CONTOUR DETECTION BY MULTIRESOLUTION SURROUND INHIBITION

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ABSTRACT

In natural images, luminance changes occur both on object contours and on textures. Often, the latter are stronger than the former, thus standard edge detectors fail in isolating object contours from texture. To overcome this problem, we propose a multiresolution contour detector motivated by biological principles. At each scale, texture is suppressed by using a bipolar surround inhibition process. The binary contour map is obtained by a contour selection criterion that is more effective than the classical hysteresis thresholding. Robustness to noise is achieved by Bayesian gradient estimation.

Keywords: edge, context, contour, surround suppression, texture

1. INTRODUCTION

Edge and contour detection, an important task in computer vision, is a fertile field of ongoing research (see [1] for a survey). Standard edge detectors react to all non-negligible luminance changes in an image, irrespective whether they are originated by object contours or by texture (grass, foliage, waves, etc.). Moreover, luminance changes due to texture are often stronger than ones due to contours. Our goal is to isolate objects in a scene; therefore, some further process is needed with respect to general purpose edge detectors. Specifically, we use some principles deployed in the Human Visual System (HVS). Psychophysical studies show that the perception of an oriented stimulus can be influenced by other similar stimuli in the surroundings [2]. Neurophysiological researches show that surround modulation is due to a specific neural mechanism. In [3] it has been suggested that surround suppression effectively enhances contours in natural images rich in textures. Other psychological experiments show that the retinal image is decomposed through band-pass filters. Low-pass filters are responsible for the so called pre-attentive stage of vision, corresponding to the first 0.1 – 0.3 s of the image persistency on the retina, where only the general morphology is perceived [4]. High-pass filters deliver information for the subsequent attentive stage where details are recognized. A multiresolution approach to contour detection has been proposed in [5]. In the current work we extend our previous studies [6] in combining a multiresolution approach and surround inhibition. We propose a method that detects contours at different resolutions and combines them by a contour-oriented selection algorithm. At each scale, noise is reduced by optimal Bayesian Minimum Mean Square Estimation (MMSE) of the gradient in additive noise and texture is suppressed by a biologically motivated surround inhibition process.

2. SCALE DEPENDANT CONTOUR DETECTOR

The proposed single scale contour detector is depicted in Fig. 1, where \( I'(x,y) \) is a noisy version of a given image \( I(x,y) \) corrupted by additive independent noise \( w(x,y) \). First, the gradient of the input image \( I' \) is evaluated by convolution with the gradient of a Gaussian kernel \( g(x,y) \) [8]. The gradient estimation depends on the parameter \( \sigma \), which we will call scale, or resolution.

\[
\nabla a I' = \nabla [I' * g_{1/\sigma}] = [I' * \nabla g_{1/\sigma}], \quad g_{1/\sigma}(x,y) = \frac{1}{2\pi \sigma^2} e^{-\frac{x^2+y^2}{2\sigma^2}}
\]

(1)

Then, Bayesian denoising, described in Section 2.1, is applied on the noisy image gradient. Surround inhibition is performed as described in Section 2.2.

2.1 Bayesian denoising

Our goal is to find the optimal estimator \( \hat{a} \) of the unknown vector \( a = \nabla a I \), when a noisy version \( z = \nabla a I + \nabla a w \) is observed. As well known from the Bayesian estimation theory, the optimal MMSE estimator is given by:

\[
\hat{z} = \frac{p_{\hat{a}}(z|a)p_a(a)}{p_{\hat{a}}(z|a)p_a(a)}a
\]

(2)

According to recent statistical studies on natural images [7], both \( p_a(a) \) and \( p_{\hat{a}}(z|a) \) are assumed Gaussian Scale Mixture (GSM), with covariance matrices \( A_i \) and \( N_i \) respectively:

\[
\begin{align*}
  p_a(a) &= \sum_{i=1}^{K_i} \lambda_i N(0,A_i), \\
  p_{\hat{a}}(z|a) &= \sum_{i=1}^{K_i} \beta_i N(z,a,N_i)
\end{align*}
\]

(3)

where:

\[
N(\xi,R) = \frac{1}{2\pi \det R} \exp \left[ -\frac{1}{2}(\xi - \mu)^T \Omega^{-1}(\xi - \mu) \right]
\]

(4)

By substituting eq. (3) in eq. (2), we can find the following closed expression for the optimal MMSE estimator:

\[
\hat{a}(z) = \frac{\sum_{i=1}^{K_i} \beta_i \lambda_i N_i(z,0,A_i+N_i)A_i^{-1}(A_i+N_i)^{-1}z}{\sum_{i=1}^{K_i} N_i(z,0,A_i+N_i)}
\]

(5)

The nonlinearity defined by eq. (5), applied to each pixel of the gradient \( \nabla a I' \), gives the best estimation of \( \nabla a I \).

2.2 Surround inhibition

Next, a surround inhibition operator taking into account the context
influence of the surrounding of each point is deployed. In [3] an inhibition term \( T_m(x, y) \) is introduced as the local average of the gradient magnitude \( M_m(x, y) = |\nabla I(x, y)| \) on a ring \( r \) around each pixel. \( T_m(x, y) \), large in textured areas and small for isolated edges, is then subtracted from \( M_m(x, y) \), thus reducing the response to texture. With this type of inhibition, there is a certain auto-inhibition of isolated edges. Moreover, edges at texture borders are considerably inhibited as well, which is not desirable with respect to the detection of region boundaries. In order to overcome these problems, we propose a bipolar inhibition term and a two-level inhibition process.

A. Bipolar inhibition term

The ring \( r \) is split along the edge direction \( S_\phi(x, y) \) in two halves \( r^+ \) and \( r^- \), on which two local averages \( T_m^\phi(x, y) \) are evaluated (see Fig. 2) and the smaller value is taken as an inhibition term. Specifically, let us consider the following pairs of orientation dependent filters \( w_{\phi, \sigma}(x, y) \), which define two half-rings oriented along an angle \( \phi \in [0, \pi] \):

\[
\begin{align*}
W_{\phi, \sigma}^+(x, y) &= |g_{\phi, \sigma}(x, y) - g_{\phi, \sigma}(x, y)| \cdot U[\pm (x \cos \phi + y \sin \phi - \alpha)] \\
W_{\phi, \sigma}^-(x, y) &= |g_{\phi, \sigma}(x, y) - g_{\phi, \sigma}(x, y)| \cdot U[\pm (x \cos \phi + y \sin \phi - \alpha)]
\end{align*}
\]

where

\[
\int_{I^-} = \begin{cases} \xi, & \xi \geq 0 \\
0, & \xi < 0 \end{cases} 
\]

\[
U(\xi) = \begin{cases} 1, & \xi \geq 0 \\
0, & \xi < 0 \end{cases}
\]

The weighted local averages are defined by the following convolutions and, for each pixel, the minimum response is taken:

\[
\begin{align*}
T_m^+(x, y) &= M_m \ast w_{\phi, \sigma}^+(x, y) \\
T_m^-(x, y) &= M_m \ast w_{\phi, \sigma}^-(x, y)
\end{align*}
\]

The convolutions are computed for a discrete set of orientations \( \{\phi\}_{i=1}^{N_\phi} \), \( \phi = \pi (i - 1) / N_\phi \) and, for each pixel, the result obtained for the angle \( \phi \) that is closest to the gradient orientation \( \delta_\phi(x, y) \), is used (see Fig. 3).

On isolated edges (Fig. 2a), the local averages on both sides are very low, ideally zero. Consequently, \( T_m(x, y) \) is low and contours are not inhibited. In textured areas (Fig. 2b), the local averages on both sides are high and so will be the inhibition term. Borders of textured areas are not inhibited, since \( T_m(x, y) \) is low on such points (Fig. 2c). These modifications lead to a considerable improvement of the surround inhibition effect obtained in [3].

B. Two-level inhibition

The proposed inhibition scheme is shown in Fig. 4, where the inhibition term \( T_m(x, y) \) is computed as specified in Section 2.2.4. Two inhibited gradient fields \( c_{\sigma, \alpha_1}(x, y) \) and \( c_{\sigma, \alpha_2}(x, y) \) are evaluated, corresponding to strong and weak inhibition, respectively:

\[
c_{\sigma, \alpha}(x, y) = |M_m(x, y) - \alpha T_m(x, y)|, \quad \alpha = \alpha_1, \alpha_2, \quad \alpha_1 > \alpha_2
\]

The strongly inhibited \( c_{\sigma, \alpha_1}(x, y) \) contains only little texture, but some weak contours are broken (Fig. 5a). On the contrary, the weakly inhibited \( c_{\sigma, \alpha_2}(x, y) \) contains all contours, but texture is still present (Fig. 5b). In order to get the advantages of both inhibition levels, we combine \( c_{\sigma, \alpha_1} \) and \( c_{\sigma, \alpha_2} \) as follows:

First, we apply non-maxima suppression and consider the sets \( S_1 \) and \( S_2 \) of the non-zero pixels of \( c_{\sigma, \alpha_1} \) and \( c_{\sigma, \alpha_2} \):

\[
S_i = \{(x, y) \mid c_{\sigma, \alpha_i}(x, y) \neq 0, \quad \frac{\partial c_{\sigma, \alpha_i}}{\partial u} = 0, \quad \frac{\partial^2 c_{\sigma, \alpha_i}}{\partial u^2} < 0\}, \quad i = 1, 2
\]

Fig. 2 Half-rings on which \( M_m(x, y) \) is averaged, for: isolated edges (a), textured areas (b), borders of textured areas (c).

The sets \( S_1 \) and \( S_2 \) have been obtained without thresholding the output binary map \( b_u \).

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where \( u \) is the direction of the gradient \( V_u \). Note that \( S_1 \subseteq S_2 \), since \( \alpha_1 > \alpha_2 \). Then, the output binary map \( b_u \) is defined as the set of pixels of \( S_2 \) which are connected to at least one point of \( S_1 \). In this way, the broken contours of \( S_1 \) are restored and most of the texture present in \( S_2 \) is removed (Fig. 5c). The sets \( S_1 \) and \( S_2 \) have been obtained without thresholding the output binary map \( b_u \).
gradient magnitude in order to preserve the weak contours, thus some undesired edges are still present in Fig. 5c. In the common situation where some object contours are weaker than texture, the standard hysteresis thresholding techniques will fail. In the next section, the information at more resolutions are combined to select the desired contours and suppress even more texture.

3. MULTISCALE CONTOUR COMBINATION

As well known from multiresolution analysis, coarse scales contain the general morphology and almost no texture. On the other hand, contours detected at coarse scales are smoothed, shifted [9], and the non-maxima suppression destroys the junctions [10]. Thus, information at more scales can be combined in order to contain contours as detailed as at the fine scales, but without the texture that does not appear at coarse scales [5, 6, 11]. In [6], this has been achieved through the pixel by pixel logic AND combination of binary contour maps obtained at different scales. A morphological dilation at coarse scales is applied, in order to compensate the shifting and restore the junctions (see [6] for details). However, this approach has the drawbacks shown in Fig. 6a: part of the object contour \( C_i^{(n)} \), detected at the scale \( n \), falls outside its counterpart \( C_i^{(n)} \) at coarser scale \( n \), therefore it is destroyed by the logic AND. Conversely, the accidental superposition of some residual texture in \( C_{-1}^{(n)} \) and \( C_{-1}^{(n)} \) is maintained.

To overcome these problems, we propose the multiscale contour detector shown in Fig. 7. First, the binary contour maps \( b_1, \ldots, b_N \) at the scales \( \sigma_1 < \sigma_2 < \ldots < \sigma_N \) are computed using the contour detector introduced in Section 2. Given two binary contour maps \( b_{n-1} \) and \( b_n \), detected at two adjacent scales, a new map \( b_{n-1}^\text{out} = \text{CS}(b_{n-1}, b_n) \) is obtained as detailed in Fig. 8, by means of the mathematical operator CS (Contour Selector). It selects from \( b_{n-1} \) (finer scale), the pieces of contours having a good overlap with the contours \( b_n \) (coarser scale) and forming long chains of non-zero pixels. The operator CS is applied iteratively from the coarsest scale up to the finest one.

In more detail, the block CS operates as follows: first, the morphological dilation \( \tilde{b}_n = b_n \oplus D_2 \) is computed, with a disk \( D_2 \) of radius 2 pixel as a structuring element. The connected components of \( b_{n-1} \) and \( \tilde{b}_n \) are denoted by \( C_{k}^{(n-1)} \) and \( C_i^{(n)} \), respectively:

\[
b_{n-1} = \bigcup_k C_k^{(n-1)}, \quad \tilde{b}_n = \bigcup_i C_i^{(n)}.
\]

We measure the degree of overlapping between \( C_i^{(n-1)} \) and \( B_2 \) by the following quantity:

\[
X_i^{(n-1)} = \frac{\text{card}(C_i^{(n-1)} \cap \tilde{b}_n)}{\text{card}(C_i^{(n-1)})}.
\]

where \( \text{card}(X) \) indicates the cardinality of the set \( X \). All the components \( C_{k}^{(n-1)} \) such that \( X_{k}^{(n-1)} \) is below a threshold \( T_d \) are removed. Thus the component \( C_i^{(n-1)} \) in Fig. 6a will not be broken and the undesired component \( C_{-1}^{(n-1)} \) will be completely removed.

The second step consists in labeling the components \( C_i^{(n-1)} \), which are included in the same component \( C_i^{(n)} \), as part of the same object \( O_i^{(n)} \) (Fig. 6b).

The final contour map \( b_{n-1}^\text{out} \) is given by the union of all the objects \( O_i^{(n-1)} \) whose weight is above a given threshold \( T_g \):

\[
b_{n-1}^\text{out} = \text{CS}(b_{n-1}, b_n) = \bigcup_i O_i^{(n-1)}
\]

In this way, we exploit the fact that object contours form long chains of non-zero pixels (high weight), whereas textures only forms short rods (low weight). Such approach is more effective than thresholding the local gradient magnitude, because often luminance changes due to texture are stronger than the ones due to object contours.

4. EXPERIMENTAL RESULTS AND COMPARISON

The performance of the proposed contour detector has been compared with four other existing algorithms. The results are presented in Figs. 9 and 10 for a test image, without and with additive noise (SNR = 13 dB). Other results are available on the webpage www.cs.ru.nl/~papari/resultsICIP06.htm. As it can be seen, our approach gives the best results in terms of texture suppressed, cleanliness of the detected contour, and robustness to noise.

Fig. 7. Proposed multiscale contour detector.

Fig. 6. (a) A pixel based superposition would destroy part of the object contour \( C_i^{(n-1)} \), and would keep part of the spurious texture \( C_{-1}^{(n-1)} \). (b) The object \( O_i^{(n-1)} \), given by the union of the four connected components \( C_i^{(n-1)}, C_{e-1}^{(n-1)}, C_{o-1}^{(n-1)} \) of \( b_i \), belongs to the connected component \( C_i^{(n)} \) of \( \tilde{b}_n \).
With respect to the Canny edge detector (Figs. 9c, 10c), the benefits of the multiscale analysis [5], without surround inhibition, are shown in Figs. 9d, 10d: some texture is removed and noise is reduced. Comparable texture suppression is achieved with the single scale surround inhibition algorithm proposed in [3], (see Figs. 9e, 10e). The combination of multiscale analysis and surround inhibition [6] gives the much better results shown in Figs. 9f, 10f. The improvement proposed here leads to the even better result shown in Figs. 9b, 10b.

A ground-truth based performance evaluation has also been performed. The similarity $\rho$ between each Algorithmic Result (AR) and the Ground Truth (GT) has been computed as follows:

$$\rho = \frac{EC}{EC + MC + FP}$$  \hspace{1cm} (14)

where $EC$ (Exact Contours) indicates the number pixels present both in the AR and in the GT. $MC$ (Missing Contours) indicate the number of pixel present in the GT but not in the AR. $FP$ (false Positive) indicates the number of pixel present in the AR but not in the GT, and measure the amount of not suppressed texture. $\rho$ is always between 0 and 1, with $\rho = 1$ iff AR = GT.

![Fig. 9](image_url) Input image (a) and contours detected with: (b) the proposed approach, (c) the Canny edge detector, (d) the multiscale edge detector CARTOON without surround inhibition [5], (e) single [3] and (f) multi scale surround inhibition [6].

For each studied algorithm, the values of $\rho$ have been computed on a set of 24 images. The average value $\bar{\rho}$ and the standard deviation $\sigma_\rho$ are shown in Fig. 11, both for noiseless and noisy images.

5. SUMMARY AND CONCLUSION

The proposed multiscale contour detector exploits important aspects of the HVS, in order to isolate object contours from texture. Edges surrounded by other edges are inhibited, since the HVS perceives them as texture rather than object contours. The bipolar mechanism introduced here avoids the auto-inhibition of the weak contours. The two-level inhibition process operates a strong inhibition on textured areas and a weak one on object contours. Similarly to the HVS, contours are detected at more resolutions. All the contours’ parts having a low overlapping degree $\chi_2$ with respect to the adjacent coarser scale, and a low weight $R_1$ are removed. Thresholding global quantities as $\chi_2$ and $R_1$ is more effective than thresholding the local gradient magnitude $M_\alpha(x,y)$. Robustness to noise, for the general non-Gaussian case, is achieved by using a Bayesian estimator. GMS models are employed for both the image and the noise and a closed form of the estimator has been provided. As shown by experimental results and performance evaluations, our algorithm outperforms both standard and more sophisticated approaches, based on single and multiscale surround inhibition.

![Fig. 11](image_url) Quantitative performance comparison.

6. REFERENCES