## Causal Inference Illustrated via Simpson's paradox



Ofer Engel

## DAAAS Become a Member

# Sex Bias in Graduate Admissions: Data from Berkeley 

P. J. Bickel ${ }^{1}$, E. A. Hammel ${ }^{1}$, J. W. O'Connell ${ }^{1}$

+ See all authors and affiliations
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## Article

## Info \& Metrics

Abstract
Examination of aggregate data on graduate admissions to the University of California, Berkeley, for fall 1973 shows a clear but misleading pattern of bias against female applicants.
Examination of the disaggregated data reveals few decision-making units that show statistically significant departures from expected frequencies of female admissions, and about as manv units annear th favor women as to favor men If the data are nronerlv nonled

| f Sex Bias in Graduate Admissions: Data from Berkeley | ARTICLES <br> Sex Bias in Graduate Admissions: Data from Berkeley |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0 |  | Department | Men |  |  | Women |  |  |
| (in) |  |  | Applicants | Admitted |  | Applicants | Admitted |  |
|  |  | A | 825 | 512.00 | 62\% | 108 | 89 | 82\% |
|  | Articl | B | 560 | 353 | 63\% | 25 | 17 | 68\% |
|  |  | C | 325 | 108 | 33\% | 593 | 202 | 34\% |
|  | Ab: | D | 417 | 138 | 33\% | 375 | 131 | 35\% |
|  | Exar | E | 191 | 48 | 25\% | 393 | 98 | 25\% |
|  | Exar | F | 373 | 22 | 6\% | 341 | 24 | 7\% |
|  | ${ }_{\text {stait }}$ | SUM | 2691 | 1181 | 43.9\% | 1835 | 561 | 30.6\% |




Did apply sun screen
Did not apply sun screen

| Exposure <br> to the <br> Sun | Cancer | No cancer | \% of patients <br> with cancer | Cancer | No cancer | \% of patients <br> with cancer |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| a little | 1 | 19 | $5.0 \%$ | 3 | 37 | $7.5 \%$ |
| A LOT | 12 | 28 | $30.0 \%$ | 8 | 12 | $40.0 \%$ |
| Total | 13 | 47 | $\mathbf{2 1 . 7 \%}$ | 11 | 49 | $18.3 \%$ |







|  | Heart attack | No heart attack | \% of patients <br> with heart <br> attacks | Heart attack | No heart attack\% of patients <br> with heart <br> attacks |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Female | 1 | 19 | $5.0 \%$ | 3 | 37 | $7.5 \%$ |
| Male | 12 | 28 | $30.0 \%$ | 8 | 12 | $40.0 \%$ |
| Total | 13 | 47 | $21.7 \%$ | 11 | 49 | $18.3 \%$ |

Two drugs are tested on patients with a heart condition. The table shows the results of an experiment on a perfectly representative sample of patients. Which is correct (more than one)?
A. Males are less at risk when taking drug A (rather than B )
B. Females are less at risk when taking drug B (rather than A)
C. Overall, patients are less at risk when taking drug $A$ (rather than $B$ )
D. Overall, patients are less at risk when taking drug B (rather than A)

|  | Heart attack | No heart attack | \% of patients <br> with heart <br> attacks | Heart attack | No heart attack | \% of patients <br> with heart <br> attacks |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Female | 1 | 19 | $5.0 \%$ | 3 | 37 | $7.5 \%$ |
| Male | 12 | 28 | $30.0 \%$ | 8 | 12 | $40.0 \%$ |
| Total | $\mathbf{1 3}$ | $\mathbf{4 7}$ | $\mathbf{2 1 . 7 \%}$ | $\mathbf{1 1}$ | $\mathbf{4 9}$ | $\mathbf{1 8 . 3} \%$ |

Men more at risk

Type of drug

Controlling for gender,
Heart $\operatorname{drug} B \rightarrow$ more risk

|  | Drug A |  |  |  |  | Drug B |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Heart attack | No heart attack | \% of patients <br> with heart <br> attacks | Heart attack | No heart attack | \% patients <br> with heart <br> attacks |  |  |
| Low blood <br> pressure | 1 | 19 | $5.0 \%$ | 3 | 37 | $7.5 \%$ |  |
| High blood <br> pressure | 12 | 28 | $30.0 \%$ | 8 | 12 | $40.0 \%$ |  |
| Total | 13 | 47 | $21.7 \%$ | 11 | 49 | $18.3 \%$ |  |

Two drugs are tested on patients with a heart condition. The table shows the results of an experiment on a perfectly representative sample of patients. Which is correct (more than one)?
A. Drug $A$ is associated with lower blood pressure than $B$
B. Drug B is associated with lower blood pressure than A
C. Overall, patients are less at risk when taking drug A (rather than B)
D. Overall, patients are less at risk when taking drug B (rather than A)

|  | Heart attack | No heart attack | \% of patients <br> with heart <br> attacks | Heart attack | No heart attack | \% of patients <br> with heart <br> attacks |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Low blood <br> pressure | 1 | 19 | $5.0 \%$ | 3 | 37 | $7.5 \%$ |
| High blood <br> pressure | 12 | 28 | $30.0 \%$ | 8 | 12 | $40.0 \%$ |
| Total | $\mathbf{1 3}$ | $\mathbf{4 7}$ | $\mathbf{2 1 . 7 \%}$ | $\mathbf{1 1}$ | $\mathbf{4 9}$ | $\mathbf{1 8 . 3} \%$ |

## Blood pressure

High blood pressure $\rightarrow$ more risk

Controlling for blood pressure, drug $B \rightarrow$ more risk

## Heart attack

Simpson's Paradox:
a trend observed in a population disappears when partitioned to subgroups

OR Ov®n reverses



