Computation, Efficiency and Endogeneity in Discrete Choice Models

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COMPUTATION, EFFICIENCY AND ENDOGENEITY IN DISCRETE CHOICE MODELS

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