University of Groningen

Coupling of Yang-Mills to $N = 4$, $d = 4$ supergravity

Bergshoeff, E.; Koh, I.G.; Sezgin, E.

Published in:
Physics Letters B

DOI:
[10.1016/0370-2693\(85\)91034-2](https://doi.org/10.1016/0370-2693(85)91034-2)

IMPORTANT NOTE: You are advised to consult the publisher's version (publisher's PDF) if you wish to cite from it. Please check the document version below.

Document Version
Publisher's PDF, also known as Version of record

Publication date:
1985

[Link to publication in University of Groningen/UMCG research database](#)

Citation for published version (APA):

Bergshoeff, E., Koh, I. G., & Sezgin, E. (1985). Coupling of Yang-Mills to $N = 4$, $d = 4$ supergravity. *Physics Letters B*, 155(1-2), 71-75. [https://doi.org/10.1016/0370-2693\(85\)91034-2](https://doi.org/10.1016/0370-2693(85)91034-2)

Copyright

Other than for strictly personal use, it is not permitted to download or to forward/distribute the text or part of it without the consent of the author(s) and/or copyright holder(s), unless the work is under an open content license (like Creative Commons).

The publication may also be distributed here under the terms of Article 25fa of the Dutch Copyright Act, indicated by the "Taverne" license. More information can be found on the University of Groningen website: <https://www.rug.nl/library/open-access/self-archiving-pure/taverne-amendment>.

Take-down policy

If you believe that this document breaches copyright please contact us providing details, and we will remove access to the work immediately and investigate your claim.

Downloaded from the University of Groningen/UMCG research database (Pure): <http://www.rug.nl/research/portal>. For technical reasons the number of authors shown on this cover page is limited to 10 maximum.

COUPLING OF YANG-MILLS TO $N = 4$, $d = 4$ SUPERGRAVITY

E. BERGSHOEFF, I.G. KOH¹ and E. SEZGIN

International Centre for Theoretical Physics, Trieste, Italy

Received 5 March 1985

We couple $N = 4$, $d = 4$ supersymmetric Yang-Mills theory to supergravity. The scalars of the theory parametrize the coset $(SO(n,6)/[SO(n) \times SO(6)]) \times (SU(1,1)/U(1))$. Keeping the composite local $SO(n) \times SO(6) \times U(1)$ invariance intact, we gauge an $(n+6)$ parameter subgroup of $SO(n,6)$ which is either (i) $SU(2) \times SU(2) \times H$ ($\dim H = n$), (ii) $SO(4,1) \times H$ ($\dim H = n-4$) or (iii) $SO(6,1) \times H$ ($\dim H = n-15$). In all these cases the theory has an indefinite potential.

Matter couplings of $N = 1$ supergravity have been widely studied in recent years^{†1}. Although they have been applied to phenomenology with some success^{†2}, a great deal of arbitrariness remains in these theories. This is mainly due to the fact that scalar multiplets in arbitrary representations can be coupled to $N = 1$ supergravity, the only restriction being that the scalars of the matter multiplet parametrize a Kahler manifold [1]. This still allows two arbitrary functions of the scalars in the theory. The matter couplings in $N = 2$ supergravity are somewhat more restrictive. In that case, the scalars of the matter multiplets must parametrize a quaternionic Kahler manifold [1] and only one arbitrary function is allowed. On the other hand, supersymmetry breaking from $N = 2$ to $N = 1$ in Minkowski background has been shown to be impossible [3].

Since matter multiplets exist upto $N = 4$, it is natural to consider the matter couplings of $N = 4$ supergravity [4]. In fact, the only $N = 4$ matter multiplet available is the vector multiplet [5] which contains six scalars. Thus, the $N = 4$ supergravity coupled to matter is clearly the largest possible and the most restrictive matter coupled supergravity. The scalar couplings in this theory are described by the manifold

$(SO(n,6)/[SO(n) \times SO(6)]) \times (SU(1,1)/U(1))$, where n is the number of vector multiplets. The $N = 4$ ungauged matter couplings based on this coset structure have been recently constructed by the Roo [6]. For phenomenological purposes, one must gauge an appropriate subgroup of the global $SO(n,6) \times SU(1,1)$. Such gaugings require the addition of a potential to the theory. It is important to determine whether such a potential allows the breaking of supersymmetry from $N = 4$ down to $N = 1$.

With these motivations in mind, we have constructed the gauged matter couplings of $N = 4$, $d = 4$ supergravity. In this paper we gauge an $(n+6)$ parameter subgroup of $SO(n,6)$, and do not consider the gauging of the $U(1)$ subgroup of $SU(1,1)$. We find that the gauge group must be either $SU(2) \times SU(2) \times H$ ($\dim H = n$) or $SO(4,1) \times H$ ($\dim H = n-4$) or $SO(6,1) \times H$ ($\dim H = n-15$). In the latter two cases there is a natural Higgs mechanism which breaks $SO(4,1)$ to $SO(4)$ and $SO(6,1)$ to $SO(6)$, respectively. The potential which we find is indefinite, and it depends on the structure constants of the gauge group and the representative elements of the $(SO(n,6)/[SO(n) \times SO(6)]) \times (SU(1,1)/U(1))$ coset scalars. In obtaining these results, we follow closely the methods of refs. [7-9] which were recently applied to $d = 7$ supergravity [10].

In this letter we use a formulation of the $N = 4$, $d = 4$ supergravity multiplet and the n vector multiplets that has manifest global $SU(4)$ invariances [4]. The field components of the supergravity multiplet

¹ On leave of absence from Physics Department, Sogang University, Seoul, Korea

^{†1} For a review with references for earlier work, see ref. [1].

^{†2} For a review with an extensive list of references, see ref. [2].

are given by a vierbein e_μ^m , four gravitini ψ_μ^I of positive chirality⁺³, six vector fields A_μ , four spinors χ^I of negative chirality (i.e. $\gamma_5 \chi^I = -\chi^I$) and one complex scalar z that parametrizes an $SU(1,1)/U(1)$ coset space [4]. On the other hand, an $N=4$ vector multiplet consists of one vector field A_μ , four spinors λ^I of positive chirality (i.e. $\gamma_5 \lambda^I = +\lambda^I$) and six scalars. In the coupled system the scalars of the n vector multiplets parametrize the coset $SO(n,6)/[SO(n) \times SU(4)]$. Recall that $SU(4) \approx SO(6)$.

The $6n$ scalars of the n vector multiplets are conveniently described by an $(n+6) \times (n+6)$ matrix L_I^A ($I, A = 1, \dots, n+6$), which is a representative element of the coset space $SO(n,6)/[SO(n) \times SU(4)]$ [8]. The index A can be decomposed into a $\mathbf{6}$ of $SU(4)$ and an $\mathbf{n}$ of $SO(n)$

$$L_I^A \rightarrow (L_I^{ij}, L_I^a), \quad i, j = 1, \dots, 4, \quad a = 1, \dots, n, \quad (1)$$

where L_I^{ij} is antisymmetric in $SU(4)$ indices and subject to an $SU(4)$ covariant constant

$$L_I^{ij} = (L_{Iij})^* = \frac{1}{2} \epsilon^{ijkl} L_{Ikl}. \quad (2)$$

In terms of the fields defined by (1) the orthogonality condition for the $SO(n,6)$ matrix L_I^A reads:

$$-L_I^{ij} L_{Jij} + L_I^a L_{Ja} = \eta_{IJ}, \quad (3)$$

where $\eta_{IJ} = \text{diag}(-, -, -, -, -, +, +, \dots, +)$. The components of the inverse matrix L_I^A are defined by

$$L_I^a L_{Ia}^I = 0, \quad L_I^{ij} L_{Ikl}^I = -\frac{1}{2} (\delta_k^i \delta_l^j - \delta_l^i \delta_k^j), \quad (4)$$

The matrix L_I^A transforms under global $SO(n,6)$ from the left and local composite $SO(n) \times SU(4)$ from the right. The latter transformations are given in table 1.

Similarly, the complex scalar z of the supergravity multiplet can be described by two constrained complex scalars ϕ and ψ :

$$\phi^* \psi + \phi \psi^* = 2. \quad (5)$$

In terms of the unconstrained variable z they are given by

⁺³ We use the chiral notation, i.e. $\gamma_5 \psi_\mu^I = +\psi_\mu^I$ and $\gamma_5 \psi_{\mu I} = \gamma_5 C(\bar{\psi}_\mu^I)^T = -\psi_{\mu I}$. We use the signature $(-+++)$, and the Ricci tensor $R_\mu^a = e_b^\nu (\partial_\mu \omega_\nu^{ab} - \dots)$

Table 1

Transformation properties and restrictions of the fields

Field	$SO(n) \times SU(4) \times U(1)$	Restrictions
e_μ^m	$(1, 1, 0)$	
ψ_μ^I	$(1, \mathbf{4}, -1/2)$	$\gamma_5 \psi_\mu^I = +\psi_\mu^I$
A_μ^I	$(1, 1, 0)$	
L_I^a	$(\mathbf{n}, 1, 0)$	
L_I^{ij}	$(1, \mathbf{6}, 0)$	$L_I^{ij} = \epsilon^{ijkl} L_{Ikl}/2$
χ^I	$(1, \mathbf{4}, 3/2)$	$\gamma_5 \chi^I = -\chi^I$
λ^{aI}	$(\mathbf{n}, \mathbf{4}, 1/2)$	$\gamma_5 \lambda^{aI} = +\lambda^{aI}$
ϕ, ψ	$(1, 1, 1)$	$\phi^* \psi + \phi \psi^* = 2$

$$\phi = (1 - z^*)/(1 - zz^*)^{1/2}, \quad \psi = (1 + z^*)/(1 - zz^*)^{1/2}. \quad (6)$$

The transformations of ϕ and ψ under the composite $U(1)$ are given in table 1. The $SU(1,1)$ invariance is realized only in the equations of motion [4]. We find that after gauging the global $SU(1,1)$ is broken.

We now require that all the remaining fields of the supergravity and vector multiplets transform in definite representations of the global $SO(n,6)$ and the local composite $SO(n) \times SU(4) \times U(1)$ symmetries of the coset space $(SO(n,6)/[SO(n) \times SU(4)]) \times (SU(1,1)/U(1))$. The $n+6$ vector fields A_μ^I ($I=1, \dots, n+6$) transform according to the defining representation of $SO(n,6)$ [7]. The transformation properties of the remaining fields under the composite $SO(n) \times SU(4) \times U(1)$ are given in table 1. The vector fields A_μ^I are now used to gauge an $(n+6)$ parameter subgroup of $SO(n,6)$ with structure constant f_{IJ}^K .

A central role in the construction of an action and supersymmetry transformation rules is played by the gauge covariant Maurer–Cartan form $L^{-1}(\partial + A)L$, which has the following components [11,12,8].

$$\begin{aligned} P_{\mu a}^I &= L_a^I (\partial_\mu \delta_I^K + f_{IJ}^K A_\mu^J) L_K^I, \\ Q_{\mu ab} &= L_a^I (\partial_\mu \delta_I^K + f_{IJ}^K A_\mu^J) L_{Kb}^I, \\ Q_{\mu j}^I &= L^{Ik} (\partial_\mu \delta_I^K + f_{IJ}^K A_\mu^J) L_{Kkj}. \end{aligned} \quad (7)$$

Note that we have absorbed the gauge coupling constant into the structure constants f_{IJ}^K .

In order to ensure the composite local $SO(n) \times SU(4)$ transformation properties of P and Q , the structure constants must satisfy

$$f_{IJ}^L \eta_{KL} = f_{[IJ}^L \eta_{K]L}. \quad (8)$$

This condition can be satisfied by taking η_{IJ} to be the Cartan–Killing metric of the gauged algebra. Since η_{IJ} has 6 minus, and n plus signature it follows that the gauge group is either (i) $SU(2) \times SU(2) \times H$ ($\dim H = n$), (ii) $SO(4,1) \times H$ ($\dim H = n - 4$) or (iii) $SO(6,1) \times H$ ($\dim H = n - 15$). In case (i) the coupling constants of the two $SU(2)$'s need not be equal. Furthermore, it is convenient to introduce the following projections of the structure constants f_{IJ}^K [8]:

$$\begin{aligned} C_{ij} &= f_{IJ}^K L^I_{ik} L^J_{jl} L^K_{kl}, \\ C_{aj}^i &= \frac{1}{2} f_{IJ}^K L^I_{ik} L^J_{jl} L^K_{ka}, \\ C_{ab}^{ij} &= f_{IJ}^K L^I_a L^J_b L^K_{ij}. \end{aligned} \quad (9)$$

The P and Q defined in eq. (7) satisfy the following Maurer–Cartan equations [8,10]:

$$\begin{aligned} D_{[\mu} P_{\nu]}^a &= -\frac{1}{2} F_{\mu\nu}(A)^I L_I^{ak} [C_{ak}^j] + \frac{1}{2} F_{\mu\nu}(A)^I L_I^b C_{ab}^{ij}, \\ P_{[\mu}^{aik} P_{\nu]}^{akj} &= \frac{1}{2} Q_{\mu\nu}^{ij} - \frac{1}{2} i F_{\mu\nu}(A)^I L_I^a C_{aj}^i \\ &\quad + \frac{1}{3} [F_{\mu\nu}(A)^I L_I^{ik} C_{kj} - \text{h.c.}], \end{aligned} \quad (10)$$

where $F_\mu(A)^I$ and $Q_{\mu\nu}^I$ are the field strengths of A_μ^I and $Q_{\mu\nu}^I$, respectively and h.c. denotes hermitian conjugation. In products of C functions one can make use of the Jacobi identity $f_{[IJ}^K f_{K]LM} = 0$. This leads to the following identities, which will be crucial in proving the supersymmetry of the action^{†4}

$$C_{ik}^{ai} C_{aj}^k - \frac{4}{9} C_{ik}^{ik} C_{aj}^k - \text{trace} = 0, \quad (11a)$$

$$C_{k(i}^{ab} C_{b)j}^k - \frac{2}{3} C_{(i}^{ak} C_{j)k} = 0. \quad (11b)$$

We remark that similar identities play an important

role in $N = 8, d = 4$ [12], and in $N = 8, d = 5$ [13] supergravities. Derivatives of C functions yield again C functions. For instance,

$$\begin{aligned} D_\mu C_{aj}^i &= i P_\mu^{bik} C_{abkj} - \frac{2}{3} i P_\mu^{aik} C_{kj} + \text{h.c.} - \text{trace}, \\ D_\mu C_{ij} &= -3 i P_{\mu(i} C_{j)}^k \end{aligned} \quad (12)$$

Similarly, we define for the $SU(1,1)/U(1)$ coset space

$$\begin{aligned} a_\mu &= -\frac{1}{2} (\phi \partial_\mu \psi^* + \psi \partial_\mu \phi^*), \\ P_\mu &= \frac{1}{2} (\phi \partial_\mu \psi - \psi \partial_\mu \phi). \end{aligned} \quad (13)$$

Their Maurer–Cartan equations are given by

$$D_{[\mu} P_{\nu]} = 0, \quad P_{[\mu}^* P_{\nu]} = -\partial_{[\mu} a_{\nu]}. \quad (14)$$

Another useful identity is

$$D_\mu \phi = -P_\mu \phi^*, \quad D_\mu \psi = P_\mu \psi^* \quad (15)$$

We are now able to derive the action and supersymmetry transformation rules for the coupled system. Using all the symmetries discussed above we can immediately write down an ansatz for the action and transformation rules up to some undetermined coefficients. These coefficients can easily be determined by requiring closure of the commutation algebra on the bosonic fields and supersymmetry of the action. The resulting lagrangian is given by

$$\begin{aligned} e^{-1} \mathcal{L} &= \frac{1}{2} R - \bar{\psi}_\mu^i \gamma^{\mu\nu\rho} D_\nu \psi_{\rho i} - \frac{1}{2} a_{IJ} F_{\mu\nu}^I F_{\mu\nu}^J \\ &\quad - \frac{1}{2} \bar{\chi}^i \not{D} \chi_i - P_\mu^* P_\mu - \bar{\chi}^i \not{D} \lambda_{ai} - \frac{1}{2} P_\mu^{aij} P_{\mu aij} \\ &\quad + \bar{\chi}^i \gamma^\mu \gamma^\nu \psi_{\mu i} P_\nu^* - 2 i \bar{\lambda}^{ai} \gamma^\mu \gamma^\nu \psi_\mu^j P_{\nu aij} \\ &\quad - (1/\phi) F_{\mu\nu}^I (\frac{1}{2} i \bar{\psi}_i^\lambda \gamma_{[\lambda} \gamma^{\mu\nu} \gamma_{\tau]} \psi_j^\tau L_I^{ij} \\ &\quad - \frac{1}{2} i \bar{\psi}^{\lambda i} \gamma^{\mu\nu} \gamma_\lambda \chi^j L_{Iij} \\ &\quad + \frac{1}{2} \bar{\psi}_\lambda^i \gamma^{\mu\nu} \gamma^\lambda \chi^{ai} L_{Ia} + \frac{1}{2} \bar{\lambda}_i^a \gamma^{\mu\nu} \chi^i L_I^a \\ &\quad + \frac{1}{2} i \bar{\lambda}^{ai} \gamma^{\mu\nu} \chi^{aj} L_{Iij}) \\ &\quad - \frac{2}{3} i \phi C_{ij} (\bar{\psi}_i^\mu \gamma^{\mu\nu} \psi_\nu^j - \bar{\psi}_\mu^i \gamma^\mu \chi^j - \bar{\lambda}^{ai} \lambda_j^a) \\ &\quad + 2 i \phi C_{aj}^i (\bar{\psi}_i^\mu \gamma^\mu \lambda_j^a + \bar{\chi}^j \lambda_i^a) - 2 i \phi C_{ab}^{ij} \bar{\lambda}_i^a \lambda_j^b \\ &\quad - \frac{1}{2} \phi^* \phi (A_{aj}^i C_{ai}^j - \frac{4}{9} C^{ij} C_{ij}) + \text{h.c.} \\ &\quad + \text{quartic fermions.} \end{aligned} \quad (16)$$

^{†4} The proof of both identities is similar. Here we sketch the proof of (11a). We start with $C_{ik}^{ai} C_{aj}^k$ (see eq. (9)), and use $L_I^a L_j^a = \eta_{IJ} + L_I^{mn} L_{Jmn}$ (see eq. (3)). The part containing $L_I^{mn} L_{Jmn}$ can be easily expressed in terms of products of C^{ij} . The part containing η_{IJ} is of the form $(6 \times 6 \times 6 \times 6)^{ij} = (15 + 1)^{ij}$. Noting that $6 \times (6 \times 6 \times 6)$ contains 15 only, it follows by the Jacobi identity that in $(6 \times 6 \times 6 \times 6)^{ij}$ only the singlet survives. This proves (11a).

Here we have used the following definitions

$$a_{IJ} = (\psi^*/\phi^*) L_I^I L_{J\bar{I}} + (\psi/\phi) L_I^I L_{J\bar{I}},$$

$$D_\mu \lambda_a^I = \partial_\mu \lambda_a^I + \frac{1}{4} \omega_\mu^{mn}(e) \gamma_{mn} \lambda_a^I + Q_{\mu a}^b \lambda_b^I + Q_{\mu j}^I \lambda_a^j - \frac{1}{2} a_\mu \lambda_a^I, \quad (17)$$

and similar definitions for $D_\mu \psi_\rho^I$ and $D_\mu \chi^I$. The action defined by eq. (16) is invariant under the following supersymmetry transformation rules:

$$\delta e_\mu^m = \bar{\epsilon}^I \gamma^m \psi_{\mu I} + \text{h.c.},$$

$$\delta \psi_\mu^I = 2D_\mu \epsilon^I + (1/2\phi) \gamma^{mn} F_{mn}^I L_I^I \epsilon_j + \frac{2}{3} 1\phi^* \gamma_\mu C^I \epsilon_j + \text{bilinear fermions},$$

$$\delta A_\mu^I = -21\phi L_{I\bar{I}}^I (\bar{\epsilon}^I \psi_\mu^I - \frac{1}{2} \bar{\epsilon}^I \gamma_\mu \chi^I) + \phi \bar{\epsilon}^I \gamma_\mu \lambda_a^I L_a^I + \text{h.c.},$$

$$\delta L_I^I = 2i L_{I\bar{I}}^I \bar{\epsilon}^I \lambda^I + \text{h.c.},$$

$$\delta L_{I\bar{I}}^I = -2i \bar{\epsilon}_{[I} \lambda_{\bar{I}}^I] L_a^I - \text{dual},$$

$$\delta \chi^I = (1/\phi^*) \gamma^{mn} F_{mn}^I L_I^I \epsilon_j + 2\gamma^m P_m \epsilon^I + \frac{4}{3} \phi C^I \epsilon_j + \text{bilinear fermions},$$

$$\delta \lambda^{aI} = -(1/2\phi^*) \gamma^{mn} F_{mn}^I L_I^I \epsilon^I + 2i \gamma^m P_m^{aI} \epsilon_j - 21\phi C^{aI} \epsilon^I + \text{bilinear fermions}, \quad (18)$$

$$\delta \phi = -\bar{\epsilon}_I \chi^I \phi^*, \quad \delta \psi = +\bar{\epsilon}_I \chi^I \psi^*,$$

where $D_\mu \epsilon^I$ is defined as in eq. (17). Both in the action and transformation rules the terms proportional to the C breaks the global $SU(1,1)$ invariance. Note also the absence of $\bar{\chi}\chi$ terms in the Pauli and mass terms [4]. Furthermore, we observe an interesting interference between the $SU(1,1)/U(1)$ and $SO(6,n)/[SO(6) \times SO(n)]$ coset structures in the definition of a_{IJ} (see eq. (17)). For pure supergravity we expect that our results reduce to those of ref. [14].

Let us finally comment on the potential that emerges from our gauging. In terms of the unconstrained variable z of the $SU(1,1)/U(1)$ coset space (see eq. (6)) it is given by

$$V(z, L) = \frac{(1-z)(1-z^*)}{(1-zz^*)} (C_{aI}^I C^{aI} - \frac{4}{9} C^I C_I). \quad (19)$$

Minimization of this potential with respect to the variables z ($0 \leq |z| < 1$) and L leads to the following equations, respectively

$$C_{aI}^I C^{aI} - \frac{4}{9} C^I C_I = 0, \quad C_{a[I}^I C_{J]k}^{ab} = 0 \quad (20)$$

The supersymmetry of the ground state is determined by the number of supersymmetry parameters which satisfy the equations $\delta \psi_\mu^I = \delta \chi^I = \delta \lambda^{aI} = 0$. In Minkowski background these equations read

$$C^I \epsilon_j = 0, \quad C_{aI}^I \epsilon^I = 0. \quad (21)$$

Using eqs. (11) one can show that these equations lead to the following integrability conditions

$$\{C_{aI}^I C^{aI} - \frac{4}{9} C^I C_I\} \epsilon_k = 0, \quad C_{a[I}^I C_{J]k}^{ab} \epsilon^I = 0. \quad (22)$$

This shows that the minimization condition, eq. (20), for the potential is sufficient for the fulfillment of the integrability conditions, eq. (22). The first condition in eq. (20) can only have a non-trivial solution if both C_{aI}^I and C^I are non zero. It turns out that this cannot be achieved for the gauge group $SU(2) \times SU(2) \times H$ ($\dim H = n$), $SO(4,1) \times H$ ($\dim H = n-4$) and $SO(6,1) \times H$ ($\dim H = n-15$). It would be interesting to see whether the $n+6$ vector fields, A_μ^I can be used to gauge groups other than the ones mentioned above and to see whether they can lead to an interesting super-Higgs effect that breaks the $N=4$ supersymmetry down to a lower one.

We are grateful to Professor Abdus Salam, the International Atomic Energy Agency and UNESCO for hospitality at the International Centre for Theoretical Physics, Trieste. One of us (I.G.K.) would like to thank KOSEF for partial financial support.

Note added After completing this work we became aware of the fact that de Roo [15] has also constructed the gauged matter couplings of $N=4$, $d=4$ supergravity.

References

- [1] G.A. Bagger, Lectures Bonn-NATO Advanced Study Institute on Supersymmetry (1984)

- [2] E g H.P. Nilles, Phys. Rep. 110 (1984) 1.
- [3] S Cecotti, L Girardello and M Porrati, Milan University preprint (1984)
- [4] E. Cremmer, J Scherk and S Ferrara, Phys Lett 74B (1978) 61
- [5] L. Brink, H. Scherk and J Schwarz, Nucl Phys B121 (1977) 77,
F. Gliozzi, P Olive and J. Scherk, Nucl Phys B122 (1977) 253
- [6] M de Roo, Groningen preprint (1984)
- [7] M Gunaydin, G Sierra and P K. Townsend, Nucl Phys B242 (1984) 244
- [8] S J Gates Jr, H Nishino and E Sezgin, ICTP, Trieste, preprint IC/84/105 (1984).
- [9] A Salam and E. Sezgin, Phys Lett 154B (1985) 37.
- [10] E Bergshoeff, I G. Koh and E Sezgin, ICTP, Trieste, preprint IC/85/10 (1985).
- [11] E Cremmer and B. Julia, Nucl Phys B159 (1979) 141
- [12] B de Wit and H. Nicolai, Nucl. Phys. B188 (1981) 98
- [13] M Pernici, K Pilch and P van Nieuwenhuizen, Stony Brook preprint ITP-SB-84-80 (1984).
- [14] D.Z Freedman and J Schwarz, Nucl. Phys B137 (1978) 333
- [15] M de Roo, private communication