cm}^3 \, \text{s}^{-1}.$$  \hfill (A3)

(ii) Recombination rates:

(a) H II → H I:

$$\alpha_{HI} = 3.96 \times 10^{-13} T_4^{-0.7} \left(1 + T_6^{-0.7}\right)^{-1} \, \text{cm}^3 \, \text{s}^{-1};$$  \hfill (A4)

(b) He II → He I:

$$\alpha_{HeII} = 1.50 \times 10^{-10} T_4^{-0.653} \, \text{cm}^3 \, \text{s}^{-1};$$  \hfill (A5)

(c) He III → He II:

$$\alpha_{HeIII} = 2.12 \times 10^{-12} T_4^{-0.7} \left(1 + 0.379 T_6^{-0.7}\right)^{-1} \, \text{cm}^3 \, \text{s}^{-1}.$$  \hfill (A6)

(iii) Dielectric recombination rate:

(a) He II → He I:

$$\xi_{HeII} = 6.0 \times 10^{-10} T_5^{-1.5} \exp(-4.7/T_5) \times \left[1 + 0.3 \exp(-0.94/T_5)\right] \, \text{cm}^3 \, \text{s}^{-1}.$$  \hfill (A7)

APPENDIX B: COOLING RATES

In this appendix, we list the cooling rates that were included in our model.

(i) Collisional ionization cooling:

(a) H I:

$$\zeta_{HI} = 1.27 \times 10^{-21} T_1^{1/2} \left(1 + T_5^{1/2}\right)^{-1} \exp(-1.58/T_5) \, \text{erg cm}^3 \, \text{s}^{-1};$$  \hfill (B1)

(b) He I:

$$\zeta_{HeI} = 9.38 \times 10^{-22} T_1^{1/2} \left(1 + T_5^{1/2}\right)^{-1} \exp(-2.85/T_5) \, \text{erg cm}^3 \, \text{s}^{-1};$$  \hfill (B2)

(c) He II (2^3S):

$$\zeta_{HeII,2S} = 5.01 \times 10^{-27} T_5^{-0.1687} \left(1 + T_5^{1/2}\right)^{-1} \exp(-5.53/T_5) n_e n_He/n_{HeI} \, \text{cm}^3 \, \text{s}^{-1};$$  \hfill (B3)

(d) He II:

$$\zeta_{HeII} = 4.95 \times 10^{-22} T_1^{1/2} \left(1 + T_5^{1/2}\right)^{-1} \exp(-6.31/T_5) \, \text{erg cm}^3 \, \text{s}^{-1}.$$  \hfill (B4)

(ii) Collisional excitation cooling:

(a) H I:

$$\psi_{HI} = 7.5 \times 10^{-19} \left(1 + T_5^{1/2}\right)^{-1} \exp(-1.18/T_5) \, \text{erg cm}^3 \, \text{s}^{-1};$$  \hfill (B5)

(b) He I:

$$\psi_{HeI} = 9.10 \times 10^{-27} T_5^{-0.1687} \left(1 + T_5^{1/2}\right)^{-1} \exp(-1.31/T_5) n_e n_He/n_{HeI} \, \text{erg cm}^3 \, \text{s}^{-1};$$  \hfill (B6)

(c) He II:

$$\psi_{HeII} = 5.54 \times 10^{-17} T_5^{-0.397} \left(1 + T_5^{1/2}\right)^{-1} \exp(-4.73/T_5) \, \text{cm}^3 \, \text{s}^{-1}.$$  \hfill (B7)

(iii) Recombination cooling:

(a) H II:

$$\eta_{HI} = 2.82 \times 10^{-26} T_5^{0.3} \left(1 + 3.54 T_5\right)^{-1} \, \text{erg cm}^3 \, \text{s}^{-1};$$  \hfill (B8)

(b) He II:

$$\eta_{HeII} = 1.55 \times 10^{-26} T_5^{0.3647} \, \text{erg cm}^3 \, \text{s}^{-1};$$  \hfill (B9)

(c) He III:

$$\eta_{HeIII} = 1.49 \times 10^{-25} T_5^{0.3} \left(1 + 0.855 T_5\right)^{-1} \, \text{erg cm}^3 \, \text{s}^{-1}.$$  \hfill (B10)

(iv) Dielectric recombination cooling:

(a) He II:

$$\omega_{HeII} = 1.24 \times 10^{-13} T_5^{-1.5} \left(1 + 0.3 \exp(-9.4/T_5)\right)^{-1} \exp(-4.7/T_5) \, \text{erg cm}^3 \, \text{s}^{-1}.$$  \hfill (B11)
APPENDIX C: LYMAN ALPHA

For the Wouthuysen–Field coupling, it is necessary to assume a model of the Lyman alpha emission. We take into account three sources of Lyman alpha: collisional excitations, recombinations and high-energy photons from the X-ray/UV background that redshift into the Lyman alpha line and then interact with the IGM. For the latter, we adopt the Haardt & Madau (2012) model.

The Lyman alpha photon angle-averaged specific intensity (in units of $s^{-1} \text{ cm}^{-2} \text{ Hz}^{-1} \text{ sr}^{-1}$) is calculated as follows:

$$J_{\text{Ly},\nu}(z) = \frac{N_{\text{Ly},\nu}(z) \mathcal{D}_{\lambda} \, \mathcal{D}_{\mathcal{L}}}{4 \pi \mathcal{D}_{\mathcal{L}}^2} \frac{dr}{d\nu} = \frac{N_{\text{Ly},\nu}(z) \lambda_{\text{Ly},\nu,0} \lambda_{\text{Ly},\nu}}{4 \pi \mathcal{H}(z)},$$

where $\mathcal{D}_{\lambda}$ and $\mathcal{D}_{\mathcal{L}}$ are the angular and luminosity distances, respectively, and $\lambda_{\text{Ly},\nu,0} = 1215.76 \text{ Å}$ is the rest wavelength of the Lyman alpha transition. $N_{\text{Ly},\nu}$ is the number of Ly$\alpha$ photons that interact with the IGM per unit volume per unit time. For recombinations, this number follows directly from the recombination rate

$$N_{\text{Ly},\nu,\text{rec}}(z) = f_{\text{Ly},\nu} \alpha_{\text{H}II}(T_{e}, z) n_{e} n_{\text{H}II} \text{ cm}^{-3} \text{ s}^{-1},$$

where $f_{\text{Ly}}$ is the fraction of recombinations that result in a Lyman alpha photon. This fraction depends on the temperature. We use the fitting function obtained by Cantalupo, Porciani & Lilly (2008)

$$f_{\text{Ly}} = 0.686 - 0.106 \log T_{e} - 0.009 T_{e}^{-0.44},$$

which is accurate within 0.1% at temperatures 100 K $< T < 10^{5}$ K. The recombination rate is given by

$$\alpha_{\text{H}II} = 3.96 \times 10^{-13} T_{e}^{-0.7} \left( 1 + T_{e}^{0.7} \right)^{-1} (1 + z) $$

Equations (C3) and (C4) are the rates for case B recombination. The case A recombination rate is higher, but the corresponding probability of emitting a Lyman alpha photon per recombination is lower, effectively negating the difference (Dijkstra 2014). Similarly, the density of Lyman alpha photons due to collisions that interact with the IGM follows from the collisional excitation coefficient $Q_{\text{col}}$ as

$$Q_{\text{Ly},\nu,\text{col}}(z) = Q_{\text{col}}(T_{e}, z) n_{e} n_{\text{H}II} \text{ cm}^{-3} \text{ s}^{-1}. $$

The comoving collisional excitation coefficient for transitions from the ground state to level $n$ is given by (Cantalupo et al. 2008)

$$q_{\text{H}I, n}^{\text{H}I} = 8.629 \times 10^{-6} T^{-0.5} \frac{\Omega_{\nu}(T)}{\omega_{\nu}} e^{\kappa_{\nu}/k_{B} T} (1 + z)^{3} \text{ cm}^{-3} \text{ s}^{-1},$$

where $E_{\nu}$ is the energy corresponding to the transition, $\omega_{\nu}$ is the statistical weight of the ground state and the function $\Omega_{\nu}$ is the effective collision strength, given by (Giovanardi & Palla 1989)

$$\Omega_{\nu}(T) = \begin{cases} 3.44 \times 10^{-4} & +1.293 \times 10^{-5} T^{-1} \\ +5.124 \times 10^{-12} T^{2} \\ +4.473 \times 10^{-17} T^{3}, & n = 1 \\ -5.462 \times 10^{-2} & -1.099 \times 10^{-6} T^{-1} \\ +2.457 \times 10^{-11} T^{2} \\ -1.528 \times 10^{-16} T^{3}, & n = 2 \\ 4.838 \times 10^{-2} & +8.56 \times 10^{-7} T^{-1} \\ -2.544 \times 10^{-12} T^{2} \\ +5.093 \times 10^{-18} T^{3}, & n = 3. \end{cases}$$

The total collisional excitation coefficient is then the sum over all the collisional excitation coefficients, where we only consider transitions up to $n = 3$

$$Q_{\text{H}I, n}^{\text{H}I} = \sum_{n=1}^{3} q_{\text{H}I, n}^{\text{H}I}. $$

Finally, for the background Lyman alpha emission, there are two main contributions. At high redshift, quasars are dominant, whereas at low redshift the main contribution of Lyman alpha photons comes from the galaxies. For the quasars, the comoving emissivity at 1 Ryd is (Haardt & Madau 2012)

$$\epsilon_{\text{Ly},\nu}(z) = \left( 10^{24.6} \text{ erg s}^{-1} \text{ Mpc}^{-3} \text{ Hz}^{-1} \right) \times (1 + z)^{4.68} \exp(-0.28 z) \frac{26.3 + \exp(1.77 z)}{\nu / \nu_{1500}},$$

which is a fit to the Hopkins, Richards & Hernquist (2007) results. This is then integrated over frequency to get the quasar Lyman alpha photon density

$$N_{\text{Ly},\nu,\text{qu}} = \int_{v(\text{Ly},\nu)}^{v(\text{max})} \epsilon_{\text{Ly},\nu}(z(v)) \frac{\nu}{\nu_{1500}}^{-1.57} \frac{dv}{h \nu},$$

where $v_{\text{Ly},\nu}$ is the redshift at which the emission couples to the local IGM as Lyman alpha, $v_{1500}$ is the frequency corresponding to 912 Å, $\nu(z) = v_{\text{Ly},\nu}((1+z)/(1+z_{\text{Ly},\nu}))$ and the exponent $-1.57$ comes from the quasar UV Spectral Energy Distribution for wavelengths below 1300 Å. The galactic contribution to the background Lyman alpha photons follows from a fit to the star formation rate density (SFRD) by Haardt & Madau (2012)

$$\text{SFRD}(z) = \frac{6.9 \times 10^{-3} + 0.14 (z/2.2)^{-5}}{1 + (z/2.7)^{5}} \times \frac{M_{\odot} \text{ yr}^{-1} \text{ Mpc}^{-3}}{1500 \text{ Å}},$$

To convert the observed luminosity densities $\rho_{1500 \text{ Å}}$ to ongoing SFRDs, Haardt & Madau (2012) adopted a conversion factor $\kappa = 1.05 \times 10^{-28}$

$$\text{SFRD}(t) = \kappa \times \rho_{1500 \text{ Å}}(t),$$

where $\rho_{1500 \text{ Å}}$ is in units of erg s$^{-1}$ Mpc$^{-3}$ Hz$^{-1}$. We adopt the same conversion factor to go from the fitted SFRD back to a luminosity density. The galactic Lyman alpha photon density is then the integral over the SFRD

$$N_{\text{Ly},\nu,\text{gal}} = \int_{v(\text{Ly},\nu)}^{v(\text{max})} \frac{\text{SFRD}(z(v)) / \kappa}{B_{\nu}(T_{\text{gal}})} \frac{B_{1500}(T_{\text{gal}})}{h \nu} \frac{dv}{h \nu},$$

where $B_{\nu}$ is the Planck function at frequency $\nu$ and $B_{1500}$ is the same at 1500 Å. The Planck functions depend on the temperature of the IGM in the galaxies, for which we adopt $T_{\text{gal}} = 6000$ K.
One more effect that needs to be taken into account is that photons can scatter multiple times before they redshift out of the Lyman alpha line. Each additional scattering adds to the Wouthuysen–Field coupling and so the Wouthuysen–Field coupling factor needs to be multiplied by the number of scatterings (Field 1959). This is given by the Gunn–Peterson optical depth (Gunn & Peterson 1965)

\[
\tau_{\text{GP}} = \frac{n_x \lambda_{\text{Ly} \alpha} f_\alpha \pi e^2}{H(z) \ m_e c}, \tag{C14}
\]

with \( n_x \) either the \( \text{HI} \) or \( \text{HeII} \) density. Because Lyman alpha photons created through recombinations originate close to the line centre, their Lyman alpha specific intensity gets an additional factor of 1.5 (Field 1959).

The evolution of the Lyman alpha intensity is shown in Fig. C1. At low redshift, for the higher densities, recombination and collisions are the dominant source of Lyman alpha, whereas for the lower densities it is the background emission.

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**Figure C1.** Lyman alpha photon angle-averaged specific intensity for hydrogen for the different mechanisms. The linewidth denotes the density.