A new study of stellar substructures in the Fornax dwarf spheroidal galaxy

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Received 5 December 2012 / Accepted 15 January 2013

ABSTRACT

Using deep V, B – V wide-field photometry, we have conducted a new study of stellar over-densities in the Fornax dwarf spheroidal galaxy by determining detailed star formation histories from colour–magnitude diagram analysis. We have concentrated on the relatively young stellar component (<4 Gyr old), and compared this to the underlying Fornax field population.

We have studied in more detail the previously known inner shell-like structure and shown that it has a well-defined age-metallicity relation with a peak at ≈1.5 Gyr, [Fe/H] = −0.6 dex. Comparison to the Fornax centre shows that the over-dense feature is consistent with the age-metallicity relation of young field stars, and likely formed from Fornax gas. This is consistent with a scenario in which the over-density was formed by the re-accretion of previously expelled gas.

We have also discovered a new stellar over-density, located 0.3 degrees (0.7 kpc) from the centre, which is only 100 Myr old, with solar metallicity. This feature constitutes some of the youngest, most metal-rich stars observed in Fornax to date. It is unclear how the young over-density was formed, although the age and metallicity of stars suggest this feature may represent the last star formation activity of the Fornax dSph.

Key words. galaxies: stellar content – galaxies: evolution – Local Group – Hertzsprung-Russell and C-M diagrams

1. Introduction

The Fornax dwarf spheroidal galaxy (dSph) has experienced an unusually complex star formation history (SFH), with stellar populations covering a large range in age and metallicity (e.g., Gallart et al. 2005; Coleman & de Jong 2008; de Boer et al. 2012b). Spectroscopic studies of red giant branch (RGB) stars have found the metallicity distribution function (MDF) to have a broad distribution with a dominant metal-rich ([Fe/H] ≈ −0.9 dex) component (e.g., Pont et al. 2004; Battaglia et al. 2006; Letarte et al. 2010). The kinematics of these RGB stars have shown the presence of at least three kinematically distinct populations (Battaglia et al. 2006; Amorisco & Evans 2012). Analysis of the stellar spatial distribution shows that Fornax contains a radial population gradient, in which younger, more metal-rich stars are found progressively more towards the centre (Battaglia et al. 2006; Coleman & de Jong 2008; de Boer et al. 2012b).

Wide-field photometric surveys of Fornax have previously found two young stellar over-densities, which have been interpreted as shell-like features resulting from the in-fall of a smaller system less than ≈2 Gyr ago (Coleman et al. 2004, 2005b; Olszewski et al. 2006). The inner feature is located at a distance of ≈17 arcmin (0.7 kpc) from the centre of Fornax, while the outer feature is located outside the tidal radius at a distance of 1.3 degrees (3 kpc) from the centre. Isochrone fitting to the observed colour magnitude diagram (CMD) determined that the main population of both over-densities formed less than 2 Gyr ago (Coleman et al. 2005b; Olszewski et al. 2006). Metallicities determined from the CMD suggest that the stellar populations of the inner feature are similar to the young stars of the Fornax field stars, indicating a connection between both components (Olszewski et al. 2006).

It is still unclear what has driven the complex evolution history of Fornax. Models predicting the formation of Fornax have tried to explain the spatial complexity and extended, multiple episodes of star formation using tidal encounters with the Milky Way, or re-accretion of expelled gas (e.g., Pasteto et al. 2011; Nichols et al. 2012; Yozin & Bekki 2012). Models involving accretion events are especially relevant, given the presence of these shell-like structures in and around Fornax.

If the over-dense features were the result of an in-fall event, it is likely that the interaction had an effect on the populations of the over-density and the Fornax field. Therefore, the detailed properties of the stellar populations in the over-densities can be used to constrain the nature of the in-falling system. If the in-falling system was a small gas-rich galaxy, the over-densities will contain a mix of populations made up of stars already present in the accreted galaxy and new populations produced as a result of the interaction. Since smaller galaxies are usually metal-poor, and young stellar populations are intrinsically blue, the over-density should contain populations different from the host galaxy onto which it is accreted (Pence 1986; McGaugh & Bothun 1990).

If the over-dense features were created by the accretion of a gas cloud onto the host galaxy, the stellar population properties will depend on the metallicity of the in-falling gas. The in-fall of...
a cloud of pristine gas would result in an over-density containing metal-poor, blue populations while the re-accretion of previously enriched gas would lead to redder populations. Finally, if the features are part of the standard Fornax field population, the stellar populations would match the age-metallicity relation (AMR) of the Fornax field stars (de Boer et al. 2012b).

In this paper we use the photometric dataset presented in de Boer et al. (2012b) to study the known over-density and search for new features in the spatial distribution of young stars in Fornax. The deep CMDs of the stellar over-densities were analysed using the technique described in de Boer et al. (2012a), to determine the ages and metallicities of the over-dense populations and obtain their AMR. By comparing the AMR of the over-densities to the Fornax field, we can constrain the likely nature and origin of the over-dense features and their role in the formation of Fornax.

The paper is structured as follows: in Sect. 2 we analyse the photometric dataset to search for photometric over-densities in the young stars of Fornax. In Sect. 3 we present the CMDs for the over-densities and their associated field component. Section 4 presents the SFH results for the over-densities, which are compared to the Fornax centre in Sect. 5. Finally, Sect. 6 discusses the possible formation scenarios for the over-densities and their effect on the formation and evolution of the Fornax dSph.

2. Over-density selection

We used the wide-field photometric survey of the Fornax dSph described in detail in de Boer et al. (2012b) to investigate the presence of young stellar over-densities in Fornax. This survey consisted of deep optical photometry obtained using the CTIO 4-m MOSAIC II camera, covering a large part of the galaxy in the $B, V$ and $I$ filters. The photometric catalogue is complete out to elliptical radius $r_{25} \leq 0.8$ degrees for the $B$ and $V$ filters, while the $I$ filter is complete only for $r_{25} \leq 0.4$ degrees. The elliptical radius is defined as the major axis length of an ellipse centred on Fornax with structural parameters according to Irwin & Hatzidimitriou (1995).

To select young over-densities in Fornax, we investigate the spatial distribution of young main sequence (MS) stars on the blue plume (BP), which stand out against the predominantly older RGB field population (see Fig. 1). These stars are selected from the CMD, with the area corresponding to the blue horizontal branch removed to avoid contaminating the young sample with old, metal-poor stars. Figure 2a shows the resulting spatial Hess-like diagram of young MS stars in Fornax, obtained by binning the spatial coordinates of each star. The young population is distributed in a nearly horizontal structure with two main over-dense regions, one of which is located very close to the position of Fix 4 (Mackey & Gilmore 2003). This is clearly different from the intermediate and old populations, which are distributed in an ellipse with position angle of 46.8 degrees (Stetson et al. 1998; Saviane et al. 2000; Battaglia et al. 2006).

The over-density discovered by Coleman et al. (2004) is clearly visible in Fig. 2a, at $\xi \approx 0.13$ deg, $\eta \approx 0.2$ deg. The position and alignment of the feature is consistent with the parameters given by Coleman et al. (2004). The current spatial coverage of our deep photometry is not enough to be able to see the outermost feature, located outside the tidal radius of Fornax at a distance of 1.3 degrees from the centre (Coleman et al. 2005a). However, another over-dense feature stands out clearly in the spatial distribution of young stars, East of the Fornax centre, at $\xi = 0.24$ deg, $\eta = 0.06$ deg (RA = 02h:41m:02.2s, Dec = $-34^\circ:27^\prime:17.6^\prime\prime$). This feature is located at a distance of 0.3 degrees, or 0.7 kpc from the centre of Fornax.

Figure 2b shows a zoom in of the distribution of young stars in the inner region of Fornax, where both over-densities are clearly visible. The sample of stars adopted for the known over-density is selected according to the structural properties derived by Coleman et al. (2004). For the new over-density we adopt a rectangular region with dimensions of 1.77 x 3.67 at a position angle of $PA = 36$ deg.

The reason why the new over-density was not found in previous Fornax surveys is mainly due to the photometric depth and available filters. Most surveys (e.g., Eskridge 1988a,b; Irwin & Hatzidimitriou 1995; Walcher et al. 2003; Coleman et al. 2005b) did not extend deep enough or were not able to make a colour selection to obtain a clean sample of young stars, which dominate the young over-density. The survey by Olszewski et al. (2006) did go deep enough, but did not cover the region of the new over-density.

2.1. Fornax field star contamination

Due to the position of the over-densities within Fornax, it is likely that the CMD of each feature is contaminated by stars belonging to the Fornax field. To determine an accurate SFH for the over-density, it is necessary to account for this contamination. Given the fact that the Fornax dSph displays different stellar populations at different elliptical radii (de Boer et al. 2012b), we determine the field star contribution by only taking into account stars with the same range of elliptical radii as the studied region. With this annulus, we select only stars located far from the over-density (more than twice the extent). The selected region is expanded until it contains a sufficient number of stars to properly sample the CMD (typically 1–2 times the number of stars in the over-density). Finally, the number of stars is scaled to the same spatial area as the studied over-density, to construct a CMD representative of the Fornax field population.

3. Colour–magnitude diagrams

Using the regions selected in Sect. 2, we construct the CMD of each over-density and compare it to the CMD of the associated Fornax field star contribution. Figure 3 shows the observed CMD for the two over-densities in the form of Hess
Fig. 2. (a) Spatial Hess–like diagram of BP stars in the Fornax dSph. The two dashed circles indicate the position of two over-densities, one known and one new. (b) The spatial distribution of BP stars in the region corresponding to both detected over-densities. Dashed (black) boxes indicate the area selected for each over-density. The (green) ellipse shows the annulus corresponding to a radius of $r_{\text{ell}} = 0.3$ degrees from the centre of Fornax, assuming the structural parameters from Irwin & Hatzidimitriou (1995).

Fig. 3. Hess diagram of (a) the known over-density found by Coleman et al. (2004) and (b) the new over-density. Three isochrones are overlaid, representative of the populations traced by the Fornax field RGB (blue and red), as well as the over-dense population in the both features (black, dashed). The range of older field populations is traced by a metal-rich ($[\text{Fe}/\text{H}] = -1.00$ dex, $[\alpha/\text{Fe}] = 0.00$ dex, age = 4 Gyr, red) and metal-poor ($[\text{Fe}/\text{H}] = -2.45$ dex, $[\alpha/\text{Fe}] = 0.40$ dex, age = 14 Gyr, blue) isochrone. Parameters of the overlaid isochrone of the over-dense population are $[\text{Fe}/\text{H}] = -0.60$ dex, $[\alpha/\text{Fe}] = 0.00$ dex, age = 1.5 Gyr in panel (a) and $[\text{Fe}/\text{H}] = 0.00$ dex, $[\alpha/\text{Fe}] = 0.00$ dex, age = 0.2 Gyr in panel (b).

Fig. 4. Hess diagrams of the Fornax field star contribution associated to (a) the known over-density and (b) the new over-density. The same three isochrones as described in Fig. 3 are overlaid on the Hess diagram, representative of the main populations traced by the average Fornax field, and over-dense populations.

diagrams (a CMD density plot). The Hess diagrams are overlaid with isochrones from the Yonsei-Yale isochrone set (Yi et al. 2001), representative of intermediate and old Fornax field RGB populations ($[\text{Fe}/\text{H}] = -1.00$ dex, $[\alpha/\text{Fe}] = 0.00$ dex, age = 4.0 Gyr and $[\text{Fe}/\text{H}] = -2.50$ dex, $[\alpha/\text{Fe}] = 0.40$ dex, age = 14.0 Gyr respectively). A reference isochrone indicating the position of the main over-dense population is also shown. The observed Hess diagram consists of a combination of stars from the over-dense populations and from the Fornax field. The Fornax field star contribution associated to each over-density is shown in Fig. 4, scaled to the same spatial area as the observed sample.

The CMD in Fig. 3a shows several features similar to those of the Fornax field, such as a broad, metal-rich RGB (traced by the red isochrone), a thin red horizontal branch and prominent red clump. Figure 3a also shows a prominent young MS population (black, dashed line), with a broad, well developed turn-off around $V \approx 22.5$. This feature is only weakly visible in
the Fornax field (Fig. 4), while the number of intermediate and old RGB stars in both CMDs is comparable. Comparison to the reference isochrone (black, dashed line) in Fig. 3a shows that the young population is consistent with an age of ≈1.5 Gyr (Olszewski et al. 2006).

The CMD of the new over-density (Fig. 3b) is also dominated by stars from the Fornax field, as shown in Fig. 4b. However, a very young, blue MS population is also visible, blueward of the main Fornax MSTO at \( B - V = 0.2 \). This feature is not reproduced in the field star contribution, and is responsible for the clear over-density in Fig. 2a. The young MS extends from the Fornax field MSTO at \( V = 23.5 \) up to \( V = 19.5 \), containing 80 stars with \( V \leq 23.5, B - V \leq 0.2 \) (compared to 18 in the associated Fornax field). Comparison to stellar evolution models shows that this young MS is consistent with an age of 0.2 Gyr (black, dashed line). This is substantially younger than the populations found in the known over-densities, and constitutes some of the youngest star formation in the Fornax dSph.

4. Star formation history

The SFH of the young over-densities is determined using the SFH fitting method Talos, described in detail in de Boer et al. (2012a). For both over-densities, the distance modulus \([m - M_V = 20.84]\) and extinction value \( E(B - V) = 0.03 \) is assumed to be the same as for the Fornax field stars (Schlegel et al. 1998; Pietrzyński et al. 2009). Given the young ages expected for stars in the substructures, we adopt the Yonsei-Yale isochrone set (Yi et al. 2001) in the SFH fitting, since it includes isochrones with ages going down to 1 Myr and a broad metallicity range. For the SFH solution, metallicities are allowed to range from \(-2.5 \leq [\text{Fe}/H] \leq +0.3 \) dex with a spacing of 0.2 dex, for ages between 0.1 and 14 Gyr with a spacing of 0.1 Gyr between 0.1–2 Gyr, 0.5 Gyr between 2–6 Gyr and 1 Gyr between 6–14 Gyr. The fitting procedure results in a 2D solution giving the star formation rate (SFR) for each age and metallicity. By projecting this solution onto the age axis we obtain the SFH, while a projection onto the metallicity axis gives the chemical evolution history (CEH).

Figure 5 shows the SFH and CEH obtained for the known over-density discussed in Sect. 2. The SFH of the associated Fornax field contribution is also shown for comparison in Fig. 5b. The SFH shows a peak at old (≥10 Gyr) ages and a well-developed AMR at younger (≤6 Gyr) ages. The young populations in Figs. 5 show increased star formation at age ≈3 Gyr, [Fe/H] = −1.0 dex and a strong peak at age ≈1.5 Gyr with [Fe/H] ≈ −0.6 dex.

The star formation episode at [Fe/H] = −1.0 dex, age ≈ 3 Gyr is consistent with the main metal-rich RGB of the Fornax field (see Fig. 3) and is recovered in both the over-density and associated field contribution. The younger peak at [Fe/H] = −0.6 dex, age 1.5 Gyr is only weakly reproduced in the Fornax field contribution. This population is clearly responsible for the stellar over-density observed in Fig. 2, showing parameters in excellent agreement with results from isochrone fitting of the observed CMD (Olszewski et al. 2006). Figure 5c further shows that the SFRs at old (≥10 Gyr) ages are consistent with those in the Fornax field at similar elliptical radii (blue,
dashed histogram) within the errorbars. This indicates that the over-density is formed purely by an excess of young, metal-rich stars without increased numbers of older stars, as suggested earlier by Oliszewski et al. (2006).

To calculate the total over-dense mass of stars in the young over-density, we consider only stars younger than 2.5 Gyr and multiply the SFR in each population bin by the duration in age. This gives a total mass in young stars of $5.75 \pm 1.31 \times 10^5 M_\odot$ for the over-density and $1.27 \pm 0.65 \times 10^4 M_\odot$ for the associated Fornax field contribution. Subtracting the field star contribution gives a total over-dense mass of $4.47 \pm 1.46 \times 10^4 M_\odot$ formed within a mass range of $0.1-120 M_\odot$, assuming a Kroupa initial mass function. Compared to the stellar mass at all ages ($9.92 \pm 2.08 \times 10^4 M_\odot$), the young populations account for $\approx 45$ percent of the total stellar mass formed within the region selected in Sect. 2.

Figure 6 shows the full SFH solution of the newly discovered young over-density. The young over-density displays populations with a slowly increasing metallicity for younger ages. The AMR shows continuous evolution up to [Fe/H] $\approx -0.9$ dex, age $\approx 3$ Gyr, with later star formation episodes at [Fe/H] $=-0.7$ dex, age $\approx 2$ Gyr and [Fe/H] $=0.0$ dex, age $\approx 200$ Myr. The peak at [Fe/H] $=-0.7$ dex displays similar parameters as the main peak in the known over-density, suggesting a possible connection between both features. However, the peak in the young over-density is shifted to slightly older ages as observed in Fig. 5. The SFH solution of the Fornax field (top, right panel in Fig. 6) shows a similar AMR as the young over-density, except for the peak at the youngest age. This is also visible in the bottom panels of Fig. 6, which show that the SFH and CEH of stars with age $\geq 1$ Gyr are reproduced by the field star contribution, within the errorbars. The SFH shows that the population responsible for the over-density in Fig. 2 is clearly extremely young, with ages between 100–300 Myr and metallicities up to [Fe/H] $\approx 0.0$ dex.

For the total over-dense mass in stars we consider only stars with ages $\leq 1$ Gyr and compute a total mass in young stars of $1.56 \pm 0.41 \times 10^5 M_\odot$ within the over-density, and $0.30 \pm 0.14 \times 10^4 M_\odot$ within the Fornax field. Relative to the Fornax field contribution, the young over-density formed a total mass of $1.26 \pm 0.43 \times 10^4 M_\odot$ in stars during the last Gyr, within an area of $\approx 6$ arcmin$^2$. This corresponds to $\approx 10$ percent of the total stellar mass of $1.32 \pm 0.37 \times 10^5 M_\odot$ in Fig. 6a.

5. Comparison to the Fornax centre
The youngest populations of the Fornax field have sofar been found in the centre of the galaxy (e.g., Gallart et al. 2005; Coleman & de Jong 2008; de Boer et al. 2012b). If the observed stellar over-densities were created by the accretion of a gas-rich companion (Coleman et al. 2004), the in-fall event likely triggered the young star formation in the central regions. This would lead to the presence of similar stellar populations in the over-densities and the Fornax centre. Furthermore, by comparing the properties of both components, we can determine if the stars in the over-densities match the enrichment history of the Fornax dSph, indicating that they were formed from Fornax gas.

To determine if the populations of the stellar over-densities match those of the youngest Fornax field populations, we compare them to the stellar population properties of the stars within the innermost annulus considered in de Boer et al. (2012b). We re-determine the SFH using the same method and parameter spacing as adopted for the over-densities (see Sect. 4), and scale the solution to the same spatial area as the known over-density to allow a quantitative comparison. Figure 7 shows the
resulting SFH of the Fornax centre in comparison to the stellar over-densities, for ages younger than 5 Gyr.

The centre of Fornax shows a narrow AMR at older ages, from $[\text{Fe/H}] = -1.3$, age $= 5$ Gyr down to $[\text{Fe/H}] = -0.7$, age $\approx 2$ Gyr. This is followed by a change in slope in the AMR and the presence of more metal-rich populations up to $[\text{Fe/H}] = 0.0$ dex at age $\approx 500$ Myr. The tight AMR between ages $2-5$ Gyr is also reproduced in both stellar over-densities, and likely belongs to the Fornax field (see also Figs. 5 and 6). In the centre of Fornax, the SFRs go down along the narrow AMR with decreasing age, followed by an increase at age $\approx 2$ Gyr, $[\text{Fe/H}] = -0.5$ dex. This coincides with the main star formation peak in the known over-density, hinting at a link between the two components. In the case of an in-fall event, the gas that formed the over-density may also have triggered new star formation in the Fornax centre around age $\approx 1.5$ Gyr.

The youngest stars in the Fornax field AMR display age $\approx 500$ Myr and $[\text{Fe/H}] \approx +0.1$ dex, marking the termination of star formation in the centre. To the middle panel of Fig. 7 shows that the very young populations in the new over-density are not reproduced in the Fornax centre or the known over-density. Comparison between the CMD of the Fornax centre and the young over-density (Fig. 8) shows that stars consistent with the young MS could be present in the Fornax centre, but only at very low levels. Therefore, the new over-density formed after the last substantial episode of star formation in the Fornax centre, with a metallicity comparable to the youngest Fornax field stars.

6. Discussions and conclusions

We have conducted a new study of young stellar over-densities in the Fornax dSph galaxy, using wide-field, deep photometric data presented in de Boer et al. (2012b). By making a colour selection to isolate young stars, we have discovered a new stellar over-density in Fornax, located at a distance of 0.3 degrees (0.7 kpc) from the centre (see Fig. 2). Using deep $V, B-V$ CMDs, we have analysed the stellar populations of the known over-density and the newly discovered over-density.

The previously discovered over-dense feature displays a CMD with a young MS feature that is only weakly reproduced in the associated Fornax field star contribution. The SFH (see Fig. 5) shows a well-developed AMR at young ages and a main over-density population with metallicity $[\text{Fe/H}] \approx -0.6$ dex and age $\approx 1.5$ Gyr. These values are consistent with the young MS feature in the CMD as well as previous studies of the overdensity (Olszewski et al. 2006). Comparison between the centre of Fornax and the over-density (see Fig. 7) shows that the main population is consistent with the Fornax AMR, although located at a relatively large distance from the centre (1.3 $r_{\text{core}}$). The high metallicity of the stars makes it unlikely that the over-density is the result of an in-falling primordial gas cloud. Furthermore, since there are no signs of increased numbers of old and intermediate stars, it is unlikely that it was formed by the accretion of a small gas-rich galaxy, unless it contained very little star formation at the time of in-fall.

The properties of the known over-density are consistent with having been formed by the re-accretion of previously expelled gas. Such a scenario has been proposed by Yozin & Bekki (2012) to explain the multiple episodes of star formation in the Carina and Fornax dSphs, and would explain why the gas is enriched to similar values as the Fornax field. Furthermore, an in-fall event is the most likely process to explain the presence of a young outer over-density feature outside of the tidal radius (Coleman et al. 2005a). If both the inner and outer over-densities were the result of the same process, the AMR of both features will be consistent. This can be determined by conducting a deep CMD study of the outer structure discovered by Coleman et al. (2005a).
The new over-density is also formed of young stars. The CMD (Fig. 3) shows a very young MS that is not reproduced in the field stars. The SFH in Fig. 6 shows a clear peak at ages \( \leq 0.3 \) Gyr with metallicities close to solar \( ([\text{Fe/H}] = 0.0 \text{ dex}) \), confirming that this over-density constitutes some of the youngest, most metal-rich star formation in Fornax. The SFH of the new over-density is peaked in the youngest age bin considered in this study (100 Myr), implying that the stars could be even younger than the age determined here. However, the excellent fit of the 100–200 Myr isochrone to the young MS (see Fig. 3) gives confidence to the age recovered in the SFH. However, the use of deeper CMDs and spectroscopic metallicity measurements would allow a more accurate determination of the age of this young over-density.

It is unclear what triggered this young star formation episode, especially given its location outside the centre of Fornax. If both previously detected over-dense features are linked to a recent in-fall event, it seems possible the new over-density may also be linked to an accretion event. The total mass in stars in the young populations is relatively small \( (\approx 10^4 M_\odot) \) suggesting it could be formed from Fornax gas or the accretion of a small gas cloud. However, since the metallicity of stars in the over-density is comparable to the youngest Fornax stars, it is more likely that the feature formed from leftover gas expelled during the last episode of star formation in the Fornax centre.

The SFH of both stellar over-densities show the presence of stellar populations with ages 1.5–2.0 Gyr. Furthermore, evidence of this population is also found in the associated Fornax field and the central region of Fornax. Therefore, this population could be more widespread than just the over-density where it was first found. If this feature was indeed formed by an in-fall event it is possible that stars with these properties were spread throughout the Fornax dSph during the accretion process. However, kinematic information is needed to unambiguously determine the origin and connection of both over-densities and their association to the young stellar populations of Fornax.

Acknowledgements. The authors thank ISSI (Bern) for support of the team “Defining the full life-cycle of dwarf galaxy evolution: the Local Universe as a template”. T.d.B and E.T. gratefully acknowledge the Netherlands Foundation for Scientific Research (NWO) for financial support through a VICI grant. E.O. is partially supported by NSF grant AST0807498. The authors would like to thank the anonymous referee for his/her comments, that helped to improve the paper.

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