Models of Social Influence: Towards the Next Frontiers

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Abstract: In 1997, Robert Axelrod wondered in a highly influential paper “If people tend to become more alike in their beliefs, attitudes, and behavior when they interact, why do not all such differences eventually disappear?” Axelrod’s question highlighted an ongoing quest for formal theoretical answers joined by researchers from a wide range of disciplines. Numerous models have been developed to understand why and under what conditions diversity in beliefs, attitudes and behavior can co-exist with the fact that very often in interactions, social influence reduces differences between people. Reviewing three prominent approaches, we discuss the theoretical ingredients that researchers added to classic models of social influence as well as their implications. Then, we propose two main frontiers for future research. First, there is urgent need for more theoretical work comparing, relating and integrating alternative models. Second, the field suffers from a strong imbalance between a proliferation of theoretical studies and a dearth of empirical work. More empirical work is needed testing and underpinning micro-level assumptions about social influence as well as macro-level predictions. In conclusion, we discuss major roadblocks that need to be overcome to achieve progress on each frontier. We also propose that a new generation of empirically-based computational social influence models can make unique contributions for understanding key societal challenges, like the possible effects of social media on societal polarization.

Keywords: Social Influence, Opinion Dynamics, Polarization, Calibration and Validation, Micro-Macro Link

This article is in memoriam of Rosaria Conte (1954-2016).

Introduction

1. Social influence is a pervasive force in human social interaction. In many social encounters, individuals modify their opinions, attitudes, beliefs, or behavior towards resembling more those of others they interact with. Individuals are socially influenced because they are persuaded by convincing arguments (Myers 1982), because they seek to be similar to others (Akers et al. 1979), because they are uncertain about a decision and follow the lead of others (Bikhchandani et al. 1992), or because they feel social pressure to conform with social norms (Festinger et al. 1950; Homans 1950; Wood 2000).

2. Despite much research, social influence remains one of the most puzzling social phenomena. On the one hand, empirical studies across a variety of areas have documented how social influence reduces differences between people, as has been found in experiments on conformity (Asch 1956), research on small group behavior (Sheriff & Sheriff 1979), persuasion (Myers 1982), innovation diffusion (Rogers 1995), the influence of mass media (Katz...
The complex relationship between social influence as a micro-level process and its macro-consequences for consensus or divisions in society resonates in classic as well as highly contemporary debates in the social sciences. A first example is Durkheim’s classical analysis of social integration in the face of increasing societal differentiation as society moves into modernity [Elias 1978; Durkheim 1982; 1895; Mâs et al. 2010; Turner 1995]. Durkheim argued that consensus in individuals’ opinions and values depends on a cohesive society that exposes its members to highly similar social influences. However, as a society modernizes, Durkheim believed, it may also become less cohesive, for example because economic differentiation and division of labor makes people’s social roles and living situations increasingly different from each other. What then are the conditions and mechanisms that prevent increasing disagreement on fundamental norms and values between members of a society?

A second example is the question why there is cultural differentiation, which is essentially Axelrod’s question. Theorists of cultural differentiation [Bourdieu 1984; 1979] aimed to understand how cultural differences and boundaries between societal groups, like between an upperclass “high-brow” culture and a lower class “low-brow” culture, emerge and are maintained although there is interaction between members of different classes in which social influence could reduce these differences. A third, highly contemporary, debate is whether and under what conditions societies polarize, falling apart into a small number of deeply antagonistic factions, with ever increasing differences between them, as some observers note for the current political landscape of the U.S. [Abramowitz & Saunders 2008; DiMaggio et al. 1996; Evans 2003; Fiorina & Abrams 2008; Gentzkow 2016] and many other Western societies. Based on extensive empirical studies of opinion formation at the community level in the U.S., Abelson [1964] noted already five decades ago the prevalence of polarization but failed to reconcile this pattern with models in which social influence was described as reducing rather than amplifying opinion differences. Abelson famously wondered “what on earth one must assume in order to generate the bimodal outcome of community cleavage studies” (p. 153). Echoing this question, Bonacich & Lu [2012] recently included explaining “how groups become polarized or how two groups can become more and more different” (p. 216) in their list of important unsolved problems of sociology.

Such questions cannot be answered by empirical studies alone, but require theoretical modelling. The evolution of a distribution of political opinions observed in a society results from numerous simultaneous interactions between individuals, typically connected by heterogeneous social networks and embedded in diverse local and socio-demographic contexts. Most importantly, social influence dynamics can give rise to complex micro-macro links in which the societal outcome of individual interactions can be unexpected and unintended from individuals’ point of view. Identifying the conditions and mechanisms of consensus, diversity and polarization in large-scale social-influence dynamics is therefore a major scientific issue with a long tradition of vivid debate [Mason et al. 2007].

The earliest formal models of the dynamics of opinion formation in a group were inspired by conformity experiments [Abelson 1964; French 1956; Harary 1959]. They took as basic building block the assumption that if two members of a group interact “each member of the group changes his attitude position towards the other by some constant fraction of the ‘distance’ between them” [Abelson 1964]. It could then be shown analytically for a broad class of models of this type that repeated social influence always leads to consensus of all group members unless the network of interactions consists of perfectly disconnected subgraphs [Abelson 1964; Berger 1961; DeGroot 1974; Harary 1959; Lehrer 1975]. This can explain why many groups often have consensus on a lot of issues – a fact that is often overlooked because these issues are not matter of contention anymore. But the result also seems to be in striking contrast to many empirical cases social scientists have studied in the field.

Neither small groups, organizations, neighborhoods, nor society at large exhibit an inevitable tendency towards perfect consensus on all issues, as examples from group discussion experiments as well as studies of political, social, and cultural views demonstrate [Glaeser & Ward 2006; Liu & Srivastava 2015; Mark 2003]. Studies of college dormitories [Feldman & Newcomb 1969], international work teams [Earley & Mosakowski 2000], representative opinion surveys on controversial issues in the public debate [Abramowitz & Saunders 2008; Evans 2003; Levendusky 2009] and experiments even suggest that influence dynamics sometimes result in gradually
increasing dissimilarity and polarization. This contrast between results from early formal models of social influence dynamics and empirical evidence led Axelrod to formulate the question why not all differences eventually disappear if social influence reducing differences between people is such a pervasive force in social interaction? 

1.8 Neither Axelrod, nor any of his predecessors, did of course believe that real social-influence dynamics consist of nothing else but of repeated encounters in which any two individuals become more alike every time they interact. In the real world, networks are not always connected, social influence is sometimes rejected, individuals’ views may be deeply entrenched on some issues and open to influence on others, and at the societal level mass media, divisive political propaganda or dividing lines between different group identities may curb the assimilating forces of interpersonal social influence. Agent-based modelling is a method that has the potential to rigorously explore the complex dynamics that may result from the interplay of all these factors with different fundamental influence mechanisms in interpersonal interactions.

1.9 As Chattoe-Brown (2014) points out, such models have the ability to separate calibration (empirically justifying, for example, assumptions about individual behavior) from validation (empirical testing of model implications, establishing how well simulated data match corresponding real data). Models can thus be built “representing social actors directly [. . .] as they interact with each other and with their environment” (p. 2). In this way, agent-based modelling holds the promise to provide models that are not only descriptive of interpersonal influence dynamics as they occur in real-world settings at the micro-level, but also can “grow” from these assumptions patterns of opinion diversity and their association with context variables (e.g. group size or initial diversity) observed at the macro-level of a group, organization, or society that the model targets. Agent-based models of empirically observed social-influence dynamics could thus move beyond the correlational explanations conventional empirical research can offer and meet instead the necessary criterion for a complete scientific explanation that Epstein famously formulated in his “bumper sticker reduction of the agent-based computational model”, “if you didn’t grow it, you didn’t explain it” (Epstein 1999).

1.10 For this promise to be fruitfully realized, however, agent-based modelers need to have a solid understanding of how each of the many factors and mechanisms that could affect the outcomes of social influence in the real world interact separately and simultaneously with simple “first principles” of interpersonal social interaction. As Macy & Flache (2009) put it, rephrasing Epstein, “if you don’t know how you grew it, you didn’t explain it” (p. 63). We thus believe that in order to understand how and why empirically calibrated models may or may not succeed in reproducing social influence dynamics in real life, agent-based modelers should have a good overview over the main approaches to modelling social influence in the literature and how they relate to the more specific models that have been proposed. In this paper, we start from an overview over the main approaches trying to answer Axelrod’s question building on “first principles”. We show that extensions of the early formal models of social influence developed in recent decades cannot only generate the emergence of persistent opinion diversity, but also patterns of collective extremization, stable diversity in form of clustering of opinions, or polarization of a population into two or more antagonistic factions with large and possibly increasing opinion differences between them alongside strong internal consensus.

1.11 In what follows, we discuss the main theoretical ingredients that have been added to the early models, and show why they generate different outcomes. Notwithstanding some exceptions (e.g., Brousmiche et al. 2016; Defluant et al. 2008), most of the work in the literature pursues the theoretical goal of identifying conditions for consensus, clustering or polarization that emerge from fundamental micro-processes of social influence. However, this does not mean that these models have not been calibrated to empirical data whatsoever, or that their outcomes have not been compared to empirical evidence. In many contributions authors derive the theoretical assumptions they make both from fundamental psychological theories about social influence and from empirical evidence, thus ‘calibrating’ models in a broad sense. Similarly, in many papers outcomes of social influence dynamics observed in experiments or field data are used to assess at least qualitatively the plausibility of model predictions, thus aiming at ‘validation’ of models in a loose sense. To show this, we discuss for each the classes of models the theoretical and empirical foundations on which they draw, which qualitatively distinct outcomes in opinion distributions they aim to generate, and how they have served as basis for follow-up work including further factors such as media influence, heterogeneous networks or different forms of social influence co-occurring at the micro level.

1.12 Yet, despite all advances, we conclude from our overview that the agent-based modelling literature still cannot offer reliable explanations and predictions for concrete real-life influence dynamics a researcher may be interested to study, a situation that has not much changed since nearly a decade ago an earlier review of the field came to a similar conclusion. One reason for this is that, as we discuss in Section 3 the field needs to move forward towards calibration and validation of models in a more precise sense, linking models and data on a more detailed level. Another, related problem is that the literature provides many explanations for
many possible collective dynamics of opinions, beliefs, or behavior. Despite efforts to gradually extend models, much remains unclear about which model ingredient or which combination of them might be the most useful one to ‘grow’ a given empirical phenomenon observed in a particular context with a particular type of data available, like for example the increasing polarization observed in surveys on political issues in recent years in the U.S. (Gentzkow 2016), the increasing acceptance of homosexual relations found in U.K. surveys since the early 2000’s (Chattoe-Brown 2014), or the dynamics of opinions subjects express in a small-scale group discussion experiment (e.g., Moussaid et al. 2013).

1.13 A central challenge for the development of social-influence models is that a model that in one setting accurately describes opinion shifts resulting from influence may fail to capture social influence in another setting. For instance, empirical research suggests that individuals are more open to voicing their opinions in computer-mediated than in face-to-face interaction (Ho & McLeod 2003) and that social influence is stronger in face-to-face interaction (Sassenberg et al. 2005). This implies that a model that was not empirically supported in a given setting may still accurately describe empirical patterns found in another one. We believe researchers should follow a “middle-range approach” (Hedström & Ylikoski 2010; Merton 1957), in which the choice of assumptions about social influence is guided by theoretical and empirical arguments specifying why a particular assumption is considered plausible in a given setting. Furthermore, both the assumptions made in a model and empirical predictions a model generates should be confronted with data available for the specific social setting a modeler wants to address.

1.14 Next to a need for more empirical grounding, another challenge the field faces in our view is insufficient theoretical integration and comparison of a multitude of different modelling approaches. Still very little is known about the dynamics resulting from two or multiple model ingredients acting in tandem. These gaps in the understanding of influence dynamics leave the modeler of a given real-life setting with a long list of alternative model assumptions and qualitatively different sets of parameter values that can be included in her model. As even very subtle and seemingly innocent changes in the assumptions in social-influence models can have profound and unexpected effects on model predictions, the modeler’s ability to derive precise and reliable predictions is highly limited. This leads us, finally, to propose frontiers for future research on models of social influence dynamics. Future work should move towards these frontiers with theoretical as well as empirical research, and with addressing new practical applications of social influence models.

Ideal Typical Models and Outcomes

2.1 Here, we review the literature on social influence models. Given the huge number of modelling studies in the literature, it is impossible to do justice to every contribution. Nevertheless, we argue that large parts of the literature can be categorized into three classes of models.

2.2 Models were grouped into the same class if their theoretical assumptions about social influence were formally implemented in a similar way and, therefore, lead to similar answers to Axelrod’s question. Models within the same category may represent different social contexts and may be based on different theories about social influence, but the formal implementation of these theories gives rise to similar fundamental dynamics and conditions for different forms of opinion diversity.

2.3 Our review covers influence models with continuous as well as nominal traits representing opinions. In the early influence models developed in the 1950 and 60s (Abelson 1964; Berger 1981; DeGroot 1974; French 1956; Harary 1959; Lehrer 1975), actors are socially influenced in the position they take on a continuous spectrum representing their “opinion” on some issue, for example their stance on what the appropriate speed on a highway should be. In what follows, we likewise use the term “opinion” for the agent’s property that is affected by social influence in a model. However, opinion should be seen as a generic concept that can also represent a belief (e.g. What is the average speed of all cars driving in a highway?) or a behavior (e.g. How fast does the actor actually drive on highways?), or an attitude (e.g. How good or bad is it to drive at a given average speed on highways?). To paraphrase Axelrod (1997), an opinion “is taken to be what social influence influences” (p. 207). A later generation of models assumed instead that opinions do not vary on a continuous scale, but model the choice between distinct options, like a person’s favorite political party, music band, or movie genre (Axelrod 1997; Latane & L’Herrou 1996; Liggett 1985; Sznajd-Weron & Sznajd 2000). Some models see such ‘nominal traits’ as a simplified representation of underlying continuous dimensions (Nowak et al. 1999). While the assumed scale of the influence dimension can alter model predictions decisively in some cases (e.g., Flache et al. 2006), often fundamental results for models belonging to the same class generalize, as we show below.

2.4 Our review does not cover so-called diffusion or contagion models (e.g., Valente 1996). These models describe processes in which some entity, like a virus, or a piece of information spreads in a network through ‘contagion’,
a process that is unidirectional. In models of virus diffusion in networks, for instance, an actor carrying a virus can infect her network contacts, but these contacts cannot heal their infected contact. Likewise, a person who is unaware of the existence of a new product can be informed about the product but the person cannot erase the memory of others. In contrast, the models that we review assume bi-directional influence, in that they do not assume that influence acts only in one direction. Note that the information or virus diffusion models should not be confused with innovation diffusion models. Indeed, the diffusion of innovations is a more complicated process than the diffusion of information or viruses and its models generally include attitude or opinion dynamics such as the ones described below (e.g., Deffuant et al. 2005, Valente 1995).

Social influence on the micro-level can result in various macro-structures and dynamics of opinion distributions, as documented by empirical research across various contexts, such as work teams (Earley & Mosakowski 2000), groups of college students (Feldman & Newcomb 1969), school classes (Pearson et al. 2006), society at large (Abramowitz & Saunders 2008, DiMaggio et al. 1996, Fiorina & Abrams 2008) and in the laboratory (Mäs & Flache 2013). Figure 1 illustrates three distinct ideal-typical opinion dynamics for continuous opinions that received much attention in the modeling literature. Some other patterns will be discussed elsewhere in this paper. To generate the figure we used the illustrative models that we formally define in the remainder of this section (Equations 1–3).

First, reflecting Durkheim’s concern with societal integration, models can describe the formation of a collective consensus from initial disagreement. Figure 1a shows how such a consensus emerges on a ‘moderate’ position close to the mean initial opinion in the population. However, sometimes a pattern called “group polarization” (Myers & Lamm 1976) in social psychology occurs, when a group moves towards a consensus that is more extreme than most or even all of the views individuals held prior to being exposed to social influence (Moscovici & Zavalloni 1969, Myers 1978). Below we discuss how this emergence of an extreme consensus was likewise addressed with formal models. Second, as a potential answer to Bourdieu’s (and Axelrod’s) question how social differentiation can persist, models were developed that can generate opinion clustering. Figure 1b shows such a process in which a population with initially uniformly distributed opinions divides into multiple internally homogenous but mutually distinct clusters in the opinion spectrum. Third, while opinion clustering does not necessarily imply sharp differences between subgroups, modelers also addressed Abelson’s question of how processes of polarization could be understood (called bi-polarization hereafter to distinguish this from the concept of “group polarization” which describes the formation of an extreme consensus). Figure 1c illustrates such a dynamic. It shows how bi-polarization is distinct from opinion clustering in that a random start the population increasingly falls apart into two factions with disagreement between them eventually growing towards the theoretical maximum.

Table 1 provides an overview over the three classes of models that we distinguish. In the following subsections, we illustrate for each class the main idea with a simple illustrative model, discuss alternative theoretical and empirical arguments underlying the models assigned to each class, and main results as well as different ver-

Figure 1: Typical opinion dynamics generated by agent-based models of social influence: Evolution of the distribution of opinions in a one-dimensional bounded opinion space in a fully connected population.
<table>
<thead>
<tr>
<th>Model class</th>
<th>Core assumption</th>
<th>Core result</th>
</tr>
</thead>
<tbody>
<tr>
<td>Models of assimilative social influence</td>
<td>Individuals connected by a structural relationship always influence each other towards reducing opinion differences.</td>
<td>If relationships form a connected network, influence dynamics (with continuous opinions) inevitably generate consensus in the long run.</td>
</tr>
<tr>
<td>Models with similarity biased influence</td>
<td>Only sufficiently similar individuals can influence each other towards reducing opinion differences. How much similarity is sufficient depends on additional psychological mechanisms (e.g. social identity, confidence in others).</td>
<td>Consensus can be avoided. If the similarity bias is sufficiently strong, then multiple homogenous but mutually different clusters emerge (fragmentation). Opinions, however, never leave the initial range.</td>
</tr>
<tr>
<td>Models with repulsive influence</td>
<td>When individuals are too dissimilar (in some models on a specific opinion dimension) they can also influence each other towards increasing mutual opinion differences (repulsive influence). How much dissimilarity is needed to trigger repulsive influence depends on additional psychological mechanisms (e.g. social identity, “ego-involvement”).</td>
<td>Consensus can be avoided. Clusters form and may even adopt maximally opposing views (bi-polarization). Opinions can leave the initial range.</td>
</tr>
</tbody>
</table>

Table 1: Three classes of social-influence models.

While our three ideal-types of models capture a large part of the literature, they are not exhaustive. For instance, many contributions to the literature combine assumptions from multiple ideal types. Yet, we believe that a good understanding of the characteristic behaviors of each type of model is indispensable for understanding the dynamics of combined models, too. Furthermore, our synthesis of the literature identifies critical assumptions and central predictions of existing models and, therefore, proposes perspectives for future empirical and theoretical research on social-influence dynamics that we discuss in Section 3 of this paper.

Models of assimilative social influence

Main idea

The central building block of models in this class is the assumption that if two individuals are connected by an influence relationship, they will always exert influence on each other towards reducing their opinion differences (assimilation). Note, however, that while the network of influence relationships is assumed to be structurally given and fixed in these models, it is not excluded that social influence can be ineffective. Influence does not result in opinion adjustments, for instance, when an actor is exposed to influences from multiple sources that cancel each other out, or when the influence exerted by an actor is superseded by more influential parties. However, models of assimilative influence share the assumption that actors connected by an influence relationship would always grow more similar if there were no such third-party effects.

Theoretical and empirical justifications

Models of assimilative influence have been developed based on various theoretical and empirical lines of research. Cognitive theories emphasized that when interaction partners discuss an issue they persuade each other [Myers1982, Vinokur & Burnstein1978], other approaches highlighted the role of imitation or social learning among peers (Akers et al.1979), or of social pressure to conform with group norms (Allport1924, Asch1955, Homans1950, Sherif1935). Likewise, cognitive consistency theories and social balance theory posit that individuals seek to be similar to people they like or respect (Festinger1957, Heider1967). In order to resolve the dissonance resulting from disagreement with other actors, individuals try to convince those actors to adopt...
similar opinions or may change their own opinions to conform to theirs (for a formal derivation how this entails assimilative influence see Groeber et al. 2014). It has also been argued that social influence is deeply rooted in humans’ nervous system, forming a natural and unconscious propensity to imitate or echo the gestures and postures of observed others (Rizzolatti & Craighero 2004). Evolutionary game theory and empirical research on social learning suggest furthermore that our tendency to imitate and follow group pressures may have evolved as a successful decision making strategy in the human evolutionary past (Richerson & Boyd 2005).

**Formal implementations with continuous opinions**

**2.11** Prominent representatives of models with assimilative social influence are the averaging-models that were developed in the 1950ies and 60ies (Abelson 1964, DeGroot 1974, French 1956, Harary 1959, Lehrer 1975). These models treat individuals as nodes in a network. Nodes are connected by a network link if they, in one way or the other, exert influence on each other. Network links are assumed to remain unchanged over time, but they are weighted. Weights scale the strength of social influence one actor exerts upon another and can be seen as capturing structural differences in, for example, persuasiveness, social status, frequency of interaction, or power between actors. The defining feature of this type of models is that influence weights are fixed. Following Hegselmann & Krause (2002) models of assimilative influence, with continuous opinions and fixed influence weights, are also often called “classical” models in the literature.

**2.12** Classical averaging models assume that opinions vary on a continuous scale and implement social influence as averaging (Friedkin & Johnsen 1990, 2011). That is, when an actor’s opinion is updated, her new opinion moves towards the weighted average of her previous opinion and the opinions of her network neighbors. Equation (1) illustrates how under social influence actor $i$ shifts her opinion $o_{i,t}$ at time point $t$. The weights $w_{i,j}$ represent the impact that agent $j$ has on $i$‘s opinion. To simplify the exposition, we assume $0 \leq o_{i,t} \leq 1$ throughout, but this is not an essential model feature.

$$o_{i,t+1} = o_{i,t} + \Delta o_{i,t} = o_{i,t} + \mu \sum_j w_{i,j} (o_{j,t} - o_{i,t})$$

**2.13** The parameter $\mu$ ($0 < \mu \leq 1$) defines the rate of opinion convergence and can be used to smoothen opinion dynamics. Often, in these models the constraint is imposed that the weights represent the influence of a particular other actor on $i$ relative to the total amount of influence imposed on a target, i.e. $\forall i: \sum_j (w_{i,j}) = 1$. Most classical implementations also assume that all agents update their opinions simultaneously in one discrete time step, based on the state of the population that resulted after updating at the previous time point. Figure 2 shows model behavior under these assumptions for a smooth rate of change ($\mu = 0.1$).

**Typical macro behavior**

**2.14** Already early contributions demonstrated that the classical averaging models imply the emergence of perfect opinion consensus in the long run, as long as the social network is connected. In a connected network, every actor is influenced directly or indirectly via intermediate links by every other actor. Whenever there is influence, overall opinion differences in the network decline such that eventually all actors align with the emergent consensus. Figure 2 illustrates this dynamic.

**Formal implementations with nominal opinions**

**2.15** Deviating from the classical averaging models, several formal theories assume that the opinion scale is nominal, i.e. an opinion represents a choice from a set of distinct options, like a choice between political parties or different music styles, rather than a position on a continuous scale. This makes it impossible to define gradual distances between different opinions, two actors can only agree or disagree in one dimension of the opinion space. Depending on how social influence is implemented in these models, this seemingly innocent assumption can alter model implications profoundly, even when there is always assimilative social influence between connected actors.

**2.16** An important implication of assuming nominal opinions is that social influence cannot be implemented as averaging. The voter model assumed, for instance, that actors can adopt an opinion of either +1 or -1, and copy the opinion of one of their contacts (Holley & Liggett 1975). Similar to the macro-implications of the classical averaging models, this imitation dynamics typically entails eventual consensus in connected networks.
studies of this model by socio-physicists also revealed that the dynamic can provide very rich patterns including metastable states with co-existing regions with opposite opinions in a network, when networks have special structures or are infinitely large [Castellano et al. 2009].

2.17 An alternative implementation of unconditional social influence in models with discrete opinions assumes that actors adopt the most frequent opinion amongst their network contacts, like in models implementing a local majority rule intended to describe dynamics of public debate [Galam 2002]. Sometimes influence of network neighbors is weighted by their individual “social impact” [Latané & L’Herrou 1996; Liggett 1985; Nowak et al. 1990; Parisi et al. 2003]. When opinions adopt either a value of -1 or +1, Equation 2 describes this model.

\[ o_{i,t+1} = \text{Sign} \left( \sum_j w_{ij} o_{jt} \right) \]  

2.18 This model generates consensus when all pairs of agents in a population are connected by influence relationships. However, when all actors are only exposed to a small local subset of the population in their network, configurations can arise in which everyone holds an opinion that is locally a majority view, but is different in different regions of the network.

Critical conditions and limitations

2.19 Models of assimilative influence are prone to generate consensus, in particular when they assume opinions with a continuous scale. Across different model versions, the most important critical condition for whether diversity can be maintained is the structure of networks. Segmented networks can preserve diversity if they entirely isolate subgroups from outside influence or at least restrict interactions to small local neighborhoods (in models with local majority rules).

2.20 Some diversity may also be maintained in continuous models despite connected networks, if agents are assumed to be stubborn to some extent [Friedkin 1990; Friedkin & Johnsen 2011]. These models assume that opinion adjustments are always a tradeoff between social influence and actors’ initial view that represents individual interests, or entrenched beliefs differing between individuals. With stubbornness, models can reach equilibria where actors still disagree but refuse to change opinions any further, because they do not want to deviate even more from their initial convictions. However, even then social influence greatly reduces opinion diversity over time. In particular, the averaging assumption implies that opinions will never move outside of the range of initial opinions [Friedkin & Johnsen 2011]. Models that assume assimilative social influence thus fall short of explaining how diversity could increase over time (Abelson’s question) or how opinion clustering can persist in dense highly connected networks (Axelrod’s question) without individuals’ fixation on their initial opinions.

Models with similarity bias

Main idea

2.21 Models with similarity bias abandon the assumption that there is always influence as long as there is a structural connection between agents. Instead, whether social influence occurs between connected individuals and how strongly they influence each other, is now linked to individuals’ similarity.

2.22 Agent-based modelers used this assumption to explain why under certain conditions influence may stop altogether reducing opinion differences [Axelrod 1997; Carley 1999; Deffuant et al. 2000; Hegselmann & Krause 2002; Mark 1998]. The key assumption in these models is that if an agent disagrees too much with the opinion of a source of influence, the source can no longer influence the agent’s opinion. How much disagreement is “too much” before an agent loses “confidence” in a source, that is – at what point exactly the disagreement exceeds the critical level and an agent is no longer open to influence – can be further elaborated, modelling psychological processes that were studied in research on “attitude strength” in social psychology (e.g., [Eagly & Chaiken 1993; Festinger 1957]). Confidence in the opinion of a source may be related to things like whether two actors belong to the same social category or not, or whether the issue at stake is very salient or central for an agent’s identity (“ego-involvement”), etc.

2.23 With these assumptions a similarity bias can generate a self-reinforcing dynamic in which agreement strengthens influence and influence leads to greater agreement with those who already have a similar opinion. Multiple
modelling studies demonstrated how this feedback loop can result in the emergence of persistent opinion clusters [Axelrod 1997; Deffuant et al. 2000; Hegselmann & Krause 2002; Mark 1998].

2.24 Models with similarity bias were first proposed for opinion dynamics in nominal opinion spaces [Axelrod 1997; Carley 1991]. For sake of illustration we present here a slightly modified version of the continuous model of Deffuant et al. 2000. Unlike in the model of assimilative influence formalized by Equation 1, the weights \( w_{ij} \) are in this model not exogenously given, but depend on the current disagreement in opinions between the two agents, \( w_{ij} = f_w(o_i, o_j) \).

2.25 In our illustrative model, the influence dynamic consists of a sequence of events in which at every time point exactly one randomly chosen population member \( i \) can update her opinion and does so by selecting at random one other agent \( j \) to interact with. If \( i \) and \( j \) interact, then \( i \) modifies her opinion to move closer towards the opinion of \( j \), but only if their opinions were sufficiently similar before. Equations 3 and 4 below describe the rules for opinion change in our illustrative model.

\[
a_{i,t+1} = a_{i,t} + \Delta a_{i,t} = a_{i,t} + f_w(a_{i,t}, o_{j,t})(a_{j,t} - a_{i,t}) \tag{3}
\]

\[
f_w(o_i, o_j) = \begin{cases} 
\mu, & \text{if } |o_i - o_j| \leq \epsilon \\
0, & \text{otherwise} 
\end{cases} \tag{4}
\]

2.26 The parameter \( \epsilon \) in Equation 4 defines what Hegselmann & Krause 2002 called a confidence level (also called confidence threshold). Influence from another actor \( j \) can only affect \( i \)'s opinion if their disagreement \( |o_i - o_j| \) does not exceed this threshold. The parameter \( \mu \) defines the rate of opinion convergence and is typically constrained to \( 0 < \mu \leq 0.5 \) (e.g., Deffuant et al. 2000). The core principle of influence in this model has been implemented with different assumptions about the exact “communication regime” (Urbig et al. 2008). The two basic versions of the model consider on the one hand agents meeting in pairs and possibly influencing each other, and on the other hand agents meeting everyone else at once while only being influenced by those in sufficient agreement with them. Indeed, in Deffuant et al. 2000 and many follow-up papers both \( i \) and \( j \) change opinions simultaneously, while in another seminal model of bounded confidence, Hegselmann & Krause 2002 assumed instead that all agents in the population influence each other simultaneously. In their model, every agent \( i \) adopts in one step the average opinion of all those whose disagreement with \( i \) did not exceed \( \epsilon \) before the interaction. Urbig et al. 2008 integrated these different versions, varying the number of agents meeting at once, and showed that while there are some differences in model behavior, core model implications remain the same. In our illustrative model used for generating Figure 1, we thus slightly modified the model of Deffuant et al. 2000 in assuming that only one of two agents “meeting” modifies her opinion. This modification does not change the basic properties of the dynamics.

Theoretical and empirical foundations

2.27 Models that introduce a similarity bias draw on theoretical sources similar to those of unconditional social influence. Yet, an important difference is that these theories are not only applied to the way how individuals modify their opinions, but also to the change of the social or cognitive interpersonal relations through which influence occurs. Broadly, two perspectives can be distinguished. One line of work draws on cognitive theories and emphasizes the similarity between the attitude conveyed in a message of social influence and the attitude of the recipient. Another line of work focuses more on the social relation between a source of influence and the recipient, highlighting that social influence is stronger or more likely between more similar people.

2.28 Assumptions of bounded “confidence” [Deffuant et al. 2000; Hegselmann & Krause 2002] emphasize the similarity between message and attitude of the recipient, drawing on the theory of “confirmation bias” [Nickerson 1998], the tendency to take into account preferentially information that confirms one's preconceptions and avoids contradictions with prior beliefs. Social judgement theory [Sherif & Hovland 1961] links this more specifically to attitude change in interactions. In this view, individuals are most influenced by a source if the source expresses an opinion that falls within a zone of non-commitment where it is neither too similar nor too different from the receiver's opinion. If the opinion of the source is very similar, it falls within a zone of acceptance for the receiver but induces only little further change, while source opinions that are too different fall in a rejection zone where they do not influence the individual. Differences between individuals and contexts in the width of these zones can be further derived from psychological theories and experiments about the extent of ego-involvement and attitude strength [Eagly & Chaiken 1993, for a review], suggesting that more confident individuals are more resistant to influence from discrepant sources [Moussaïd et al. 2013] and thus have a smaller zone of non-commitment and a wider zone of rejection.
2.29 Other modelers highlight more the similarity between source and recipient to justify the assumption of similarity-biased influence. One foundation of this view is that individuals are cognitively more receptive to influence if the source of influence is more similar to them. [Mark 1998] bases this idea on symbolic interactionism [Stryker 1980], a theory positing that in situations where new information is needed, people seek input preferably from sources with whom they have more similarity in terms of shared ideas about the world. Others (e.g., [Axelrod 1997]) take a different approach and derive the assumption of a similarity bias from one of the most prevalent regularities of social life, known as the principle of “homophily” [Lazarsfeld & Merton 1954, McPherson et al. 2001, Wimmer & Lewis 2010], according to which people more likely interact and communicate with similar others. It should be noted that despite similar formalizations, the underlying idea is different. Homophily may be caused by structural patterns of social interaction that systematically sort similar people into similar “foci” [Feld 1982] where they meet and interact, like schools, neighborhoods, or workplaces. But a similarity bias in selecting interaction partners can also be cognitive or emotional. Psychological research underpinning Byrne’s (1971) “attraction paradigm” showed that more similar people like each other more and therefore seek each other more as partners of interaction and are more open to influence from each other, a pattern supported by research on social networks [Pearson et al. 2006, Stark & Flache 2012, Wimmer & Lewis 2010].

Typical macro behavior

2.30 Models using dynamics like those described by Equations [3] and [4] have been used to study the convergence process of opinions from initial diversity [Deffuant et al. 2000, Hegselmann & Krause 2002]. A key insight is that if the confidence level $\epsilon$ is sufficiently small, the population ends up fragmented in separate opinion clusters, while otherwise convergence towards consensus occurs just as in classic continuous models. The smaller the confidence level, the smaller and more numerous are the opinion clusters in which the population fragments.

2.31 Figure [1b] illustrates a typical dynamic for an intermediate confidence level of $\epsilon = 0.15$, using the model of Equations [3] and [4] with 100 agents with initially uniformly randomly distributed opinions. Agents who initially have relatively similar opinions are pulled towards the mean opinion in an emergent cluster close to their initial position. As clusters crystallize out, the differences between them increase until differences exceed the confidence level $\epsilon$ and influence between different clusters ceases to “pull” agents towards the opinions of other clusters than their own.

2.32 It is noteworthy that typical macro-behaviors of bounded-confidence type models also include extremization of most or all members of a population, both in the form of bi-polarization and of a pattern resembling “group polarization”. Figure [2] below shows two examples of convergence of a large majority of the population to one extreme from an initially uniform opinion distribution. This pattern can arise from bounded confidence dynamics, when the initial population of agents comprises both extremist agents, having an opinion close to the extremes and a very small confidence level $\epsilon$, and moderate agents with a larger openness to outside influences (larger confidence level) and an initially randomly distributed opinion. With these assumptions, the extremist agents are very influential and are hardly influenced by moderates.

2.33 Depending on the exact initial distributions of opinions and uncertainty levels, social influence in populations with heterogeneity in uncertainty levels may result in bi-polarization – where extreme agents on both sides of the spectrum pull large numbers of moderates to their extreme position $o$, or a pattern more resembling “group polarization”. In this outcome most or all initially moderate agents move to the same position more extreme than their initial opinion. Figure [2] shows group polarization with a small minority of moderates taking the extreme position opposite to the emergent mainstream, while Figure [2b] shows “single extreme convergence” in which everyone except the initial extremists at $\alpha = 0$ ends up in the extreme group with $\alpha = 1$. Also a mix of those patterns with some moderate groups surviving the influence from extremists is possible.

2.34 As Figure [2b] demonstrates, bounded confidence dynamics can in particular also imply that a whole population of initial moderates can be driven to one extreme, despite an equal initial distribution of extremists at both extremes of the opinion spectrum. This pattern, and the others, have been systematically studied for different variants of the bounded confidence model, particularly ones in which the tolerances are also modified during the interactions, different types of networks and different values of the model parameters [Amblard & Deffuant 2004, Deffuant 2006, Deffuant et al. 2002, Lorenz 2008, 2010]. As shown in [Deffuant & Weisbuch 2008] the single extreme convergence happens if moderates first concentrate in the center of the opinion spectrum where they can get outside of the range of influence of one of the extremes because of random fluctuations. Then the moderates drift to the other extreme. This pattern is more likely to take place when the extremists are not too numerous, because when they are, they attract the moderates to both extremes. Moreover, under the original bounded confidence model (with constant tolerances), a pattern in which, the opinions of the moderate agents keep fluctuating all the time also can take place [Mathias et al. 2016]. This is because moderate agents with
Individual trajectories in opinion space over time:

A: Bi-polarization with large majority at one pole ($\sigma_c = 0.4$, $\sigma_o = 0.01$)

B: Group-polarization ($\sigma_c = 0.45$, $\sigma_o = 0.01$)

Opinion distribution over time:

Figure 2: Examples of convergence of almost the whole population to one extreme, despite a symmetric initial distribution, using the bounded confidence model with highly confident extremists. The opinion of moderate agents is represented by blue dots, the opinion of initially extremist agents by red dots ($N = 100$, 5 extremists initially at both ends of the opinion spectrum, initial opinion moderates uniform random).

Recent work by Hegselmann & Krause [2015] used a combination of simulations and analytical tools to derive many of these phenomena from a general model in which a population following bounded confidence dynamics is exposed to an external signal as additional source of influence, sent for example by charismatic leaders, radical groups or – in a scientific discourse – by empirical evidence of the “truth” about a real world phenomenon under discussion by scientists. They showed that the exact effects of the intensity of signals on the degree of extremization in a population interact sensitively and in sometimes counterintuitive ways with the distribution of confidence levels and initial opinions in the population. Resonating earlier results discussed above, they find for example that more intensive signals may decrease rather than increase convergence on extreme positions advocated by the signal. This happens if those agents moving towards the position of the signal move too quickly, so that they drop out of the confidence range of a majority of population members who do not “hear” the signal. This majority is then “left behind” and stays at moderate positions, because it can no longer be influenced by those who hear the signal.

Bounded confidence models have become a hugely influential modelling class implementing similarity biased social influence with continuous opinions. A large literature has evolved on extensions, modifications and analytical treatments of these models, often using tools of statistical physics. It is impossible to give a complete overview here. Comprehensive reviews can be found in Lorenz [2007] or Castellano et al. [2009].

Alternative implementations of similarity-biased influence

Like for models of assimilative influence, an important distinction is between models assuming a continuous opinion space (Bounded Confidence-models) and models assuming distinct nominal opinion categories. Models with nominal opinion spaces combine social influence with homophily, implemented as a lack of interaction if dissimilarity exceeds a critical threshold. In these models the agents have a vector including several discrete opinions (or cultural traits) and the similarity is computed between such vectors. Drawing on Carley [1991], Axelrod [1997] modelled spatially local interaction with a regular bounded lattice. The likelihood for an agent to select a particular neighbor for interaction is equal to the proportion of opinion dimensions (called features by Axelrod) in which they have the same trait (modelling homophily). If an agent interacts with a neighbor, then on a feature in which they still disagree, the trait of the neighbor is copied (modelling influence) so that the agents
become more alike as a result. Most importantly for model behavior, interaction and thus influence becomes impossible if two neighbors have nothing in common.

2.38 Axelrod’s [1997] computational studies showed how local convergence can lead to stable spatial opinion clustering from initial randomness. In areas of the spatial network where agents locally happen to be relatively similar to each other, they influence each other more and thus agree on an increasing number of opinion dimensions while differentiating from neighbors at the same time. Eventually spatially connected “cultural regions” emerge and stabilize with maximal consensus within and disagreement on all features between neighboring regions.

2.39 Modelling symbolic interactionism, Mark [1998] proposed a model with essentially similar behavior, but representing opinions as a set of “facts” actors can learn from each other when interacting. The more facts two actors share in their knowledge base, the more likely they interact with each other and thus communicate more facts to each other. Again, interaction is impossible if agents have no facts in common. Mark’s model can generate in particular social differentiation from initial homogeneity. This is possible because in an interaction, actors can not only share known facts, but also create with some probability new unique facts. This models the assumption of symbolic interactionism that individuals can create in social interactions new symbols with unique meaning for them, like “cool” new words members of a youth-clique invent to distinguish themselves. New unique facts further spread through social influence primarily to those who are similar to their initial creators and so further differentiate the recipients from other agents in the system.

2.40 Like the bounded confidence models, Axelrod’s model of “cultural dissemination” has sparked a massive follow-up literature addressing a wide range of extensions, modifications and analytical treatments (for reviews see e.g. Castellano et al. 2009). Studies addressed the role of mass media (González-Avella et al. 2007; Shibani et al. 2001), globalization modelled as increasing spatial range of interaction (Greig 2002), or geographical boundaries (Paris et al. 2003). One problem that received particular attention is the sensitivity of cultural differentiation to noise. Axelrod’s model assumes that interaction and thus influence is impossible if agents disagree on all features. However, in the real world agents may occasionally be exposed to other sources of influence than their network neighbors, or may make errors in perceiving each other’s traits or similarity, even when distinct cultural regions have crystallized out. Addressing these sources of error, Klemm et al. (2003a,b) and De Sanctis & Galla (2009) allowed a small probability of random perturbation of cultural traits in Axelrod’s model and found that this small change made cultural diversity far more fragile than Axelrod had suggested. Random changes of traits can generate new cultural overlap between otherwise dissimilar neighbors, thereby breaching through emergent cultural boundaries. Further studies explored mechanisms explaining opinion clustering despite noise. One is that homophily extends to “network homophily” (Centola et al. 2007) in that agents choose to structurally disconnect from dissimilar neighbors (similar to moving into a different neighborhood). Flache & Macy (2011a) showed how cultural diversity could become even more robust when the bilateral interpersonal interaction Axelrod’s model assumed is replaced with “social interaction”, reflecting local conformity pressure. Recently, Ulloa et al. (2016) further extended their model to include conformity pressures exerted by social institutions, like a family to which one belongs that discourages deviation from the family’s cultural identity.

2.41 Other authors have moved towards integrating and comparing continuous and nominal models of similarity-biased social influence. The bounded confidence model has been adapted to a vector of binary opinions, by defining the threshold $\epsilon$ as the sum of the different opinions in two vectors (Deffuant et al. 2000). The study of this model in the case of completely connected populations showed a frequent convergence to a large majority opinion cluster and several minority opinion clusters. This skewed distribution of cluster sizes is very similar to the opinion clustering the model of Axelrod generates if multiple traits are possible per opinion dimension, whereas Axelrod’s model can lead at most to two clusters in a totally connected network with the same setting (2 possible traits per opinion dimension). Other authors approximated continuous opinions in Axelrod’s framework with features on which discrete traits have a defined distance from each other, such that the only way how interaction between $i$ and $j$ is impossible is that they maximally disagree on all features (Flache et al. 2006; De Sanctis & Galla 2009). These studies further highlighted the similarity of conclusions arising from different modelling frameworks. Like in bounded confidence models, sufficiently restrictive interaction thresholds based on opinion distance were needed to sustain levels of diversity similar to those of Axelro’s original model.

Critical conditions and limitations

2.42 Across different models of similarity-biased influence, several similar critical conditions for opinion clustering emerge. Most importantly, the more similarity is needed to make social influence possible between structurally connected agents, the smaller and more numerous are emergent opinion clusters. In bounded confidence models, this condition is governed by the width of confidence intervals. For models based on Axelrod’s [1997], the number of cultural features and traits affects the likelihood of interaction. The more features, the more likely
it is that neighboring agents agree by random chance on at least one feature and thus can interact, while more different possible traits per feature make it less likely to agree by random chance and thus have the opposite effect on the likelihood of interaction. Generally, confidence levels and the number of features on which individuals are open to influence can be seen as representation of societal level characteristics, like the degree of tolerance, “broad-mindedness” or generalized trust in a society, but also as representation of individual trust, openness to discrepant views or connectedness with dissimilar people.

2.43 Network density overall fosters the emergence of consensus in models with nominal opinions, mirroring some of the results obtained when network structures where integrated in bounded confidence models. Amblard & Deffuant (2004) for example found that “single-extreme convergence” rather than opinion fragmentation became more likely with higher connectivity (number of ties per agent in the influence graph - see also Fortunato, 2005; Stauffer & Meyer-Ortmanns 2004). In Mark’s (1998) model, network density depends on the likelihood of interaction between agents, which in turn depends on the size of the memory of agents. The more facts agents can memorize, the more likely two agents can have at least one fact in common and thus interact with a positive probability. Correspondingly, Mark finds that distinct subgroups become larger and less numerous if memory size increases.

2.44 Noise is a second condition with similar effects across different models. A small amount of random noise greatly reduces opinion diversity in Axelrod's model (cf. Flache & Macy 2011a) and similar effects of noise occur under bounded confidence dynamics (Kurahashi-Nakamura et al. 2016; Mas et al. 2010). The mechanism through which noise reduces diversity is essentially the same. In the study of Mas et al. (2010), small random changes of opinions eventually lead agents to shift their opinions into each other’s bound of confidence even when separated opinion clusters have emerged. Like in Axelrod’s model, this re-opens the possibility for new social influence across previously established subgroup boundaries, eventually eliminating opinion differences between opinion clusters. Other implementations of noise under bounded confidence (Pineda et al. 2009) show how noise also can help preserve opinion clustering. In their models, agents adopt with a small probability any possible opinion on the opinion scale, while they otherwise follow a bounded confidence rule. Agents adopting random positions in between emergent clusters can trigger influence cascades towards merging those clusters, because they fall into the confidence ranges of both of them. However, agents adopting random positions close to only one cluster join that cluster and thus stabilize its existence as a separate group in the opinion space. When noise rates are such that both dynamics are in balance, this form of noise can preserve diversity rather than destroy it.

2.45 This result resembles findings obtained in the Axelrod framework (Klemm et al. 2003a,b), where noise can help sustain diversity if the noise rate is in an intermediate range such that opinion clusters cannot merge faster with their neighboring regions than spontaneous changes create new diversity within clusters. This process, finally, is similar to how the random creation of new facts drives the emergence of differentiation in Mark’s (1998) model.

2.46 Similarity-biased social influence offers a preliminary answer to Axelrod’s question. At the same time, for many models in this class the opinion clustering generated by models with similarity-biased influence can be fragile against noise, and is limited to particular slices of the parameters space (sufficiently restrictive confidence bounds, low numbers of features, etc.). Models with similarity-biased influence can explain why there is no influence between some agents and they thus fail to converge. Especially if they assume a nominal opinion space, they can not readily offer an explanation why interaction may sometimes cause actors to even increase and accentuate their mutual differences in one opinion dimension, as suggested by Abelson’s question. The reason is that in nominal opinion spaces differences within one feature do not have a magnitude. Bounded Confidence models instead can show how a whole population can become extremist and possibly bi-polarized by adopting the opinions of its initially most extreme members. Yet, in these models a population can not become more extreme than its initial extremists. This can not account for results from some experiments on group polarization (Moscovici & Doise 1994; Myers 1982) and has thus motivated the search for further answers to Abelson’s question.

Models with repulsive influence

Main idea

2.47 Some model builders tackled Abelson's question by relaxing the assumption that if influence occurs between individuals, it always implies assimilation. Jager & Amblard 2005; Macy et al. 2003; Mark 2003; Salzarulo 2006. In these models of repulsive influence, assimilation was combined with its counterpart, differentiation – the
assumption that some interactions lead individuals to adjust their opinions in such a way as to become more dissimilar to others they disagree with. Different terms have been used in the literature to denote repulsive influence, like rejection, negative influence, differentiation or reactance. Hunter et al. [1984] referred to repulsive influence as the “boomerang” effect occurring if an attempt to attract someone through social influence can have the opposite effect.

2.48 We illustrate the implementation of this mechanism with a modification of our basic model of similarity-biased continuous opinion dynamics given in Equations 3 and 4, similar to the formalization given by Jager & Amblard [2005]. Compared to similarity-biased influence, the only change concerns the way how influence weights are implemented. Equation 5 describes that influence weights can become either positive or negative, depending on the opinion differences.

\[ f_w(o_i, o_j) = \mu(1 - 2|o_j - o_i|) \]  

2.49 Equations 3 and 5 jointly show how the direction of influence switches from a “pull” towards the opinion of the source towards a “push” away from it, as soon as the disagreement \(|o_j - o_i|\) shifts above a critical level. This critical level is here set to 0.5, half of the theoretically maximal disagreement of one unit (0 ≤ o_i ≤ 1). In this basic form, Equations 2 and 5 allow interactions to push the opinion outside of the opinion interval [0, 1]. In some models this is prevented by a smoothening (Flache & Macy [2011b] or truncating function (Feliciani et al. [2017]); in some others the opinion space is self-contained by the specification of the interaction dynamics (Huet & Deffuant [2010]). For the simulations shown in Figure 1c we used a simple truncation rule.

2.50 Different implementations of the weight function \( f \) have been proposed for models with repulsive influence on continuous opinions (e.g. Jager & Amblard [2005] Mäs et al. [2014]), including non-linear and non-continuous versions, but they all share the assumption that weights are positive for small distances and negative for large ones (hence the names “positive influence” and “negative influence” some authors also use, e.g. Takács et al. [2016]).

Theoretical and empirical motivations

2.51 A number of model builders Baldassarri & Bearman [2007] Flache & Macy [2011b] Macy et al. [2003] Mark [2003] motivated the assumption of repulsive social influence by theories that also were used to justify similarity-biased influence, Heider’s balance theory [1946] and Festinger’s theory of cognitive dissonance [1957]. But this time these theories were interpreted as to not only imply that individuals want to be similar to people they like, or to accept the opinion of others when these are similar, but also that individuals strive to be dissimilar to people they dislike, and accentuate disagreement with others if these are too dissimilar. Additionally, several authors assume that social influence relations between individuals are not only modified by homophily, but also by xenophobia Baldassarri & Bearman [2007] Flache & Macy [2011b] Macy et al. [2003] Mark [2003]. Xenophobia is the counterpart of the assumption that people are more open to influence from similar others: the larger the dissimilarity between two interacting individuals, the more they evaluate each other negatively Rosenbaum [1986], triggering differentiation from the source. Other modelers Huet & Deffuant [2010] Huet et al. [2008] derived repulsive influence from a different psychological process. In line with the social judgement theory Sherif & Hovland [1961] they assume that the degree of ego-involvement and self-relevance play a crucial role in social influence processes. In case of strong disagreement on a highly ego-involved issue (represented as an opinion dimension), individuals may increase their opinion difference on a less ego-involved issue (represented as another opinion dimension). This can occur in particular when issues are at stake that are central to the social identity of an individual. Building on research on intergroup dynamics Brewer [1991] Tajfel [1978], further models Salzarulo [2006] Dykstra et al. [2015] assume that individuals may change their opinion to adopt a position prototypical for their ingroup or to distance themselves from an opinion perceived as prototypical for an outgroup.

Typical macro behavior

2.52 Figure 1c describes a typical dynamic that has been generated with the model presented above. Starting from an opinion that is initially randomly uniformly distributed in the population, soon two clusters start to form at the opposite extremes of the spectrum, until eventually all agents have joined one of the two emergent factions. Due to their large distance from other members of the population, initial extremists “push” even moderate agents to differentiate from their extreme views and to thus shift towards the opposite pole. The assimilation pressures of positive influence then “pulls” their “moderate friends” with them in the process, adjusting their opinions towards increasingly extreme positions on the opinion scale. This class of models offers a possible
explanation of how bi-polarization can arise despite the presence of simultaneous assimilative influence, as well as how agents can adopt opinions that are more extreme than any of the initial opinions present in the population.

Alternative ways of modelling repulsive social influence

2.53 Like unconditional and similarity-biased influence, also repulsive influence has been implemented for both continuous as well as nominal opinion spaces.

2.54 Different implementations of the same principle were proposed for continuous opinions. For instance, some models (Jager & Ambilard 2005) introduce threshold levels for the difference between opinions that determine whether an interaction triggers assimilation (small differences), differentiation (large differences), or has no effect (intermediate range). These models exhibit opinion clustering, moderate and extreme consensus as well as bi-polarization.

2.55 Other models allow for smooth non-linear weight functions that approximate such threshold models (Mäs et al. 2014). Yet other modelers assume that the weight measures similarity across several opinion dimensions, including static attributes that represent demographic characteristics like gender or race (Feliciani et al. 2017 Flache & Mäs 2008a,b, Grow & Flache 2011, Macy et al. 2003). Depending on the parametrization and exact distribution of static attributes across the population, these models have been shown to generate opinion consensus on moderate opinions or bi-polarization or, sometimes, also fragmentation.

2.56 Among models that differentiate between multiple opinion dimensions, some distinguish between an opinion dimension concerning a primary topic (representing an important topic, associated with strong ego-involvement), and secondary opinion dimensions (Balassarri & Bearman 2007, Huet & Deffuant 2010, Huet et al. 2008). In such models, disagreement on the primary opinion dimension can trigger repulsive influence on the second dimension. These models display opinion clustering and polarization on at least one opinion dimension. This perspective draws on experimental research testing combined implications of social identity theory and cognitive dissonance theory (Wood et al. 1996), reflecting the view that “attitude shifts reflect normative pressures to align with valued groups and to differentiate from derogated groups” (Huet & Deffuant 2010 p. 2).

2.57 Historically, differentiation from dissimilar others was first included in models with nominal opinion spaces (Macy et al. 2003, Mark 2003). In these models, the similarity between two interacting agents determines the probability that they either copy a trait from an individual they interact with, or adopt a trait dissimilar from that of their interaction partner in order to increase difference. Like continuous models, nominal models show how repulsive influence can promote the self-organization of antagonistic factions in which opinion differences between groups align across multiple dimensions of an opinion space, maximizing intergroup differences.

2.58 Another variation of the idea of repulsive influence is that differentiation from a source of influence does not need to be caused by large dissimilarity, but could also result from high similarity. This idea was first implemented in models of majority influence in nominal opinion spaces (Galam 2004, Wio et al. 2006). Here, “contrarian” agents are introduced who after group discussion always deviate from the local majority that was adopted by other agents. These models show how the presence of contrarians can prevent the formation of a clear majority despite conformity pressure at the local level. Motivated by psychological research on nonconformity and uniqueness (Imhoff & Erb 2009, Snyder & Fromkin 2012), optimal distinctiveness theory (Brewer 1991) and Durkheim’s discussion of societal differentiation (Durkheim 1892 [1895]), some authors applied a similar idea for continuous opinion spaces (Mäs et al. 2010). They assumed that agents are simultaneously exposed to assimilative social influence and strive for uniqueness, trying to shift away from the majority opinion in their social environment when too many others adopt an opinion too similar to their own. Similar to the nominal models, they find that the combination of assimilation and strive for uniqueness can generate dynamically changing opinion clusters through a process of fusion (assimilation) and fission (splitting away of individuals from clusters if they become too big). Arguably, the combination of assimilative influence and differentiation from similar others offers a tentative answer to Durkheim's and Bourdieu's questions how some level of (local) consensus and global differentiation can co-exist in society despite tendencies towards both assimilation and individualization. The stronger social influence is relative to individualization in these models, the larger are the clusters that form and the less different are individuals’ opinions on average (Mäs et al. 2010, 2014).

Critical conditions and limitations

2.59 A core condition for bi-polarization identified by various models of repulsive influence is that in interpersonal interaction both assimilation and differentiation can occur. Assimilation occurs if agents are not too dissimilar
and differentiation happens if agents are not too similar. If this is the case, assimilative influence can lead to the emergence of factions with high levels of internal consensus among initially more similar agents, while differentiation can push these emergent factions to increasingly disagree with each other. In models with continuous opinion spaces, this can be related to the position of the threshold level of dissimilarity, above which influence turns repulsive \cite{Huet2008,Jager2005,Mas2014} – or the likelihood with which in an interaction between dissimilar agents differentiation occurs \cite{Chattoe-Brown2014} – compared to the threshold dissimilarity below which influence is assimilative. Broadly, if there is enough room for both assimilation and differentiation, bi-polarization is likely to occur, while consensus is likely to occur if interpersonal interactions result primarily in assimilation and not in differentiation. In a similar vein, repulsive influence models with nominal opinions identify “openness” to social pressures to both assimilate or differentiate \cite{Macy2003} as condition fostering bi-polarization.

2.60 The extent to which repulsive influence occurs in individual interactions also depends on macro-structural properties of the population that define how dissimilary are two interacting agents on average. One important condition here is the shape of the initial distribution of opinions. Broadly, more variance in agents’ opinions in the initial condition increases the chances that bi-polarization arises \cite{Mas2014}, because it increases the chances that agents interact who are dissimilar enough to influence each other negatively. Another, related condition is the dimensionality of the opinion space. In models with multi-dimensional opinion spaces, the dissimilarity between agents is often modelled as aggregated dissimilarity across all dimensions \cite{Flache2008,Macy2003}. If this is the case, more dimensions can decrease the likelihood that from a random start two agents who happen to interact will strongly disagree on most dimensions, which in turn makes bi-polarization a less likely outcome at the macro level. However, more complicated relationships between the number of opinion dimensions and bi-polarization arise when models differentiate between a primary and secondary opinion dimension, where the primary dimension mainly defines whether influence is assimilative or repulsive on both dimensions \cite{Huet2010}.

2.61 In addition, repulsive influence models appear to be sensitive to the network structure: networks with strong local clustering and small average distances between nodes (caveman graphs) display a strong polarizing tendency originating from long-range ties. These ties potentially connect highly dissimilar local regions in a network and thus can trigger repulsive influence \cite{Flache2011b}. Building on this finding, \cite{Feliciani2017} showed how under local interaction, spatial segregation between dissimilar groups can reduce bi-polarization dynamics, because segregation minimizes potentially repulsive influence encounters. Similarly, they found that interactions between random dyads in otherwise fixed, non-complete networks may exacerbate the polarizing tendency under certain conditions \cite{Feliciani2017}, because they increase the likelihood that demographically dissimilar actors interact.

2.62 Further research has investigated the effects of assuming multiple opinion dimensions \cite{Flache2011b} and a combination of opinion dimensions and fixed demographic attributes \cite{Flache2008,Macy2003}. On the one hand, fixed attributes allow to investigate the effects of demographic faultlines and of different distributions of influence thresholds across a population \cite{Grow2011}. On the other hand, they allow to model spatial segregation as exogenous condition \cite{Feliciani2017}. Both aspects have been shown to affect the system dynamics. Broadly, reflecting research on “demographic faultlines” in work teams \cite{Lau1998}, these studies found that the more the distribution of demographic attributes segregates a population into distinct subgroups, the more likely bi-polarization will be. An important further aspect in modelling the role of social categories is that different categories can have different relevance for the direction and magnitude of social influence. Drawing on self-categorization theory and social identity theory, some models assume that those categories central to a social identity can affect the direction of influence between individuals depending on their group membership \cite{Huet2010}, while similarity or dissimilarity on other categories may be of less relevance.

2.63 Models with repulsive influence provide a tentative answer to both Axelrod’s and Abelson’s questions. However, whether consensus, opinion clustering or bipolarization arises from their dynamics depends on a number of critical conditions including variance in the initial opinion distribution, the number of distinct dimensions of an opinion space, distribution of demographic attributes in a population and – importantly, whether agents differentiate from similar others (striving for uniqueness) or dissimilar others.

2.64 The main limitation we see at this moment for this class of models, however, is the lack of empirical work that convincingly demonstrates the micro process of repulsive social influence that is critical for the model’s behavior. While early social influence experiments \cite{Hovland1957} suggest a systematic tendency of individuals to differentiate from dissimilar or disliked sources of influence, many of these studies have been criticized for methodological weaknesses \cite{Mas2013}. More recent experiments that aim to avoid such weaknesses failed instead to find evidence that disliking or dissimilarity consistently triggers differentiation \cite{Takacs2017}.
Hybrid models and alternative models

2.65 The three classes we have described each cover a broad range of models proposed and analyzed in literatures about mathematical, socio-physical and agent-based models of social influence dynamics. Nonetheless, many other models remain that can not be readily assigned to any of these classes and that offer yet other possible answers to Axelrod’s and Abelson’s questions. It is impossible to do justice to all of this work in one overview paper. As a very coarse-grained categorization, one can distinguish hybrid models, combining assimilative influence, similarity biased influence and repulsive influence within one model, and models implementing alternative approaches to fundamental principles of social influence that do not fall into any of our three classes.

2.66 Many hybrid models have been proposed. Generally, it can be said that behavior of these models often can be well understood from combining the main conditions and mechanisms we identified for consensus, opinion clustering and bi-polarization in the three model classes. Examples can be found in models that combine bounded-confidence principles of similarity-biased influence with both assimilative and repulsive influence. For instance, the model proposed by [Huet & Deffuant 2010] that we discussed above combines bounded confidence dynamics driven by agreement on the main opinion dimension with positive or repulsive influence on the secondary dimension. Further hybrid models similarly combining similarity-biased influence and repulsive influence have been proposed for example by [Grow & Flache 2011], [Del Vicario et al. 2017] or [Duggins 2017]. In a similar vein, [Allahverdyan & Galstyan 2014] elaborated a model of opinion dynamics based on non-Bayesian probabilistic opinion revision in the evaluation of new information. Their model could reproduce empirically observed phenomena like confirmation bias, primacy-recency effect, boomerang effect or cognitive dissonance.

2.67 Next to hybrid models, a variety of models were proposed that draw on principles of social influence not covered by the three classes we discussed. One line of work are models drawing on persuasive argument theory (Myers 1982; Vinokur & Burnstein 1978), which assume that influence occurs through communication of arguments (Mäs et al. 2013; Mäs & Flache 2013). These models assume similarity biased influence in the sense that agents who are more similar interact more likely. But more similar agents also hold more likely arguments supporting the same opinion, such that the interaction between them strengthens their convictions and thus fosters extremization of their opinions towards the same pole of an opinion spectrum, a process that those models implementing social influence as averaging cannot generate (Mäs & Flache 2013). Interaction between dissimilar agents has the opposite effect, because arguments opposing the current tendency of an agent are learned in such an interaction and differences are thus reduced. The conditions under which these models generate consensus and bi-polarization overlap only partially with those known from similarity-biased or repulsive influence. In particular, bi-polarization becomes more likely when more similar agents interact in separate groups (see also Feliciani et al. 2017), a condition opposite to what models of repulsive influence suggest. Similar mechanisms with similar dynamics have also been proposed by models of selective exposure to different opinions in a multidimensional opinion space (Urbig & Malitz 2007) and models of “biased assimilation” (Dandekar et al. 2013), and information accumulation systems (Shin & Lorenz 2010).

Frontiers

3.1 Since Axelrod and Abelson formulated their research questions, a huge literature has emerged containing mathematical as well as computational agent-based models of social influence dynamics. Multiple possible answers to their questions can be derived from these models. However, we contend that the field faces at least two important challenges before formal models of social influence can be used to inform researchers aiming to understand and predict outcomes and processes as they can be observed in specific societal realms. Here, we discuss in turn the interrelated challenges of 1) theoretical integration and structuring of alternative models, and 2) empirical calibration and testing of model implications. More generally, we believe that for assessing the progress achieved in an ABM study of social influence, it is important to specify in advance whether the goal pursued is a theoretical one (e.g. comparison of implications of different models, exploring implications of a psychological process hitherto not addressed in social influence models) or whether the aim is to generate outcomes that

et al. 2016. While these results do not refute repulsive social influence, they highlight that conditions under which it occurs at the individual level may be more specific, requiring for example strong emotional content (Gargiulo & Huet 2012; Sobkowicz 2012, 2015), high ego-involvement, or strong antagonistic group identities (Huet & Deffuant 2010).

Frontiers

3.1 Since Axelrod and Abelson formulated their research questions, a huge literature has emerged containing mathematical as well as computational agent-based models of social influence dynamics. Multiple possible answers to their questions can be derived from these models. However, we contend that the field faces at least two important challenges before formal models of social influence can be used to inform researchers aiming to understand and predict outcomes and processes as they can be observed in specific societal realms. Here, we discuss in turn the interrelated challenges of 1) theoretical integration and structuring of alternative models, and 2) empirical calibration and testing of model implications. More generally, we believe that for assessing the progress achieved in an ABM study of social influence, it is important to specify in advance whether the goal pursued is a theoretical one (e.g. comparison of implications of different models, exploring implications of a psychological process hitherto not addressed in social influence models) or whether the aim is to generate outcomes that

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match empirical data observed in a specific realm. This defines how the researcher can assess whether and to what extent the aim of the modelling study has been achieved.

**Frontier 1: Theoretical questions**

3.2 A central problem of the literature on social-influence dynamics is that there are many models but little is known about their relation to each other. Many contributions fail to identify how they add to insights of earlier work. As a consequence, many publications contribute more to the accumulation of social-influence models than of scientific insight into social-influence processes.

3.3 In order to reduce the number of plausible models for a given setting and to allow the development of decisive empirical tests, modelers need to identify the critical assumptions and predictions of their models, and need to compare these assumptions as well as their formal implementation to existing models. Ironically, however, there seems to be too little influence between social-influence modelers to create the dynamic necessary to develop scholarly consensus on what are core model ingredients, in which implications models really differ and where they don't, and how models can be compared. In this section, we propose four directions for future theoretical work we believe is needed.

**Work that compares alternative technical implementations of the “same” theoretical assumption**

3.4 In Section 2 we argued that large parts of the literature can be categorized into three model classes, proposing that all models belonging to the same class share critical assumptions and key results. However, this does not imply that modelers can freely choose between models to generate whatever opinion dynamic one would like to have. Instead, modeling choices need to be made explicit, defended with theoretical and empirical arguments, and backed up with sensitivity analyses. For example, we argued that Axelrod’s model of cultural dissemination and bounded-confidence models implement – albeit in different ways – the theoretical principle of similarity-biased influence, with many similar answers emerging from seemingly very different models. While hundreds of papers work with these models, authors rarely discuss why they chose one of the two models and virtually never explore whether their conclusion might differ if they had chosen the alternative model. As a consequence, it remains unexplored whether findings hinge upon the technical differences, for example between continuous and nominal scaling of opinions, or generalize to the whole class of models and thus represent potentially more general insights. Thus, more work is needed to understand to what extent models belonging to the same class make the same predictions and whether (technical) differences between models also entail substantively different implications.

**Work that compares models with different theoretical approaches**

3.6 Our review of the literature demonstrates that models belonging to different classes employ critically different assumptions. Modelers should, therefore, provide convincing arguments for their choice of model ingredients, making explicit why or why not they assumed assimilative influence, similarity-biased or repulsive influence and why they chose a specific implementation. What is more, as similarity bias and repulsive influence can be critical assumptions, modelers should explore whether the results of their analysis hinge on their choice of assumptions. To be sure, similarity bias and repulsive influence do not always entail different model predictions. For instance, the conditions of bi-polarization proposed by some models from both classes are relatively similar. Especially for those models that link the possibility and direction of influence mainly to opinion disagreement, the higher are confidence thresholds or thresholds triggering repulsive influence, the more likely an opinion dynamics generates consensus. However, we emphasize that the fact that a given model assumption has critical impact on a theory’s prediction is not a weakness of the model. In contrast, testable hypotheses about the conditions under which similarity bias and repulsive influence lead to different predictions can guide empirical research and, thus, help identify the appropriate model for a given setting.

3.7 This also requires moving towards shared standards of how to make comparable the conditions (like thresholds triggering rejection of influence or repulsive influence) that are manipulated in computational experiments and
the model outcomes that should be compared (like bi-polarization), for example by drawing on recent advances in measuring and disentangling different aspects of bi-polarization in an opinion distribution (Bramson et al., 2016).

**Work that explores how different micro-level mechanisms can be derived from the same more fundamental principles under different conditions**

3.8 Often it is very important and leads to new insights if we open the “black box” of a model assumption and explicate in a “deeper” model the process that supposedly leads to the assumption. For example, if we just assume that more similar people influence each other more because they want to reduce cognitive dissonance, we may end up with different results than a model would generate in which we actually make the dissonance reduction mechanism explicit and then study under what conditions it produces our initial assumption (e.g. Groeber et al., 2014).

3.9 A more general question is which processes of social influence follow under which conditions from fundamental principles of human cognition. Rosaria Conte and her co-authors have repeatedly and forcefully argued for the importance of this question. They call for an integrated approach in ABM that links the social structure in which an individual is embedded to a model of its cognitive, “symbolic representations and the operations performed upon them, involved in mental activities including understanding, problem-solving, (social) reasoning and planning, communicating, interacting and [. . .] learning” (Conte & Castelfranchi, 1995, p. 1). This approach has been applied to dynamics akin to social influence, like the spreading of gossip or the formation of opinions about actors’ reputation in a population (e.g. Conte & Paolucci, 2002). Recently, first steps have been taken to link this approach to models of social influence with the development of “a cognitively grounded computational model of opinions in which they are described as mental representations and defined in terms of distinctive mental features” (Giardini et al., 2015).

**Frontier 2: Empirical questions**

3.10 The question which of the many available models of social influence is the best choice for studying a given empirical phenomenon is eventually an empirical one, given that the researcher can narrow down the empirical scope that a model addresses. Thus, while answers to the described theoretical research questions are vital to develop informative empirical studies, the assumptions and predictions of theoretical models need to be put to the empirical test. This also requires that researchers specify the empirical scope their model addresses, that is: under which empirical conditions the assumptions used in a model are expected to be valid and which empirical phenomena at macro-level the model should be able to “grow”.

3.11 Unfortunately, the assumptions of social-influence models, the dynamics that they generate, and also many of their predictions are notoriously difficult to put to the test. In the following, we outline 4 approaches to testing models of social influence that we deem promising.

**Validation and calibration of micro assumptions with experiments**

3.12 Our review of the literature has illustrated that micro-level assumptions in models of social influence dynamics often have been derived from theories based on social-psychological research, many based on experiments into social influence, conformity or small group decision making conducted in the 1950s and 1960s, notwithstanding some more recent work (e.g. Bohner & Dickel, 2011). While these studies have revealed much insights into determinants of assimilative influence, similarity-bias or repulsive influence in social interactions, basic empirical questions about how to underpin model assumptions remain unanswered. For instance, while social influence has been documented many times, little is known about the conditions under which influence is stronger or weaker. Are individuals equally open to influence on their beliefs, opinion, and behavior? How flexibly do individuals adjust their opinions in a given time frame and do opinion adjustments after social influence remain effective also in the long run? Modelers’ decisions to either adopt or reject certain assumptions can have decisive effects on model behavior, but the empirical literature on social influence is still too limited to validate social-influence models at the level of precision needed for empirically informed choices between model alternatives.

3.13 Furthermore, even some of the most important assumptions of existing models have hardly been tested. For instance, the predictions of bounded-confidence models depend critically on the position of the confidence
thresholds beyond which individuals are not influenced. Likewise, whether repulsive influence alters opinion dynamics depends on how much opinion divergence between two individuals is required to trigger repulsive influence. To our knowledge, however, there is no research quantifying these thresholds and their distributions in a population. There is also relatively little research yet directly testing the psychological and structural conditions under which confidence thresholds or repulsive-influence thresholds shift (for some exceptions see Chacoma & Zanette 2015, Mavrodiev et al. 2013, Moussaid et al. 2013). Furthermore, modeling work has demonstrated that the predictions of bounded-confidence models can change when actors sometimes deviate from the bounded-confidence assumption, even when deviations are rare and random (Kurahashi-Nakamura et al. 2016, Mäs et al. 2010, Pineda et al. 2009). There is, however, no empirical research on the frequency and nature of these deviations. While it is not necessarily the task of agent-based modellers to conduct themselves experimental studies that allow better testing and calibration of micro-level assumptions, it is important that model-builders carefully scrutinize available evidence and seek collaboration with empirical researchers where possible, in order to improve the match of empirical evidence with model assumptions.

3.14 Assessing model assumptions at the level of precision needed to inform agent-based models requires experiments that systematically vary the degree of dissimilarity between opinions and source, experimentally or statistically controlling for many other potential sources of opinion change such as learning effects, or individual differences in attractiveness, persuasiveness or salience for an issue. In the tradition of Friedkin and Johnsen’s seminal work (Friedkin & Johnsen 2011), recently laboratory experiments have become available that are designed with the goal of testing assumptions of social-influence models (Chacoma & Zanette 2015, Vande Kerckhove et al. 2016, Mavrodiev et al. 2013, Moussaid et al. 2013). While results of some of these experiments lend some support to assumptions of bounded confidence models, other studies (Takács et al. 2016) find support only for assimilative influence and not for similarity-biased or repulsive influence. Clearly, more experimental research is needed that tests social influence mechanisms in the way they are quantitatively formalized in models of social influence dynamics.

**Indirect tests of micro-models with experiments**

3.15 A fundamental problem of the empirical approach discussed in the previous section is that the assumptions of social-influence models are often hard to put to the test. A key bottleneck is that opinions are latent constructs and, thus, difficult to quantify with the precision assumed in the formal models. Standard opinion measures apply survey methods that provide measures on ordinal scales, making it impossible to directly test key model assumptions, such as the width of confidence intervals for BC models or the opinion distance between two individuals that sparks repulsive influence.

3.16 A powerful approach to indirectly test model assumptions is to create laboratory settings for which alternative models of social influence make clearly distinct predictions about the collective outcomes of social-influence dynamics. For instance, Flache & Mäs 2008a, Mäs & Flache 2013 demonstrated that models make opposite predictions about the effects of the timing of contacts. According to models of assimilative social influence, the outcome of influence dynamics hardly depend on who is when interacting with whom. In a model with repulsive influence, in contrast, opinion bi-polarization is likely to obtain when individuals are first exposed to social influence from dissimilar sources and only later experience influence from similar actors, because repulsive influence will intensify opinion differences in the first phase. In the reversed scenario, however, influence between similar actors in the first phase will decrease opinion differences in the population and, thus, decrease chances that actors will influence each other negatively when they interact with others who held divergent views at the outset. Finding empirical support for the prediction that the timing of contacts matters in the described way, would provide indirect support for the repulsive influence assumption. Furthermore, the timing-of-contacts prediction also allows the exploration of the conditions of repulsive influence. One could test, for instance, whether the timing-of-contacts effect is stronger when the issue at stake is highly emotional or when influence dynamics act in tandem with processes of group identification.

**Testing micro-models with survey data**

3.17 Surveys are the workhorse of much social-scientific research on beliefs, opinions, and behavior. While survey studies have been conducted to test assumptions about opinion changes in public debate over time (e.g. Krosnick et al. 2000), it remains challenging to link such results to the micro-assumptions about social influence in agent-based models. A central disadvantage of many survey studies is that they are based on random or quasi-random sampling, a method designed to test hypotheses about the distribution of individual characteristics and the statistical relationships between them. The challenge to using this data for the study of social influence

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is that influence processes can amplify relationships between individual characteristics. For instance, a causal relationship between individuals’ educational level and their political opinions is intensified when individuals with similar educational levels tend to interact more (homophily), and therefore tend to be socially influenced by others with similar education. As a consequence, relatively small statistical relationships resulting from a causal relation between educational level and political opinion can be largely exaggerated in survey data [Del- laPosta et al. 2015]. This may mislead research into attributing strong observed associations to causal effects of individual attributes, while actually the main driving force is social influence.

3.18 Uncovering the impact of social influence on statistical relationships with random samples is challenging because the statistical analysis of random samples requires the assumption that observations are independent, which contradicts the assumption of social influence. To be sure, it is not impossible to study social influence with random samples. For instance, Opp and Gern found that during the revolution in East Germany survey respondents who reported that their friends and family were politically active participated more in the protests [1993]. However, in order to put to the test the critical assumptions of similarity biased or repulsive influence, survey respondents would need to be able to reliably quantify the opinions of their potentially influential contacts, which appears impossible with existing survey methods.

3.19 A promising development for empirically testing micro-assumptions of social influence models in field settings is the increasing availability of longitudinal datasets that combine the dynamics of social networks as well as of opinions in complete social networks, like in school classes [Stark & Flache 2012] or workplaces [Ellwardt et al. 2012]. Rather than drawing random samples in big populations, these studies assess complete social networks in relatively small populations. Recent developments in statistical methodologies have made it possible to utilize such data. Stochastic actor oriented models developed by Snijders and others [Snijders 2011; Snijders & Steglich 2015; Steglich et al. 2010] combine agent-based modeling of such longitudinal data with statistical estimation and testing of the mechanisms assumed by the modeler. Broadly, the statistical method selects the parameters for the effects (e.g. ethnic homophily and assimilative opinion influence) specified by the modeler by simulating the distribution of the networks and actor attributes for a range of selected parameter values. The program then selects the set of parameters for which the simulation yields the best match with the observed dynamics of network and behavior, allowing statistical inference to estimate parameter values from the data. Applications of this approach allow to disentangle mechanisms of social selection, like homophily based on opinions or ethnicity [Stark & Flache 2012], from processes of social influence. Yet, while many studies using this paradigm have documented social influence, future research is needed to test more specific assumptions about social influence that allow assessing and distinguishing assimilative, similarity-biased or repulsive influence, and how the degree to which such processes occur in microlevel interactions relates to macro-structural properties of emergent network structures [Snijders & Steglich 2015] and opinion distributions.

Testing macro-predictions

3.20 A key question is whether and to what extent the structural conditions predicted by the models can explain differences in diversity or polarization at the macro-level (e.g. between countries). Large scale social surveys as the European Social Survey, the World/European Values Survey and others provide a source of validation and further improvement of social influence models (e.g. Brousmiche et al. 2016; Chattoe-Brown 2014). Such surveys repeatedly (e.g. every couple of years) ask a representative sample of the populations in several countries to report opinions and attitudes to the same or similar standard questions which are often measured on a relatively fine-grained “quasi-continuous” scale (e.g. 0 → 10). This does not provide us with data of opinion change on the individual level, but it shows macroscopic opinion landscapes as demonstrated in Figure 3 for the political left-right self-placement (and opinion about European integration) in France (and other countries) from the European Social Survey 2012.

3.21 All these opinion landscapes do neither look exactly as stylized outcomes of the simple versions from our core model, nor do they show a simple shape like a normal or Beta-distribution. Yet, these data can be seen as some evidence for the main characteristics of all the three core mechanisms of social influence dynamics discussed above:

- A strong dominant central peak in all landscapes suggests some assimilation towards the moderate or central opinion in a population.
- A tendency for off-central but non-extreme clusters – usually on both sides of the central cluster – is consistent with the clustering generated by social influence processes with similarity bias.
- Extremal peaks, typically on both extreme ends of the spectrum, resemble the bi-polarization generated by a mix of assimilative and repulsive processes. However, such peaks might also be explained by an
The fact that clusters are not perfectly separated can be explained relatively well by noise in the form of a small influx of fresh opinions through turnover or reconsideration of opinions through processes independent from social influence as modeled by random draws as the initial distribution (see Pineda et al. 2009). Nevertheless, it is not possible to model such landscapes with the bounded confidence model and noise alone (Lorenz 2017).

Analysis and characterization of such opinion landscapes can be a route to data-driven modeling of more realistic and more predictive models of social influence using the knowledge gained by a deeper understanding of the mechanisms presented here. Calibrating models to resemble patterns observed in opinion surveys will be most fruitful if agent-based modelers at the same time assess to what extent those models that best fit macro-level patterns also contain assumptions that are compatible with empirical evidence available about micro-level processes of social influences and meso-structural conditions (e.g. structures of social networks).

As we argued above, micro level evidence that can narrow down the set of models suitable to match opinion distributions observed in surveys can be obtained from experimental studies or studies of the co-evolution of networks and opinions in longitudinal data. Further empirical sources can be used to calibrate assumptions models make about meso-level structures. For example, structural features of social networks in a population at large can be assessed from increasingly available data sets of online networks (Eagle et al. 2010) or global network indicators measured in surveys (DiPrete et al. 2011).

**Conclusion**

While scholars agree that social influence is a strong force in social interaction, our review of the literature documented considerable variation across approaches on how to formally capture social influence on the micro-level, as well as about the macro-consequences arising from repeated social influence in networks. Nevertheless, we argued that a large part of the literature can be categorized into three classes of formal models, each of...
which is described by certain crucial assumptions about social influence on the micro level and characteristic predictions about emergent macro-dynamics.

4.2 Our review could not do justice to every contribution to the literature, but we believe our classification can serve as a general guideline for the development and communication of social-influence models. As important predictions generated by models belonging to each of the three classes are well understood, contributions based on a model falling into one of the three categories should make explicit the commonalities with existing models. Readers should also be provided with theoretical and empirical arguments for the choice of a given model class. Furthermore, contributions to the literature that do not belong to one of the three classes should discuss where the proposed model deviates from the assumptions defining the three classes and why this deviation was included. Ideally, it would also be tested whether and under what conditions the deviation from the three classes is responsible for new predictions about macro outcomes.

4.3 In the second part of the present paper, we identified two main frontiers in the literature on social-influence models. We argued that the field of social-influence modeling profits from a rich arsenal of theoretical models, but also suffers from a lack of systematic comparison of competing models. Likewise, resonating earlier calls for closer interaction between social scientists and model-builders (Sobkowicz2009), we conclude that there is a need for more empirical research testing micro-level assumptions, as well as macro-level predictions, and for a better link of both to model results.

4.4 Progress on both frontiers is urgently needed if modelers want to make use of the potential of social-influence models to inform public debate and decision-making about policies. Various promising developments in the literature highlight this potential. For instance, models extending the approaches discussed here have been calibrated and validated to study dynamics of citizens’ opinions about the conflicting forces in the Afghan civil war (Brousmiche et al.20162017). Similarly, an increasing number of agent-based social influence models aim to explain changes in the distribution of political opinions in western societies based on partially calibrated micromodels of social influence (Chattoe-Brown2014Duggins2017). Similar efforts address effects of agri-environmental policies on the spreading of environmentally friendly measures among farmers (Defuaut et al., 2008). As a last example, models that incorporate social-influence dynamics as one part of the process of strategic decision-making in political contexts have been calibrated to detailed data about specific policy-domains and were successfully applied in modelling outcomes in areas such as climate-treaty negotiations (Stokman et al.2013).

4.5 These examples of efforts to link agent-based models of social influence to concrete societal realms are encouraging, but too often the literature on social-influence dynamics leaves us with great uncertainty about the causes and consequences of important societal dynamics. For instance, while there is no doubt that globalization and technological advances such as the Internet have changed how and with whom people communicate, agent-based modelers have only just begun to use models of social influence to address the question how this will affect societal processes of collective decision making and opinion polarization (see e.g. Del Vicario et al.2017). Based on models of social-influence, some warn that the personalization of Internet services can contribute to processes of opinion polarization (Dandekar et al.2013Mäs & Bischofberger2015). Personalization algorithms tailor online services to the preferences and interests of each individual user, increasingly exposing them to other users advocating views and ideas that support their opinions. Being socially influenced, it has been argued, Internet users’ opinions are reinforced, a process that can aggregate to polarized opinion distributions. While this prediction has been demonstrated to be in line with some models of social influence, it is also in clear contrast to the predictions of other models – in particular models with repulsive influence. Repulsive influence fosters opinion polarization when actors with opposing opinions interact. Such encounters, however, are rare if the web is personalized, which would lead to less rather than more opinion polarization (Mäs & Bischofberger2015) according to these models.

4.6 Effects of the Internet on public debate is but one area in which different social influence models entail radically different predictions. This illustrates that based on the current state-of-the-art in the field, it remains difficult to explain and predict outcomes of social influence processes shaping concrete societal dynamics. This highlights the need to move further ahead in integrating, calibrating and testing models. The tools in the toolbox of agent-based modelers on the one hand and of empirical social scientists on the other hand, offer perspectives to successfully address these problems. A marriage between their approaches is not only possible, but also urgently needed. We are convinced that this marriage will lead to deeper insights than each of the partners could obtain without the other one.
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Notes

1In addition we assumed for Figure a population of $N = 100$ agents, initial opinions were drawn randomly from a uniform distribution and weights were homogeneous with $w_{ij} = 1/n$ for all $i, j$.

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